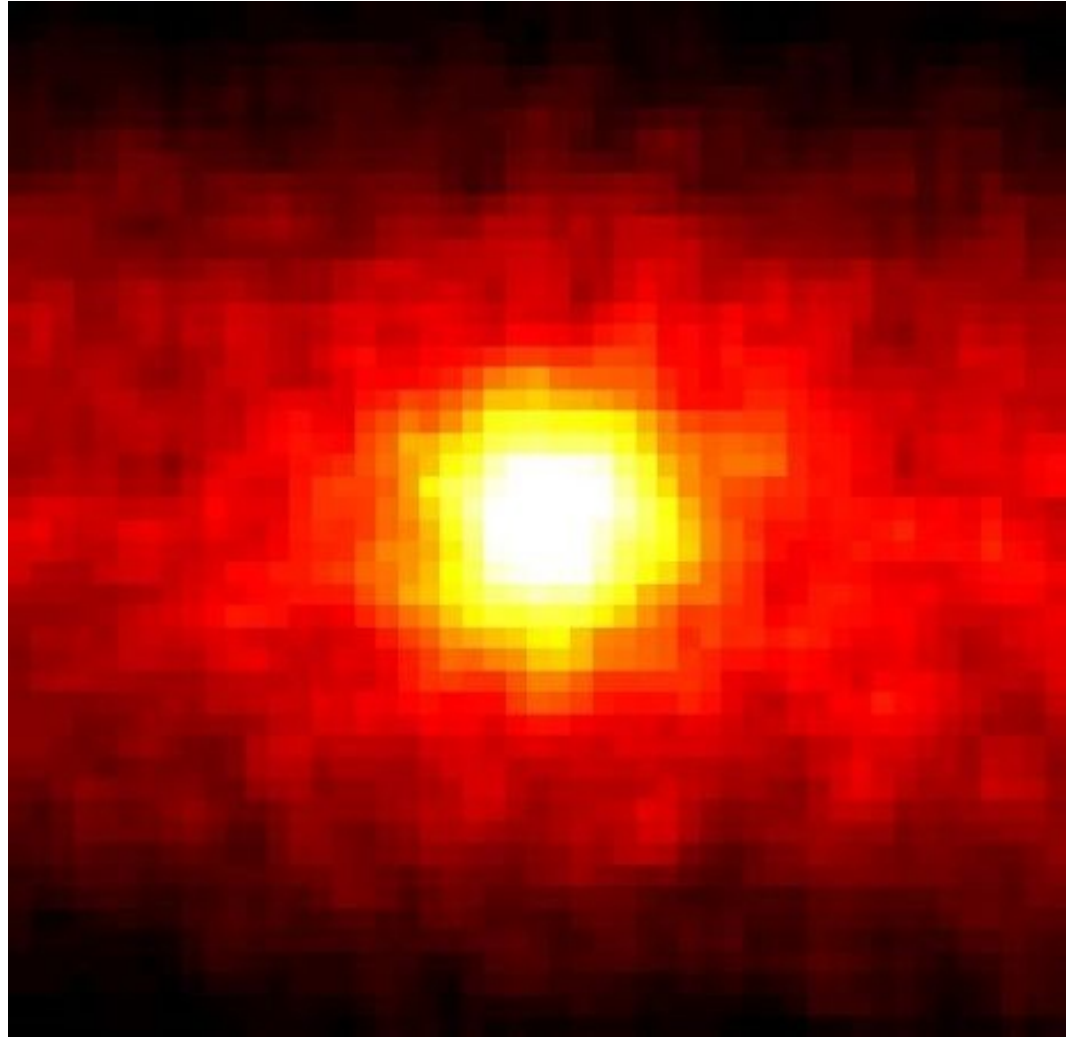


How does one know that
neutrinos have mass?

Aleksandra Adametz



History

In 1930:

Continuous spectrum of electrons from nuclear decays could not be explained

➡ New neutral particle postulated

In 1956:

First observation of neutrinos

Anti-electron-neutrinos detected in reaction

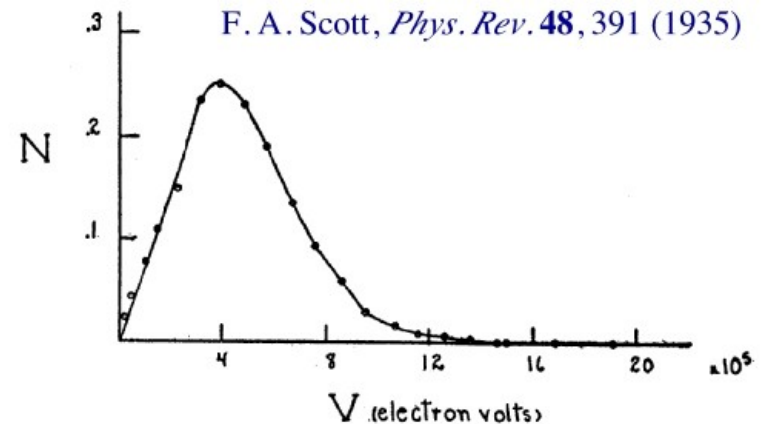
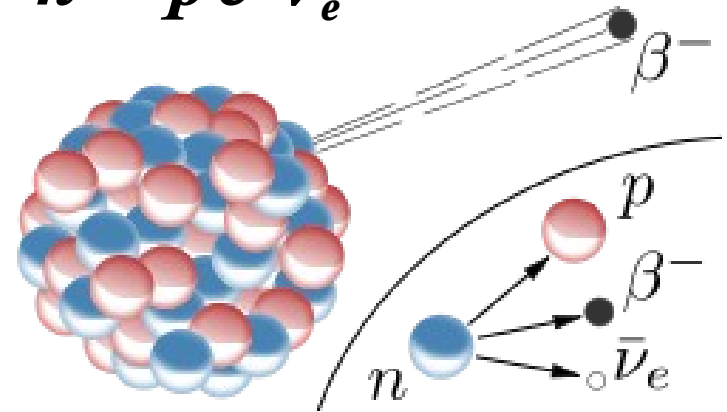
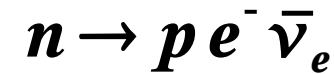
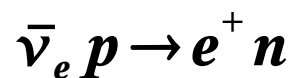


FIG. 5. Energy distribution curve of the beta-rays.

Standard Model

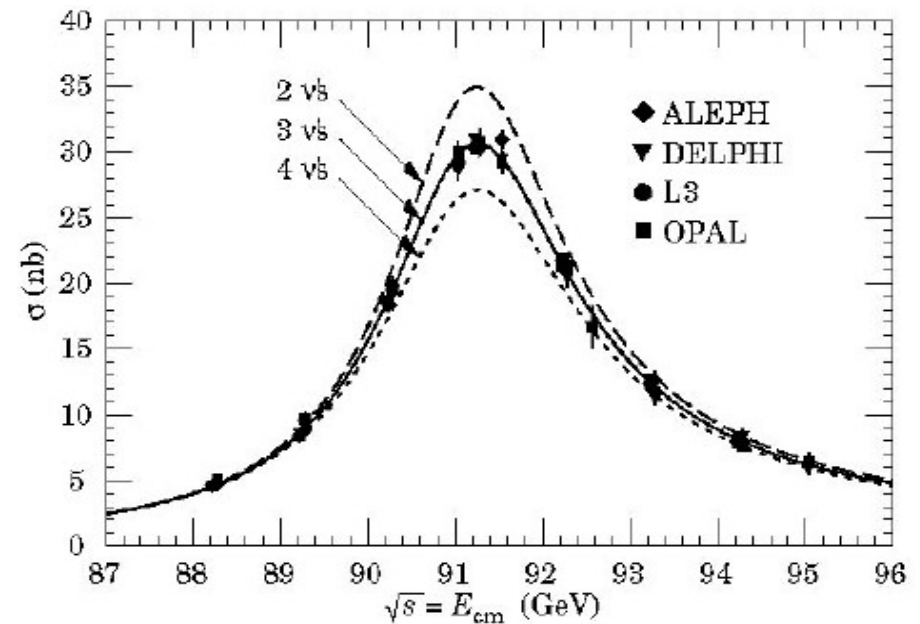
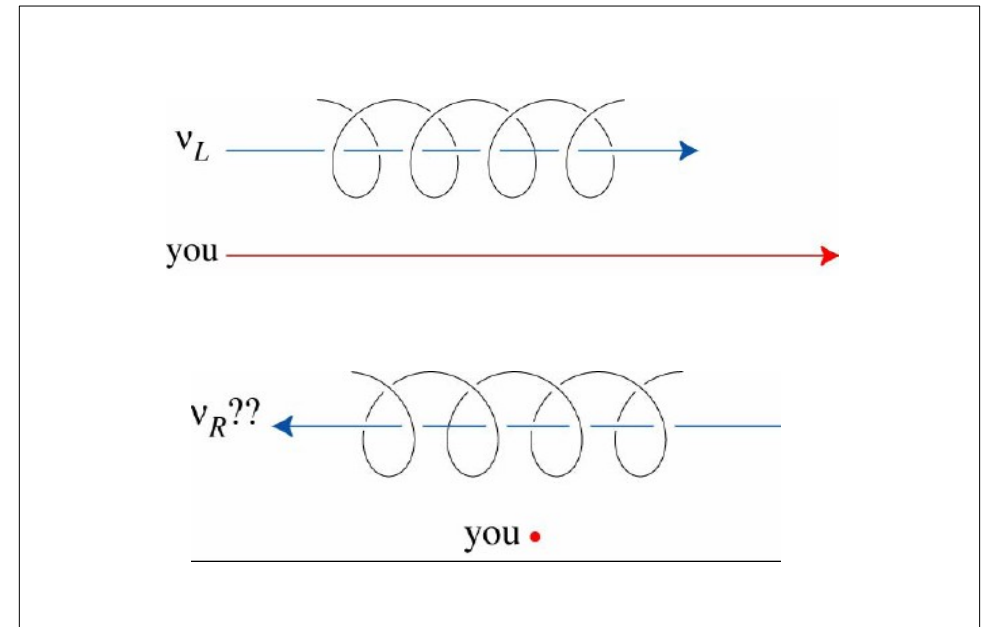
- neutrinos are always left-handed
right-handed neutrinos
never observed

➡ neutrinos are massless

- 3 types of neutrinos

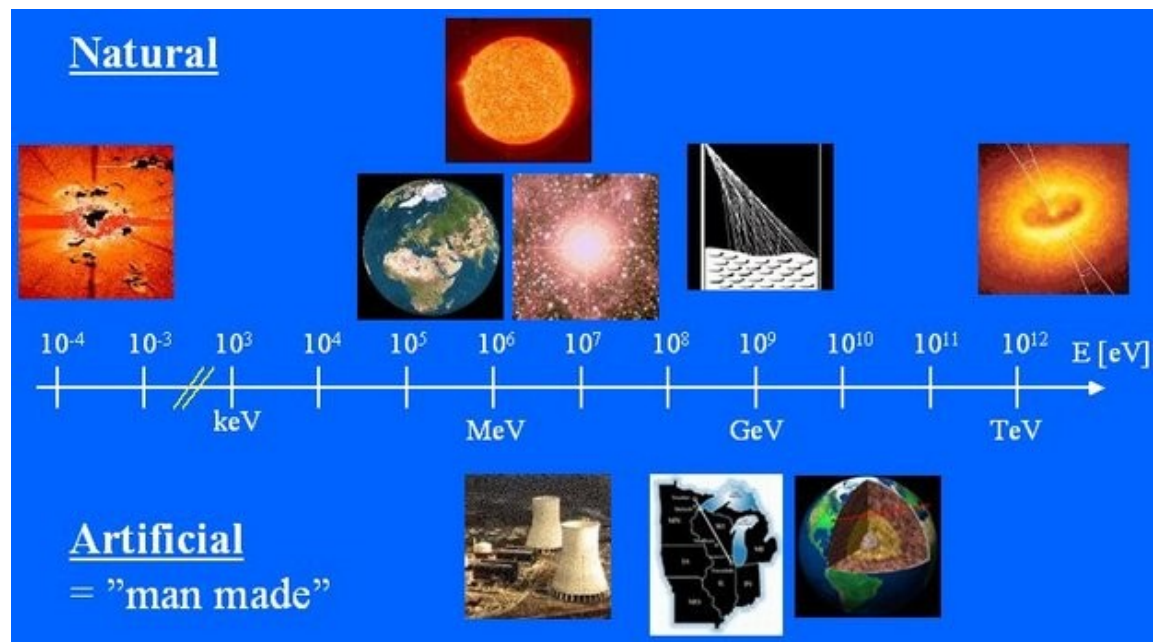
measurement of Z^0 -decays at LEP

$$\Gamma_Z = \Gamma_{\text{hadr}} + \Gamma_{l\bar{l}} + N_\nu \cdot \Gamma_{\nu\bar{\nu}}$$



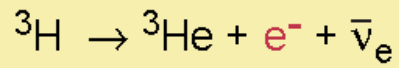
Neutrino Sources

- Sun
- Air showers (cosmic rays)
- “geoneutrinos” (e.g. decay of ^{238}U within the Earth)
- cosmic neutrino background
- Supernovae
- Accelerators
- Reactors



Direct Mass Measurements

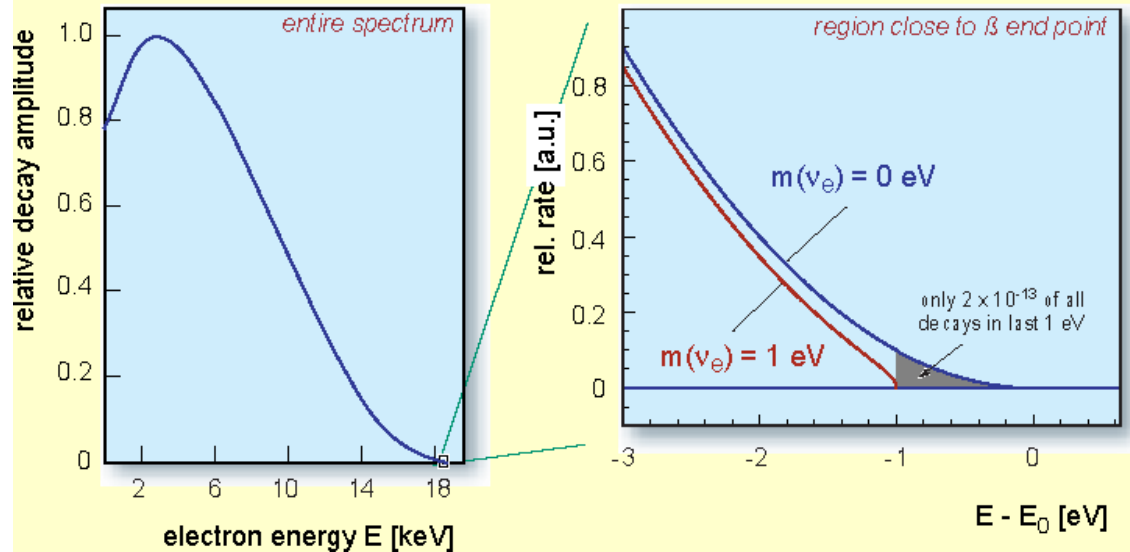
tritium β -decay and the neutrino rest mass



superaligned

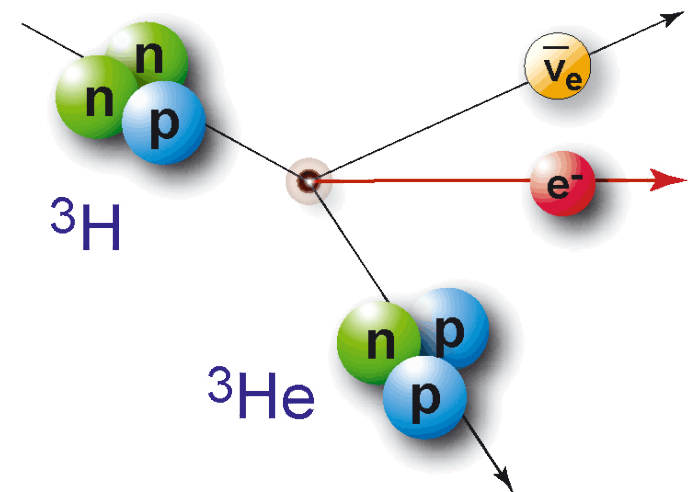
half life : $t_{1/2} = 12.32 \text{ a}$

β end point energy : $E_0 = 18.57 \text{ keV}$



Neutrino Mass Experiment:

- Mainz
- Troitsk
- KATRIN (future)



Upper limits on neutrino mass : $\sim 2 \text{ eV}$

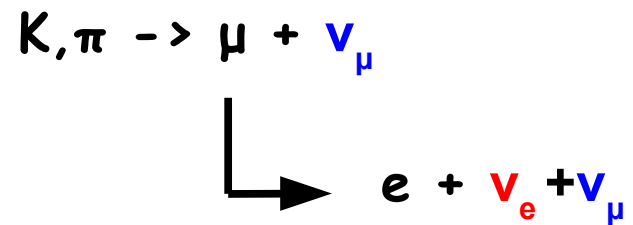
Atmospheric Neutrinos

Production process:

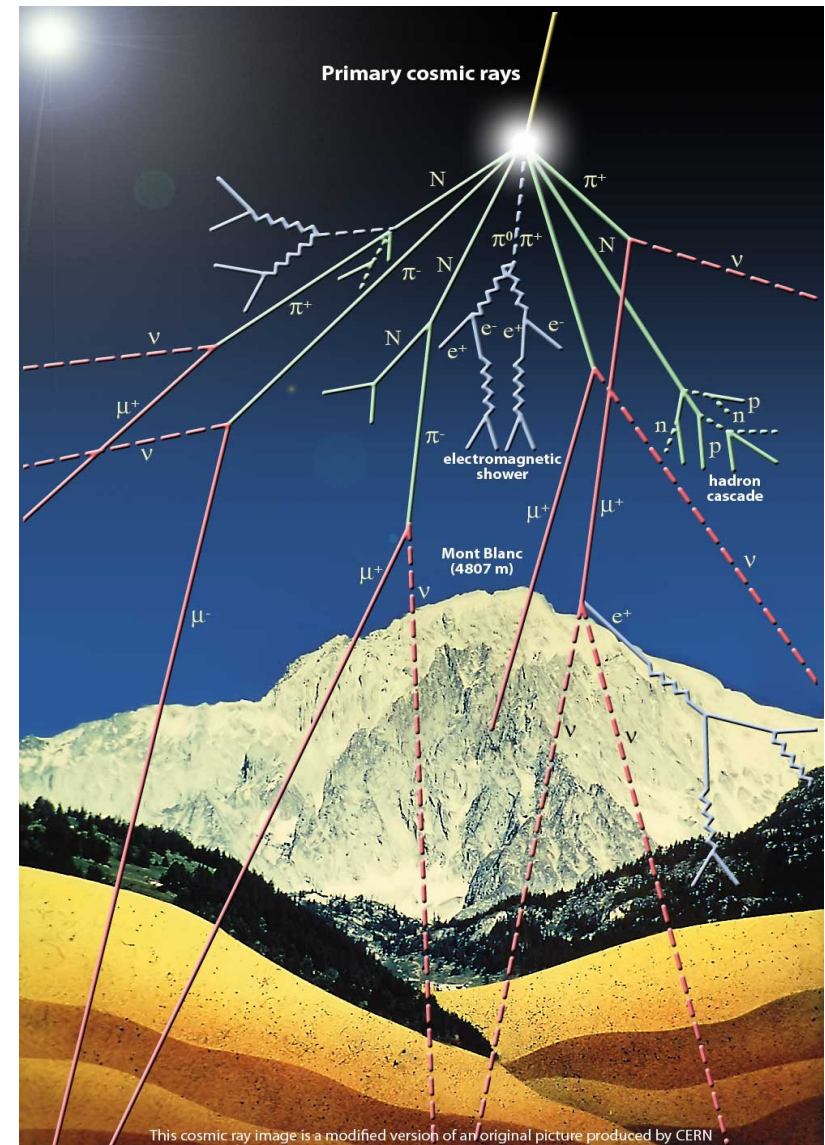
Proton collisions with nuclei

-> air showers

-> many charged Kaons and Pions



→ $N(\nu_\mu) / N(\nu_e) = 2$



SuperKamiokande

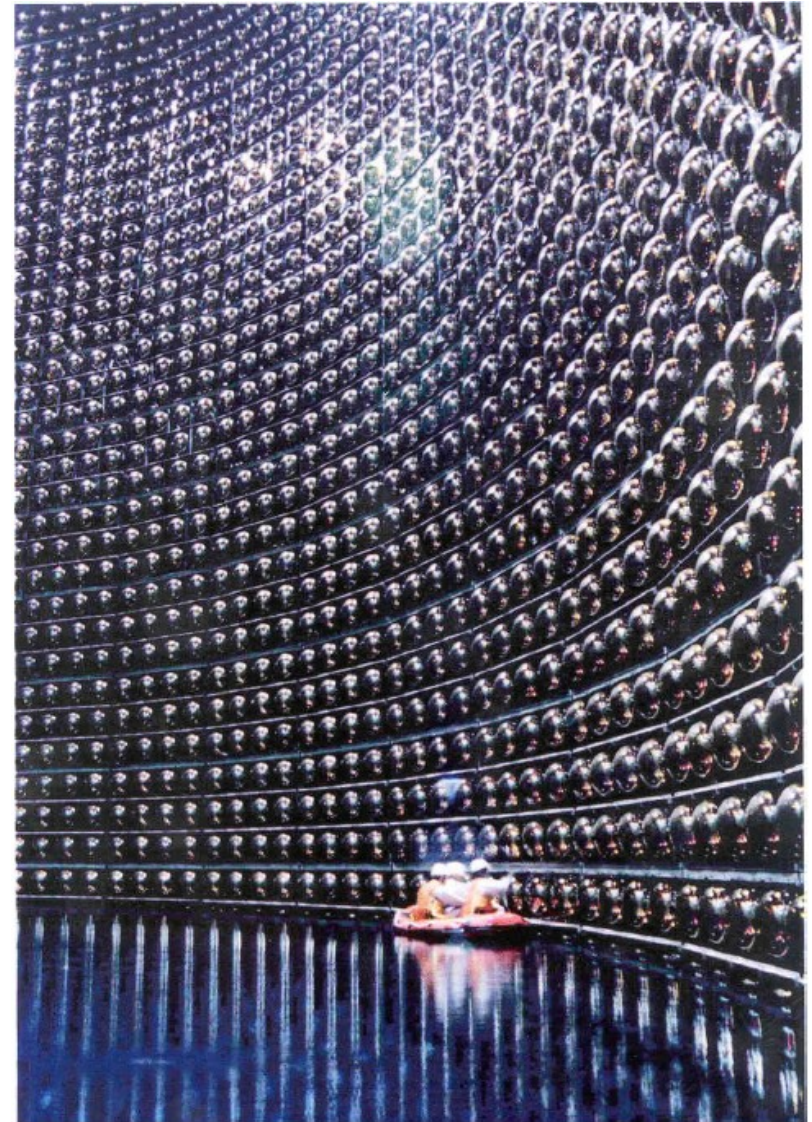
1998 First evidence for neutrino mass

Detector:

- 50k m³ H₂O
- ~13k PMTs (50 cm Ø)
- 1000 m underground

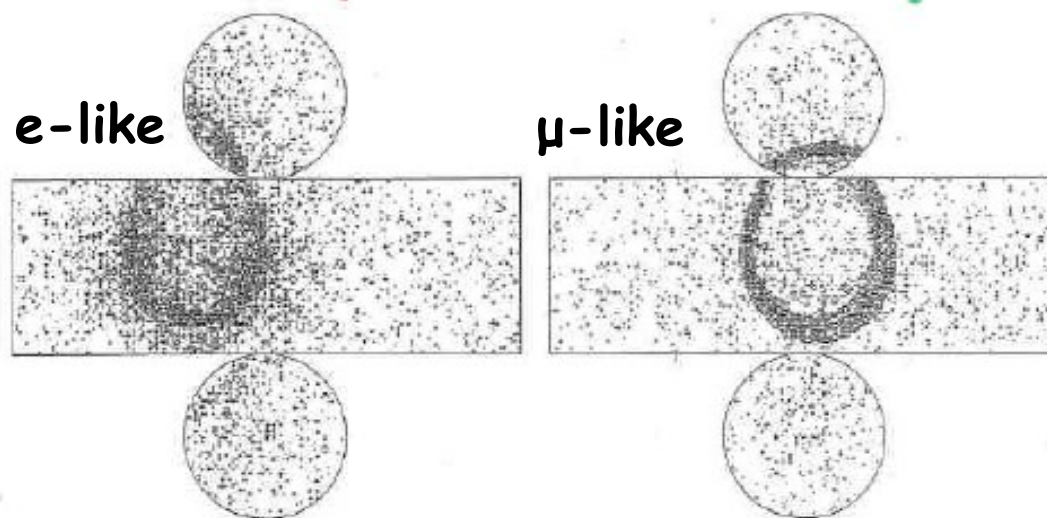
Principle:

- Reactions: $\nu n \rightarrow p l^-$
 $\bar{\nu} p \rightarrow n l^+$ ($l=e, \mu$)
- Lepton emits Cherenkov-light in water
- Cherenkov-light detected in PMTs
- For multi-GeV events:
neutrino direction \approx lepton direction



SuperKamiokande: Event Reconstruction

Ring-shape allows discrimination between e-like and μ -like events



Determination of $R = \left(\frac{\mu\text{-like}}{e\text{-like}} \right)_{Data} / \left(\frac{\mu\text{-like}}{e\text{-like}} \right)_{MC}$

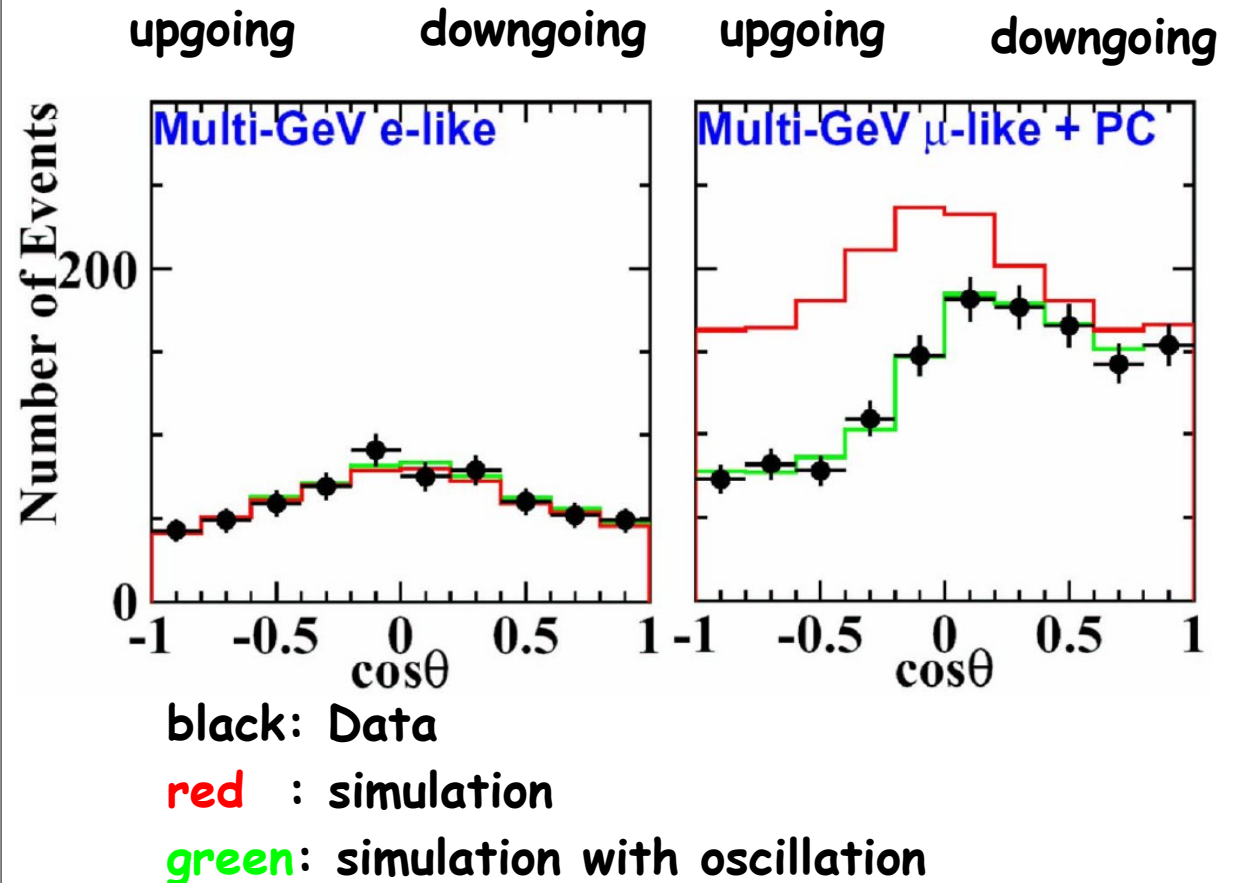
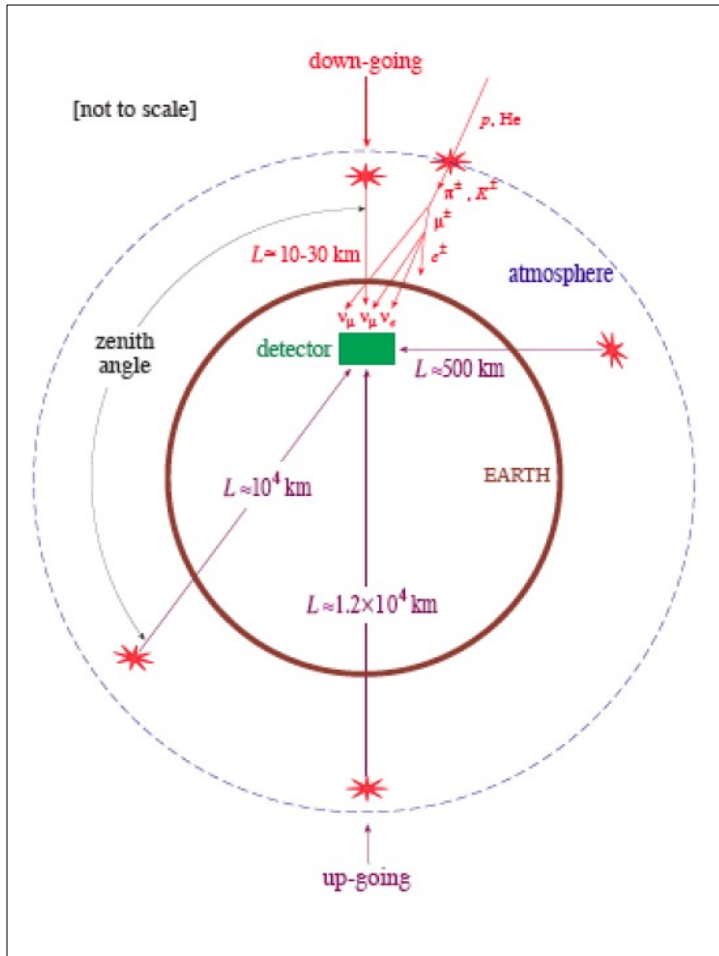
$$\frac{\mu\text{-like}}{e\text{-like}} = \frac{\nu_{\mu} + \bar{\nu}_{\mu}}{\nu_e + \bar{\nu}_e}$$

Prediction : $R = 1$

Measured : $R = 0.6$

➡ missing ν_{μ} or too many ν_e ?

SuperKamiokande: Zenith-angle dependence



Explanation for deficit: \longrightarrow Oscillation \longrightarrow Neutrino has mass!

From reactor neutrino experiments: Limits on $\nu_\mu \rightarrow \nu_e$

Conclusion: Oscillation is $\nu_\mu \rightarrow \nu_\tau$

Oscillation Formalism

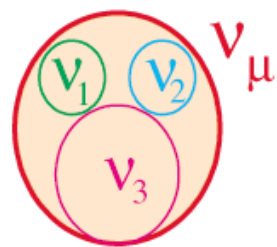
- **Flavor eigenstates** expressed as superpositions of **mass eigenstates**:

$$|\nu_l\rangle = \sum_i U_{li} |\nu_i\rangle \quad l=e, \mu, \tau; \quad i=1,2,3$$

- States ν_i propagate in dependence of distance L (assumed $E \gg m_i$):

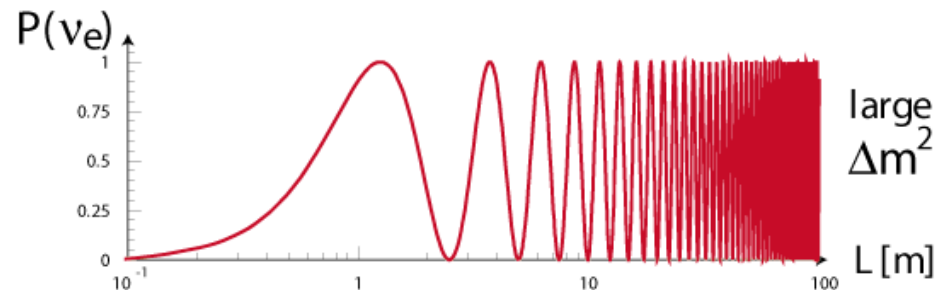
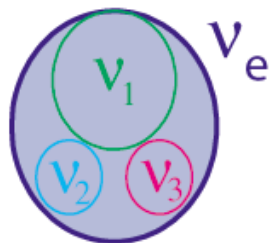
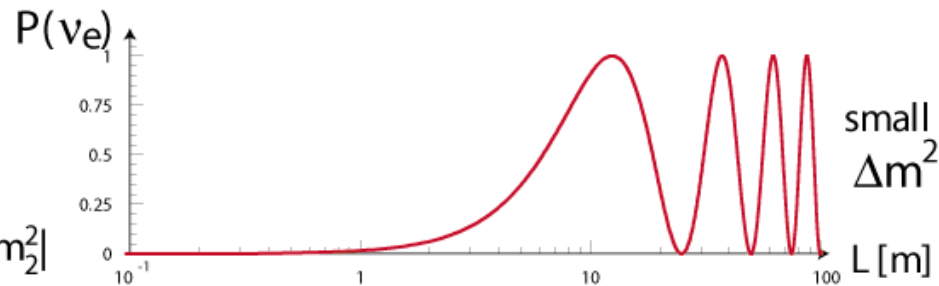
$$|\nu(L)\rangle \sim |\nu_i(L=0)\rangle \exp\left(-i \frac{m_i^2 L}{2E}\right)$$

- Oscillation Probability (assumed that only two flavors exist):



$$P(\nu_\mu \rightarrow \nu_e) = A \cdot \sin^2(1.27 \cdot \Delta m^2 \cdot L / E_\nu)$$

L, t
 $A = \sin^2(2\Theta)$
 $\Delta m^2 = |m_1^2 - m_2^2|$



Three neutrino types mixing matrix

$$(c_{ij} = \cos\Theta_{ij}, s_{ij} = \sin\Theta_{ij})$$

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

By observing oscillations (measuring oscillation probabilities) one can determine:

- 3 mixing angles: $\Theta_{12}, \Theta_{23}, \Theta_{13}$
- 2 mass squared differences $\Delta m_{21}^2, \Delta m_{31}^2$
- CP violating phase

• U corresponds to CKM-matrix but :

$$U = \begin{bmatrix} \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \end{bmatrix}$$

$$CKM = \begin{bmatrix} 1 & \blacksquare & \blacksquare \\ \blacksquare & 1 & \blacksquare \\ \blacksquare & \blacksquare & 1 \end{bmatrix}$$

Results from atmospheric neutrinos

SuperKamiokande:

$$1.9 \times 10^{-3} \text{ eV}^2 < \Delta m_{\text{atm}}^2 < 3.0 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\Theta_{\text{atm}} > 0.90$$

$$(36^\circ < \Theta_{\text{atm}} < 53^\circ)$$

Other experiments:
consistent results

- No information about sign of Δm_{atm}^2
- Lower bound on heaviest neutrino mass m_h from $m_h \geq \sqrt{\Delta m_{\text{atm}}^2}$:

$$m_h > 0.04 \text{ eV}$$

Accelerator Neutrinos: K2K experiment

long baseline experiment

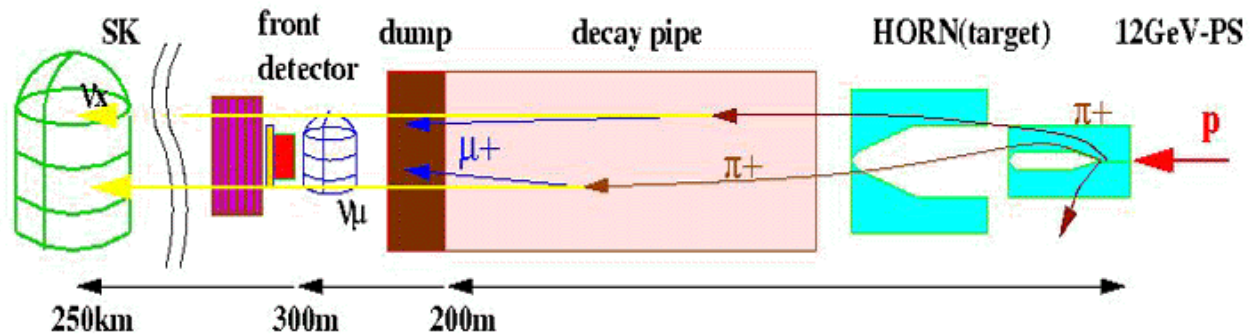
Muon-Neutrino beam ($E_\nu \sim 1\text{GeV}$):

- 12 GeV proton beam on target
 - > Kaon and pions
 - > K, π decay to $\mu + \nu_\mu$
 - > muons stopped



Detection of neutrino events:

- in "Near Detector"
- in "SuperKamiokande"



L/E_ν such that Δm_{atm} observable

Result:

158 events expected without oscillation
122 events found

➡ vanishing ν_μ

determined Δm_{atm} consistent with
other measurement

Solar Neutrinos

Production Mechanism:

Several reactions e.g.

$$pp: p+p \rightarrow D+e^++\nu_e \quad E_\nu < 0.42 \text{ MeV}$$

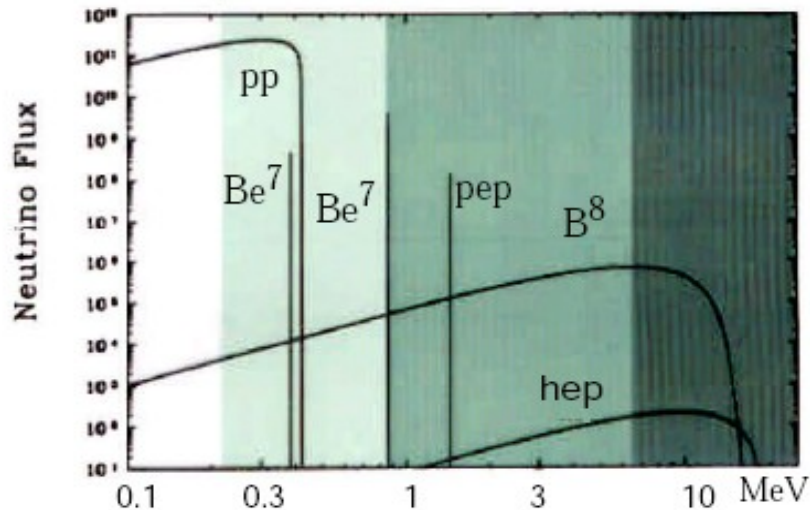
$$\text{Be}^7: \text{Be}^7 + e^- \rightarrow \text{Li}^7 + \nu_e \quad E_\nu = 0.86 \text{ MeV}$$

$$\text{B}^8: \text{B}^8 \rightarrow \text{Be}^8 + e^+ + \nu_e \quad E_\nu < 14.6 \text{ MeV}$$



only electron-neutrinos

SSM (Standard Solar Model) Neutrino Flux Prediction



Several experiments sensitive to
a different energy range measure
deficit in electron-neutrino flux:

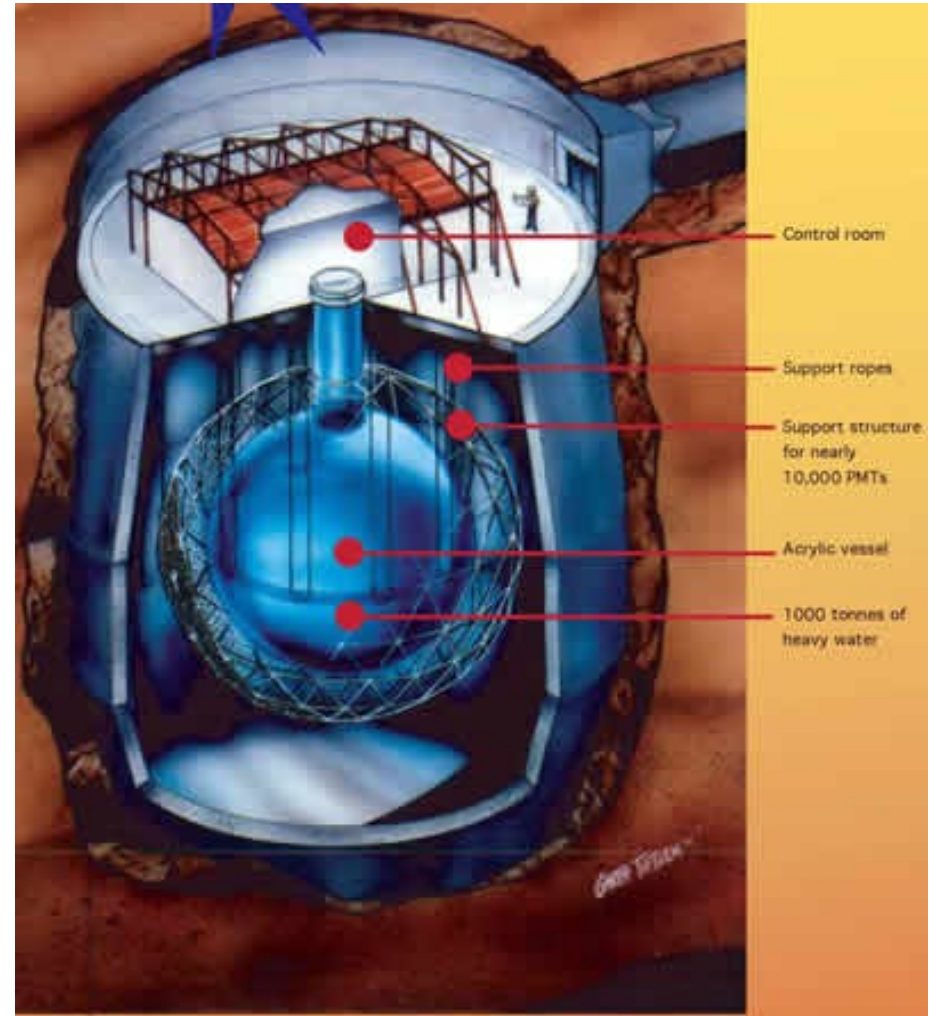
-> neutrino oscillations ?

-> SSM wrong ?

SNO Experiment

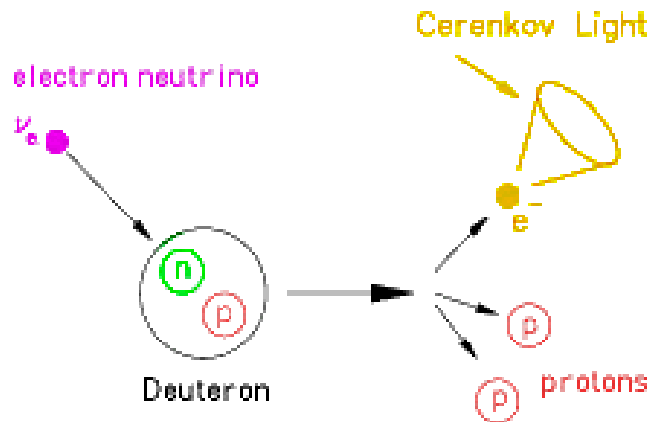
(Sudbury Neutrino Observatory, Kanada)

- ~2000m under ground (~6000 m.w.e)
- 12m diameter acrylic vessel
- 1000t of heavy water
- 2t of salt
(Chlorine as neutron absorber)
- 7000 t water
- 9600 PMTs

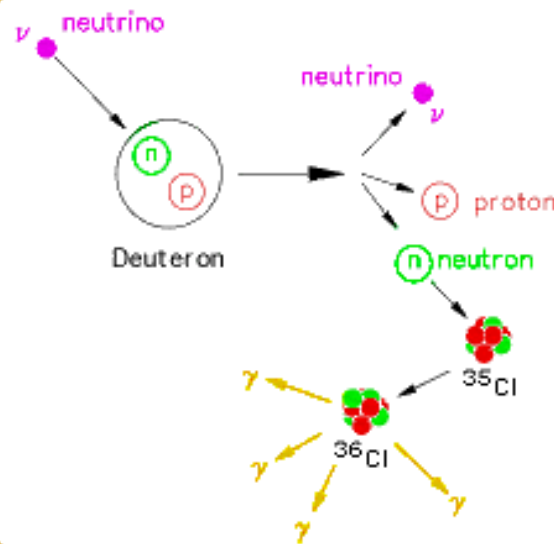
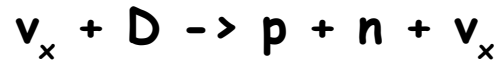


SNO Measurement

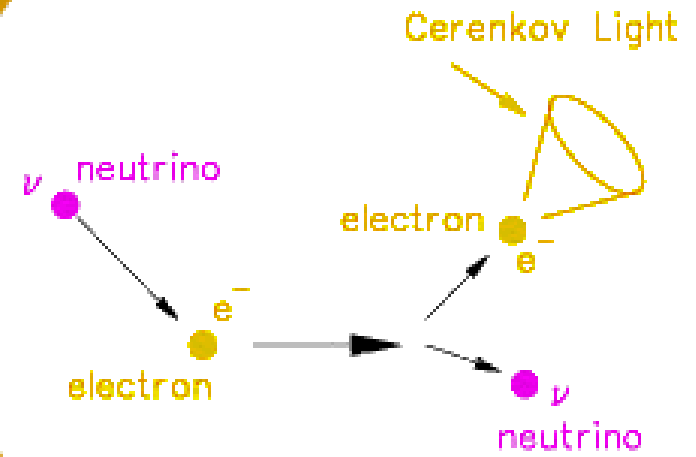
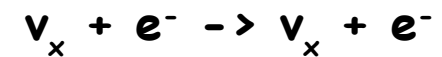
Charged Current:



Neutral Current:

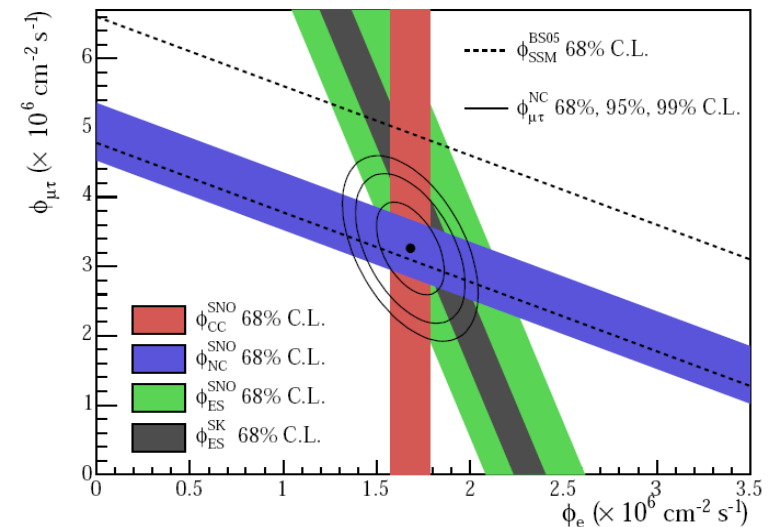


Electron Scattering:



Comparison of the fluxes gives

- evidence for $\nu_e \rightarrow \nu_\mu, \nu_\tau$ oscillation
- consistence with SSM
- consistence with other experiments



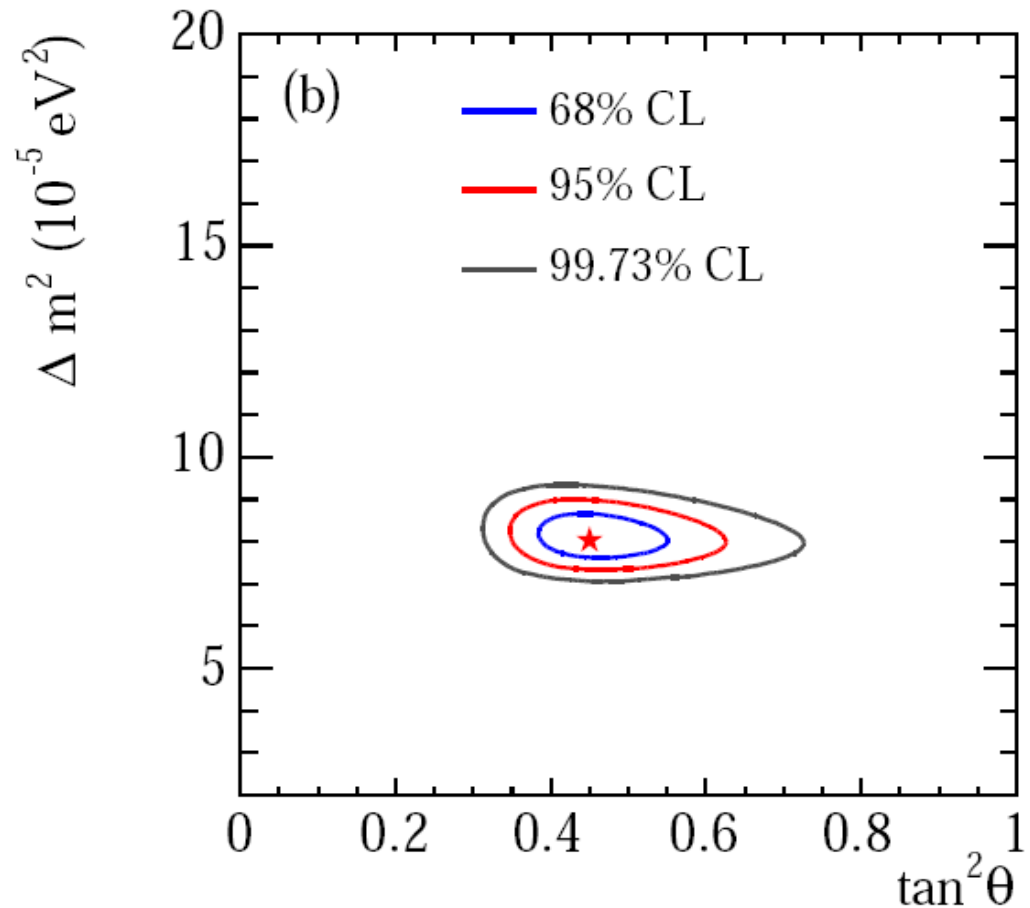
Results From Solar Neutrinos

$$\Delta m_{\text{sol}}^2 = 8.0^{+0.4}_{-0.3} \times 10^{-5} \text{ eV}^2$$

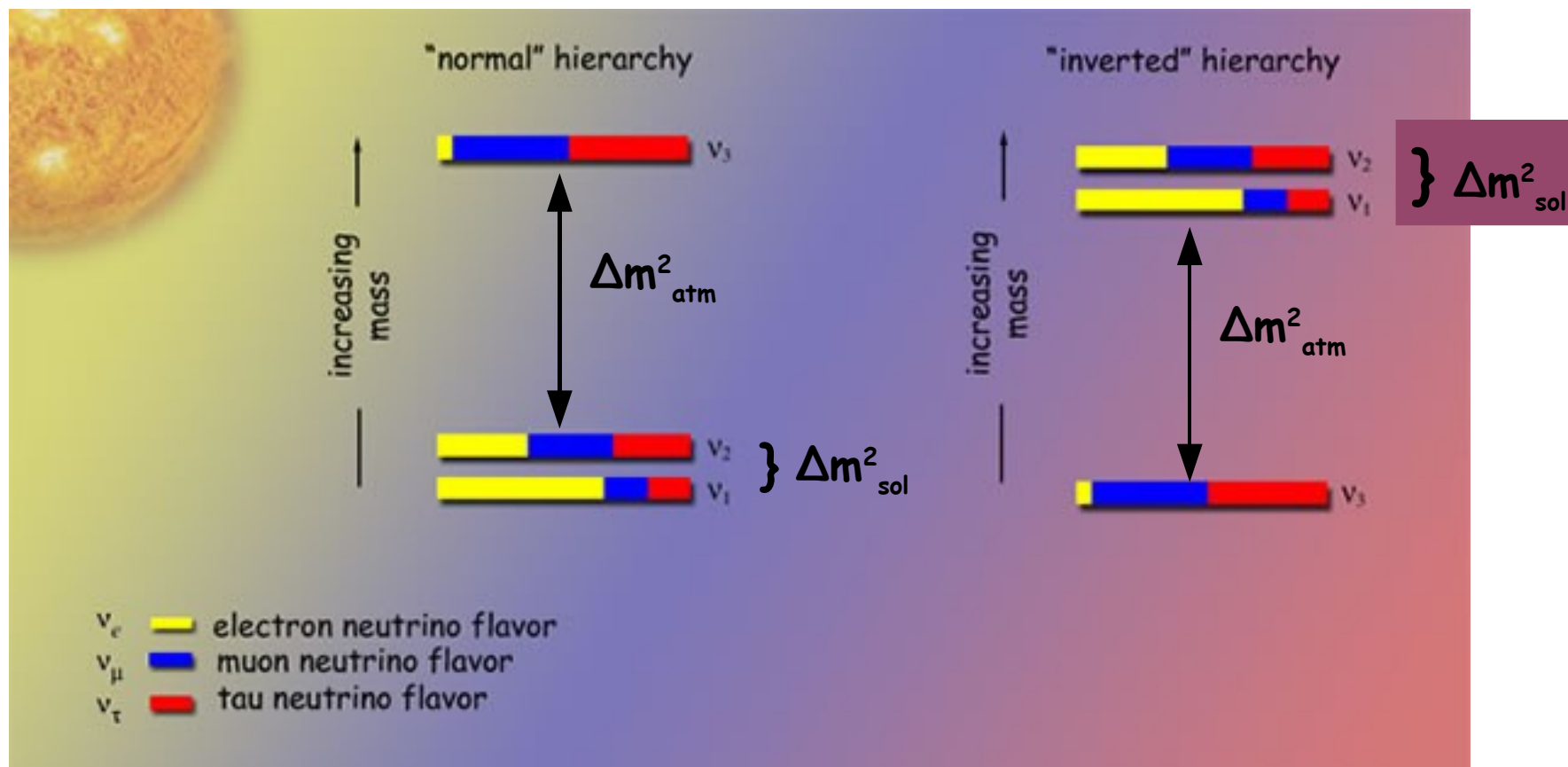
$$\Theta_{\text{sol}} = 33.9 \pm 1.6^\circ$$

- Better determined than Δm_{atm}^2
- Due to predicted matter-effects in sun:

→ sign of Δm_{sol}^2 is known



Three neutrino squared-mass spectrum



Many other neutrino-experiments to answer open questions

- What is the real Δm hierarchy ?
- What are the absolute masses ?
- Are there more neutrino types ?
(sterile neutrinos)
- Are neutrinos and anti-neutrinos identical ?
(Dirac or Majorana)
- Is there CP-violation ?
(determination of small mixing angle Θ_{13})

