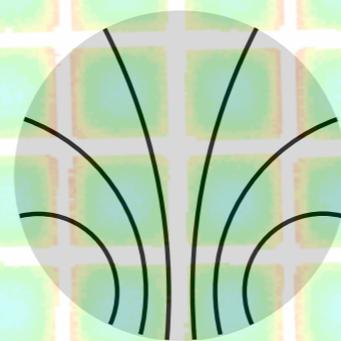


Characterization of Silicon Photomultipliers



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IRTG Seminar 05.02.2010



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Outline

- Applications
 - Calorimetry at the ILC
 - Positron Emission Tomography
- Silicon Photomultipliers (SiPM)
 - Basic Properties
 - SiPM Characterization
- Summary

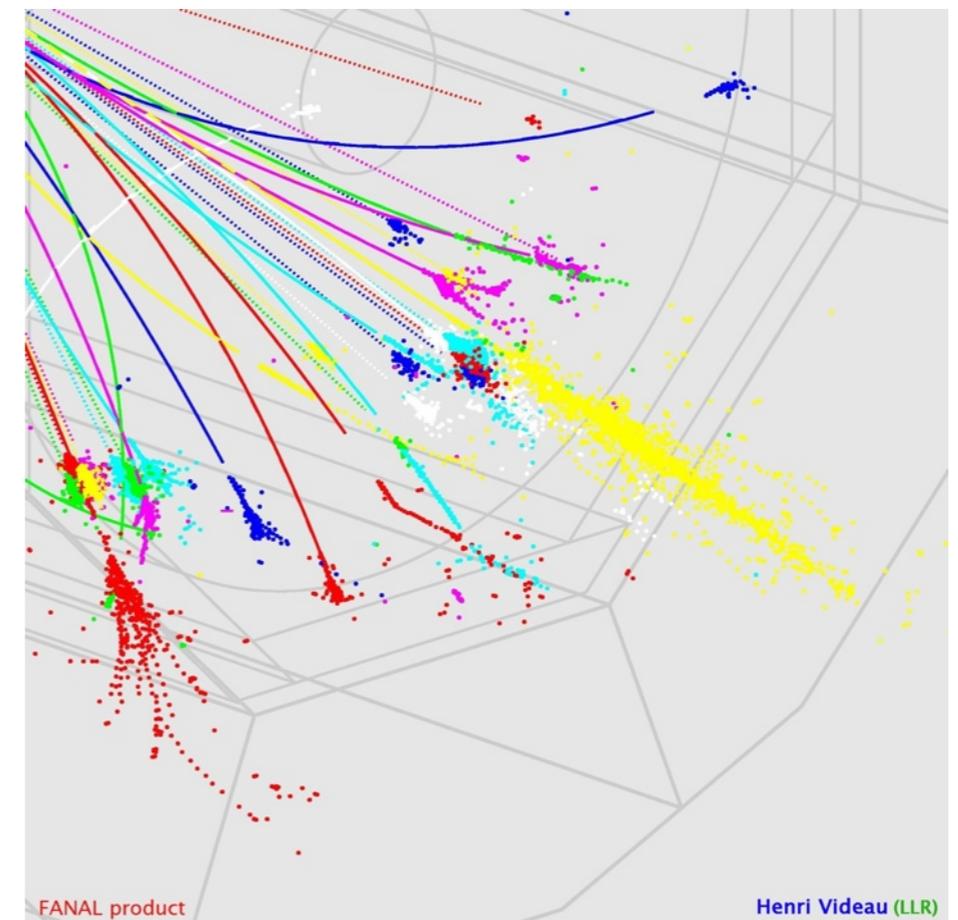
Calorimetry at the ILC

- ILC: future $e^+ e^-$ collider for precision measurements of the LHC physics
- ILC physics require excellent jet-energy resolution

- Challenging goal:

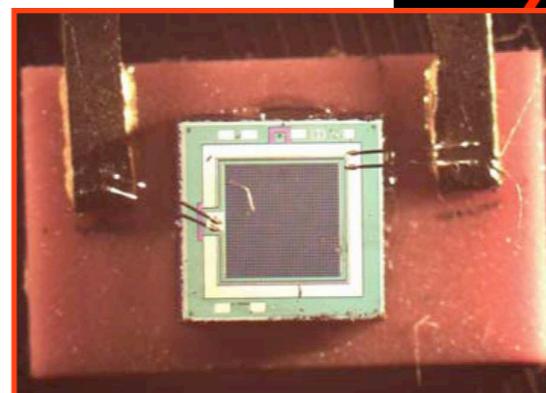
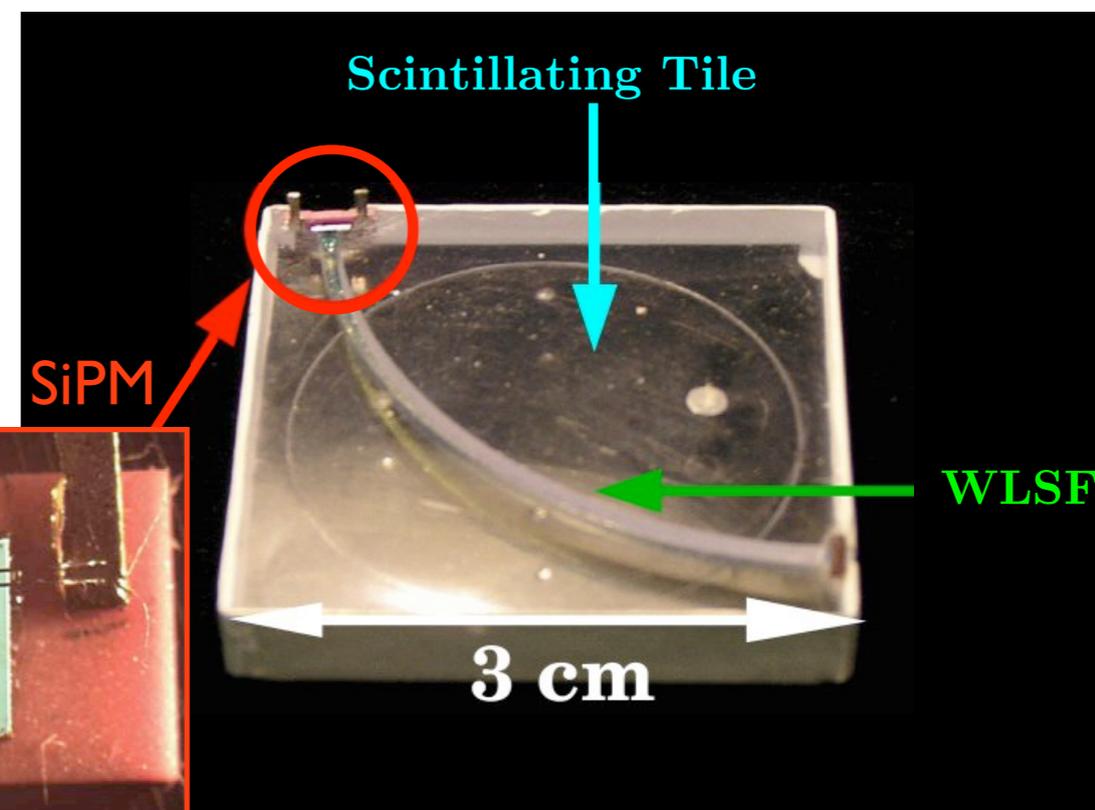
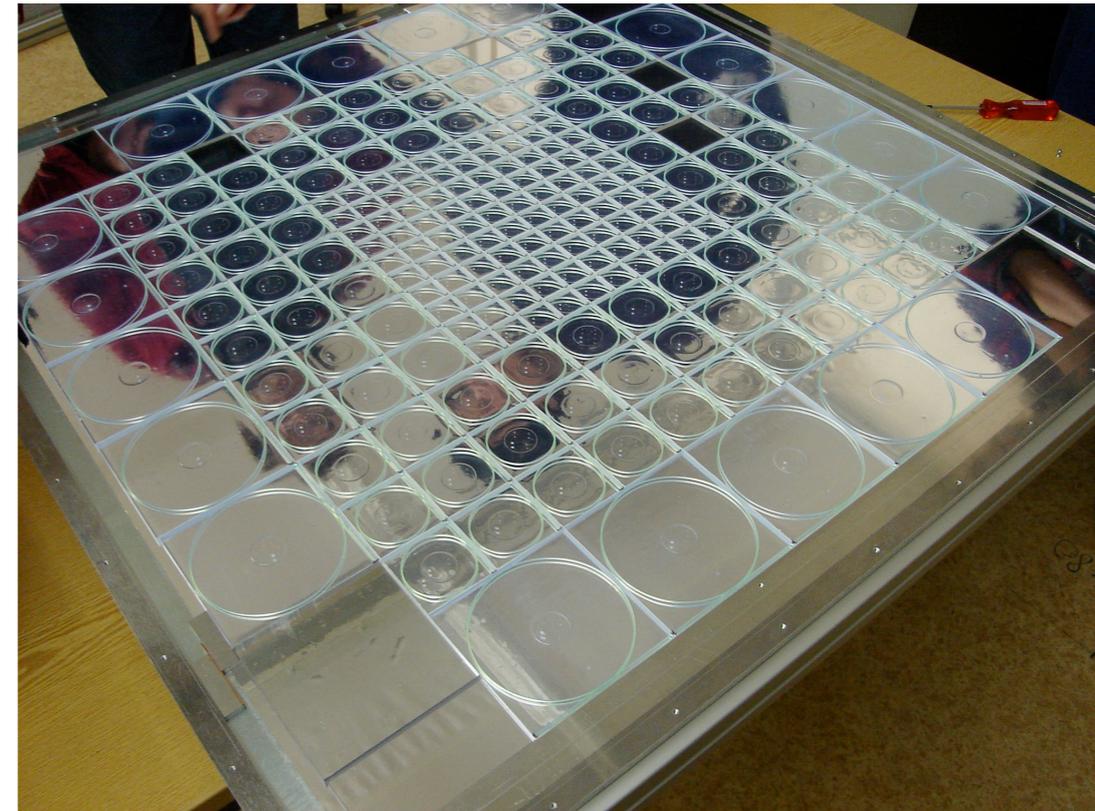
$$\sigma_{E_{jet}}/E_{jet} = 30\%/\sqrt{E_{jet}}$$

- ➔ Highly granular „imaging“ calorimeters

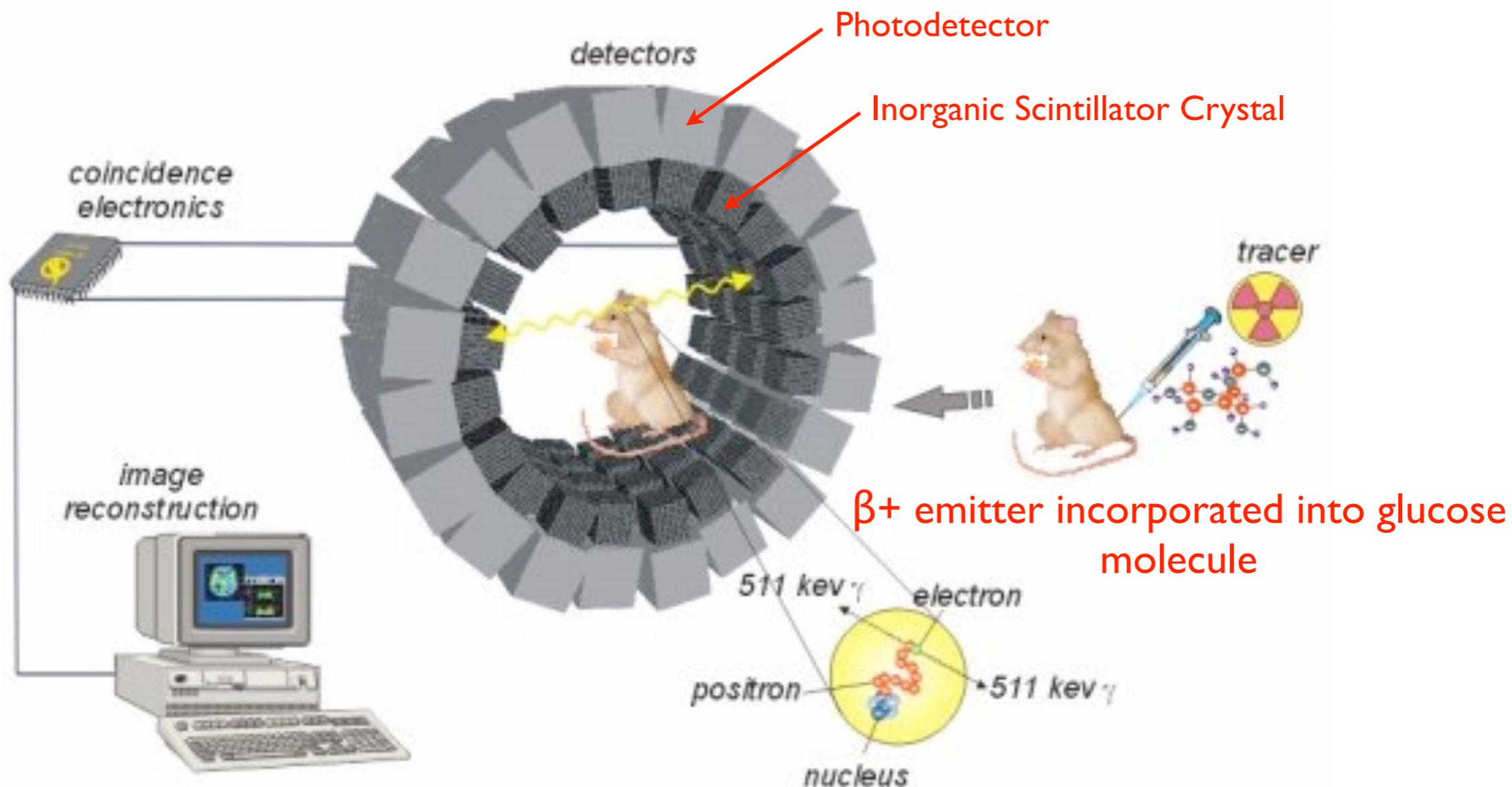


HCAL Prototype

- Sandwich calorimeter with plastic scintillator (blue scintillation light)
- 1 m³ Prototype made of 38 Layers 216 Channels per Layer
- 3x3x0.5cm³ tiles
- Wavelength shifting fiber collects the scintillation light and converts it into green light
- Tiles are read out with *Silicon Photomultipliers*:
 - Very compact
 - Insensitive to magnetic fields

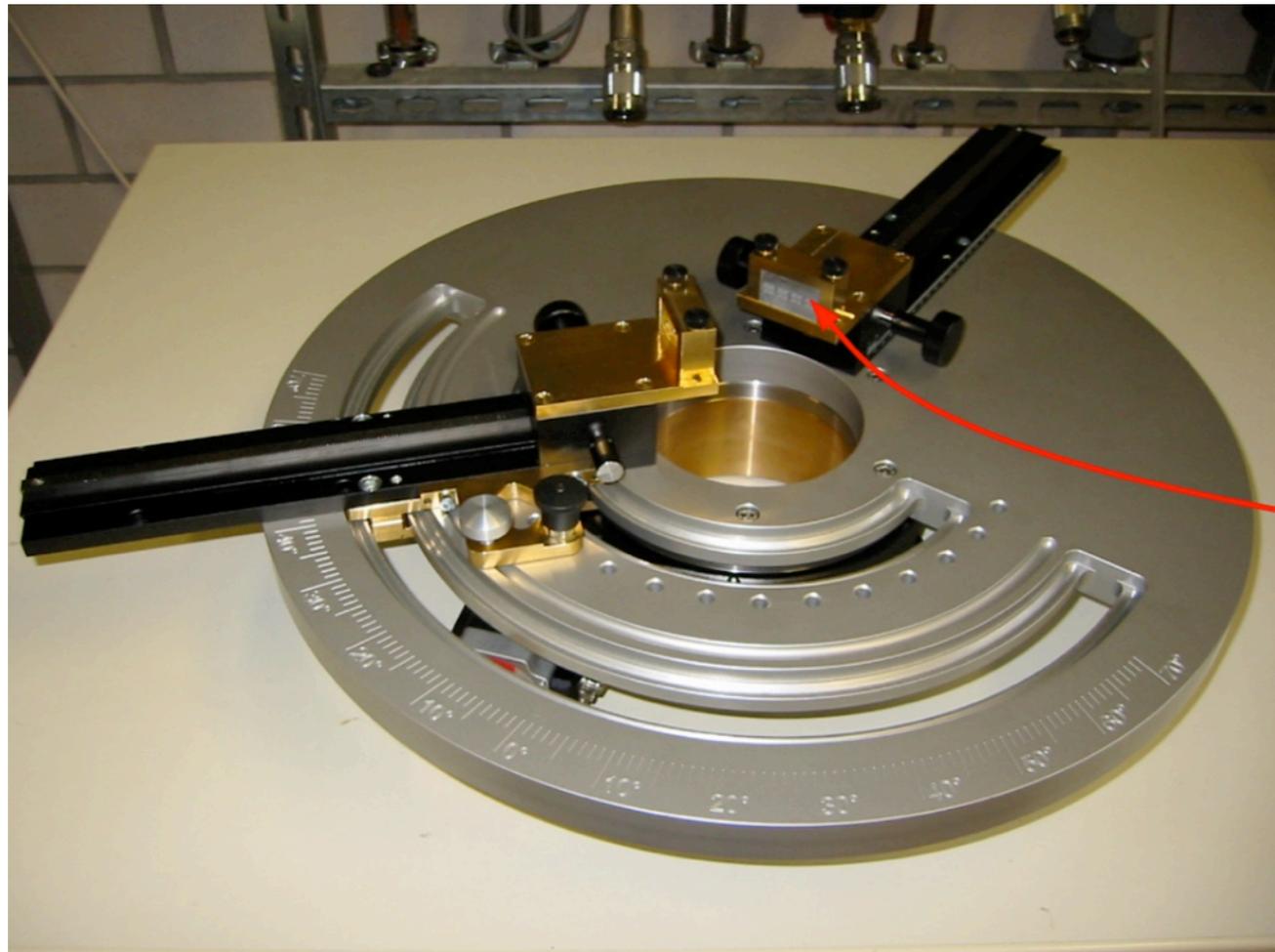


Positron Emission Tomography

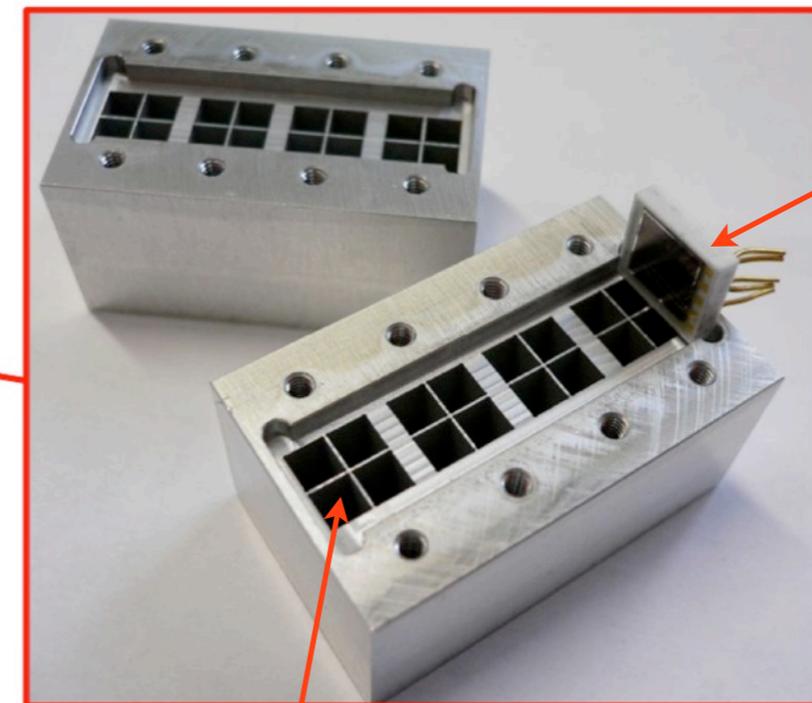


- Advantages of a PET with SiPM readout:
 - Small size \Rightarrow allows high granularity
 - Insensitivity to B-fields \Rightarrow allows combination with MRI
 - Good timing resolution \Rightarrow Time of Flight PET

PET Prototype



Detector matrix:

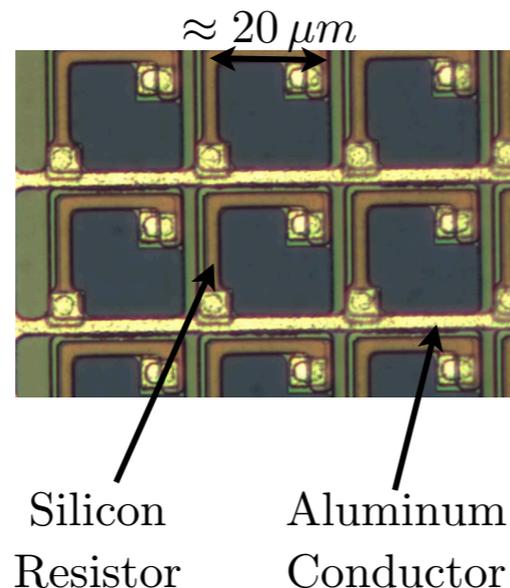
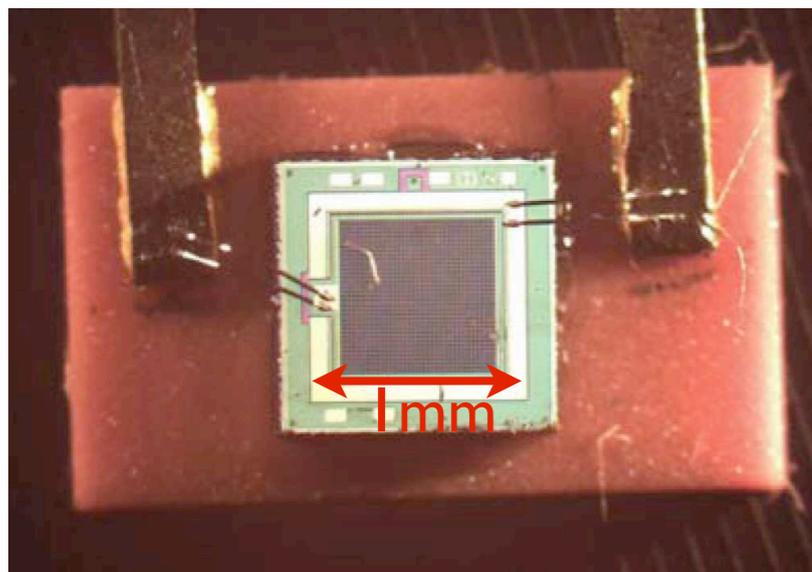


SiPM

LFS crystals

- PET prototype built in KIP workshop
- Two detector head with 4x4 channels (LFS crystals) read out by SiPMs
- Can be rotated to simulate 360° detector

The Silicon Photomultiplier



- Array of APDs (typ. 1000 per mm²) connected to a common output
- APDs operated in „Geiger mode“ ($V_{\text{bias}} > V_{\text{breakdown}}$):
 - Free charge carrier can trigger „avalanche“ in the high field region
 - ➔ Gain $\sim 10^6$

- Avalanche is self-sustaining and has to be stopped (quenched)

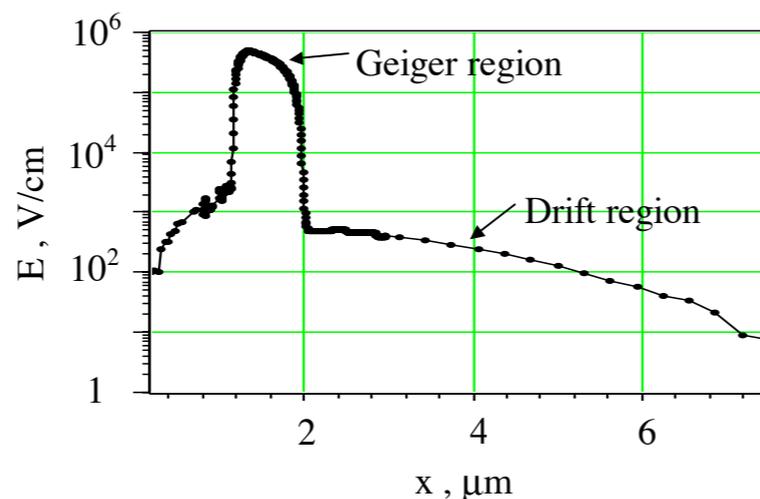
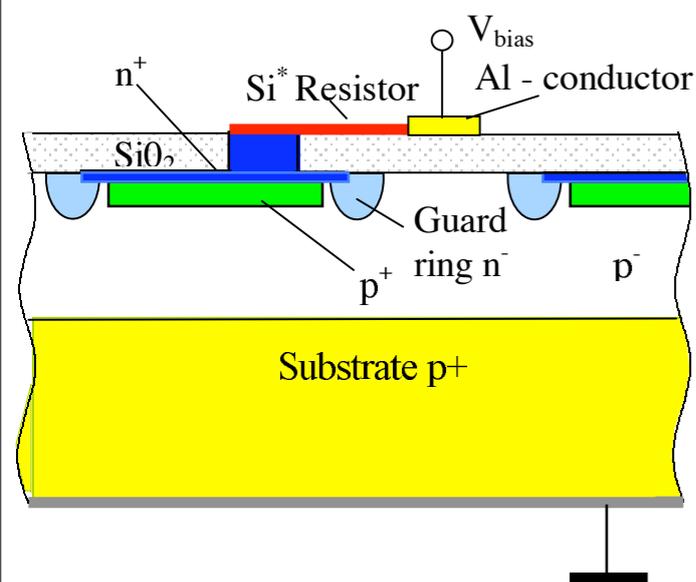
- APD signal independent from number of photons (only „yes/no“ information)

- Output signal = sum of all APD signals

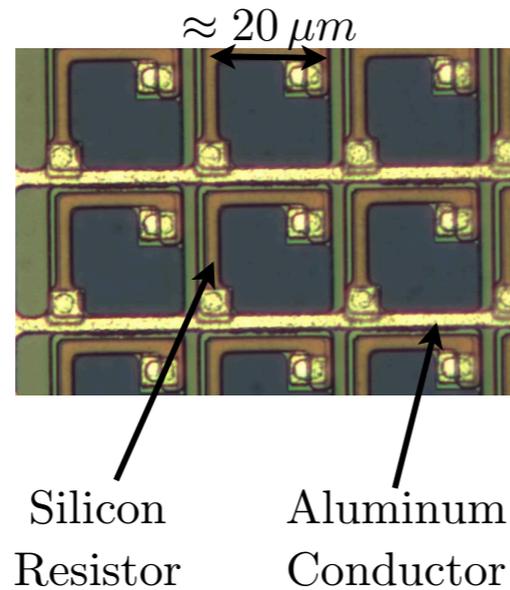
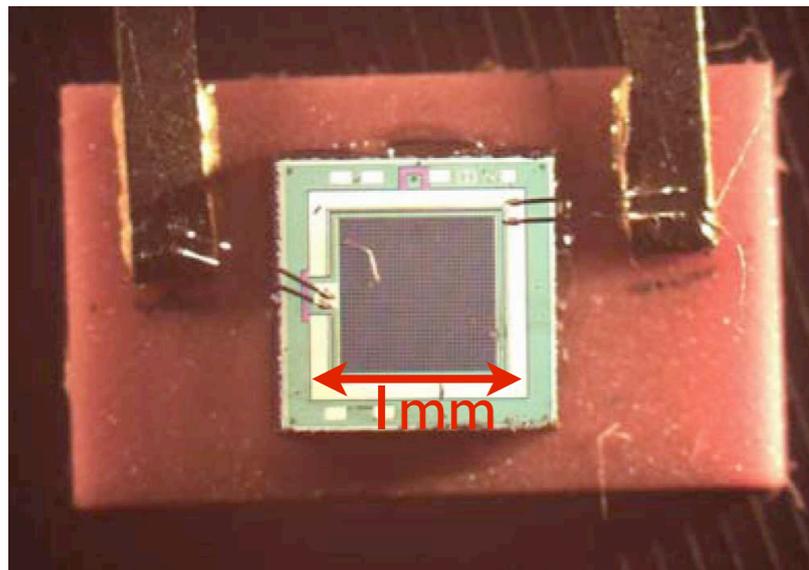
- Dynamic range limited by number of pixels:

- $N_{\gamma} \ll N_{\text{pixels}}$: linear response

- $N_{\gamma} \approx N_{\text{pixels}}$: saturation



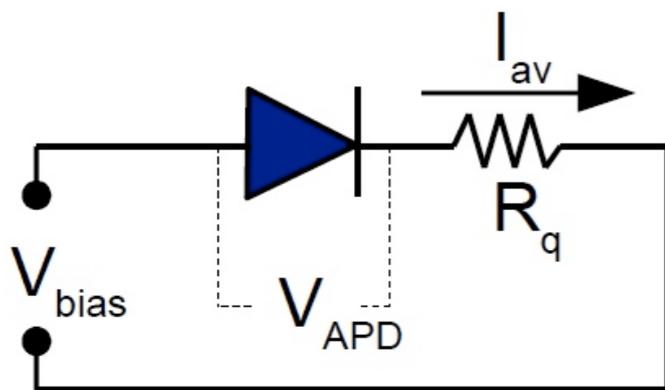
Quenching



- Avalanche is self sustaining and has to be stopped (quenched)

Passive quenching:

- APD is connected to resistance in series
- ➔ Voltage at APD drops below $V_{\text{breakdown}}$ during avalanche breakdown
- Recovery time = $R_q C$

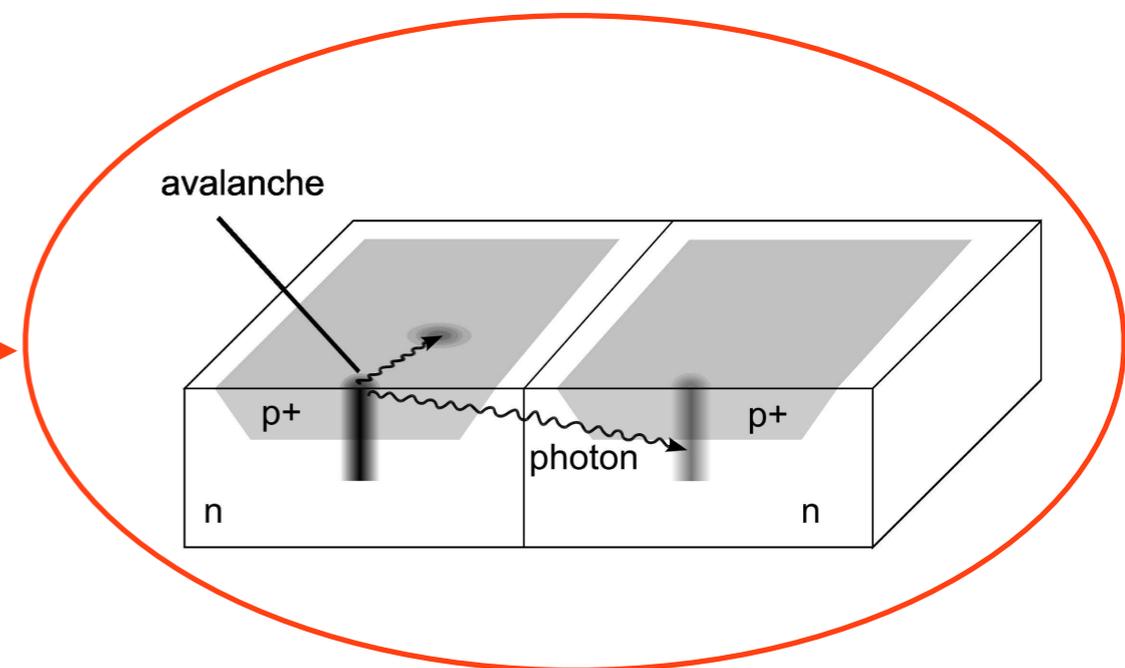
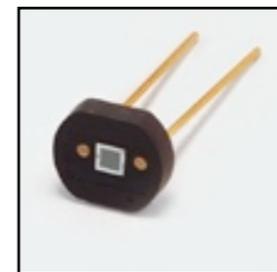


$$V_{\text{APD}} = V_{\text{bias}} - R_q I_{\text{av}}$$

Basic Properties

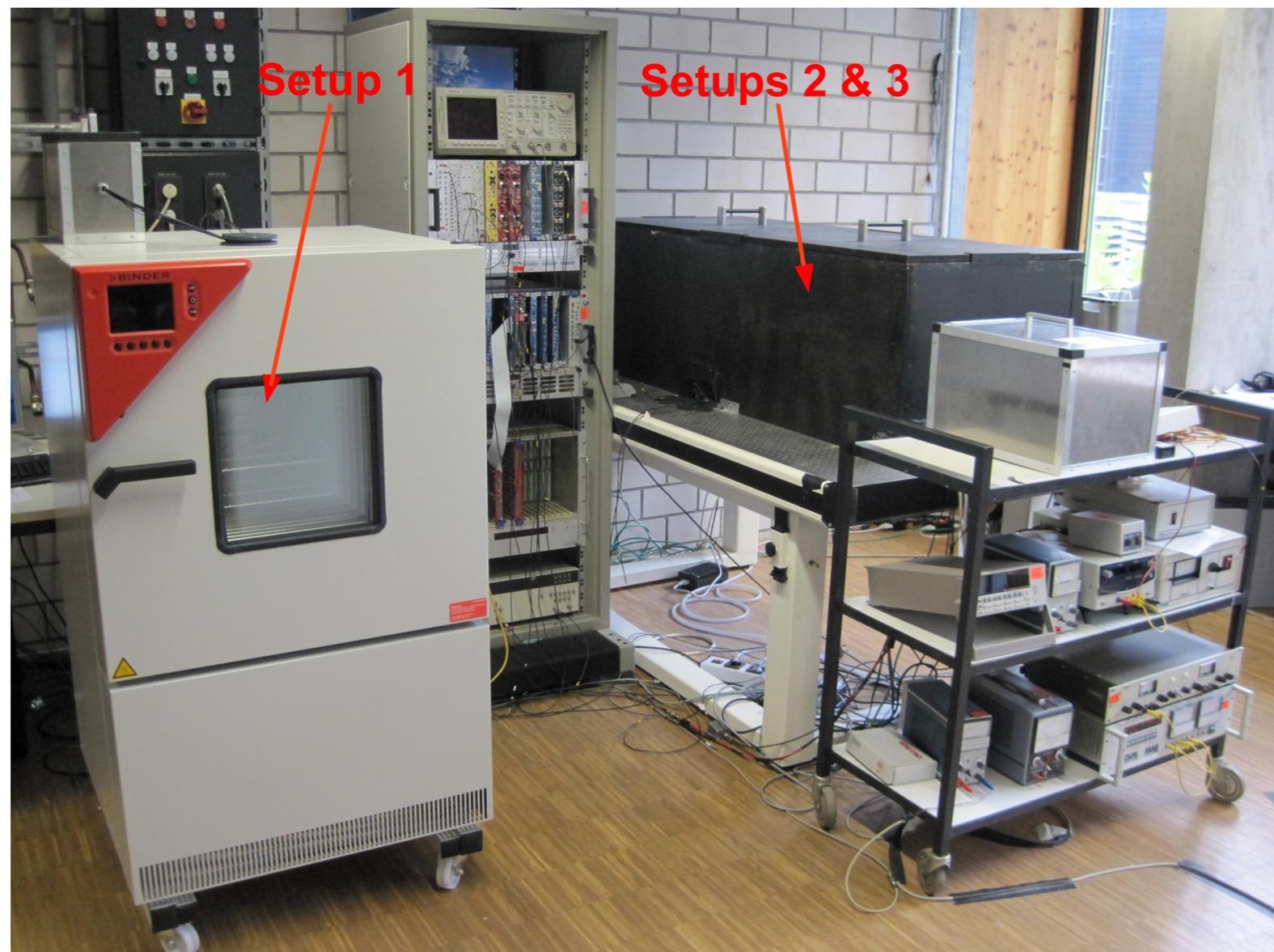
- Basic properties:

- High gain $10^5 - 10^6$
- Low operating voltage ($< 100V$)
- Very compact
- Insensitive to magnetic fields
- Very small sensitivity to charged particles
- Excellent single photon resolution
- Limited dynamic range
- Noise:
 - Dark-rate $\sim 1\text{MHz}$ (thermal excitation)
 - Cross-talk
 - After-pulses (from trapped charge carriers)



SiPM Characterization

- Compare different sensors
- Find the best operating conditions



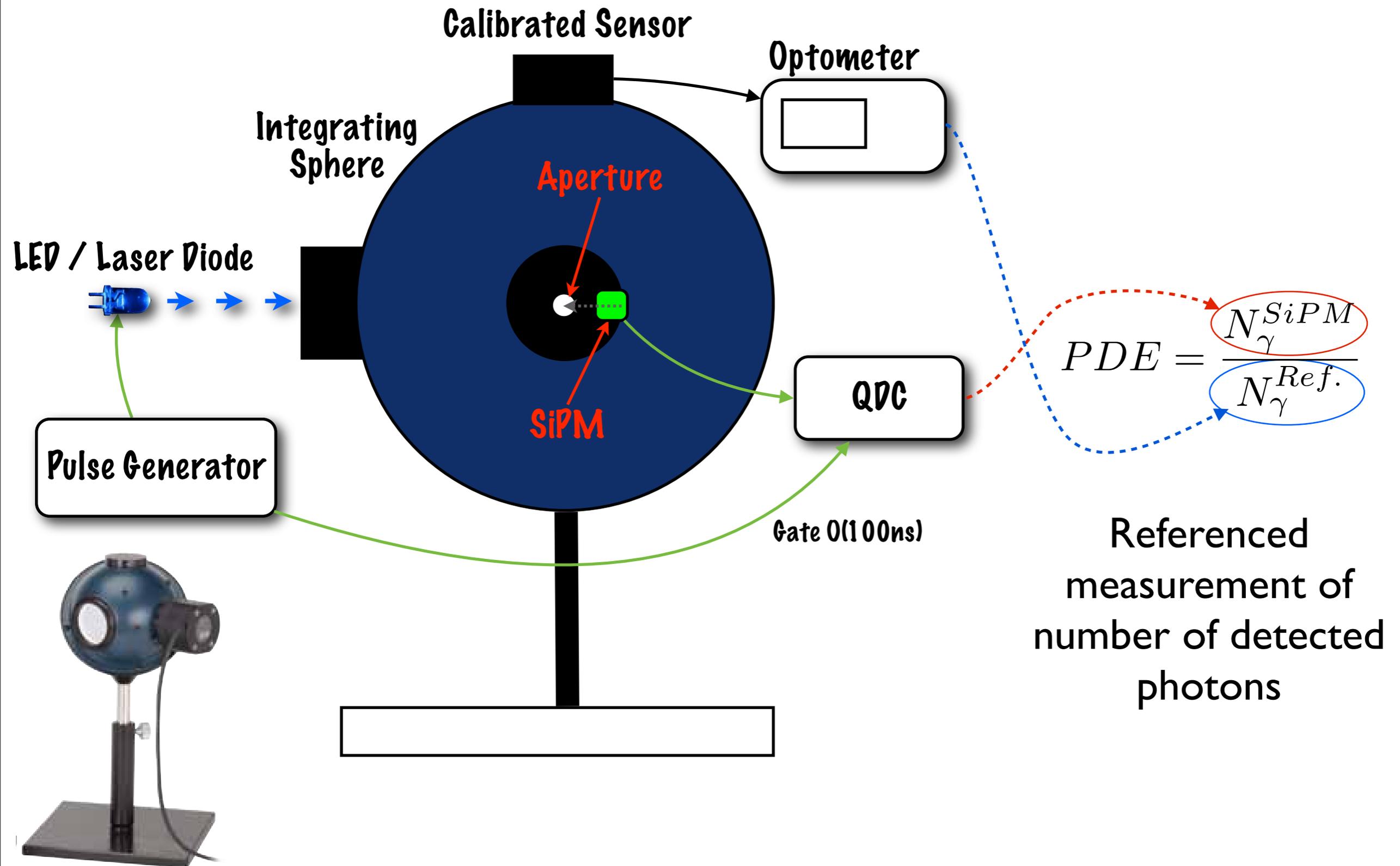
Old setup:

- Gain
- Dark-rate
- Photon Detection Efficiency (PDE)

New setup:

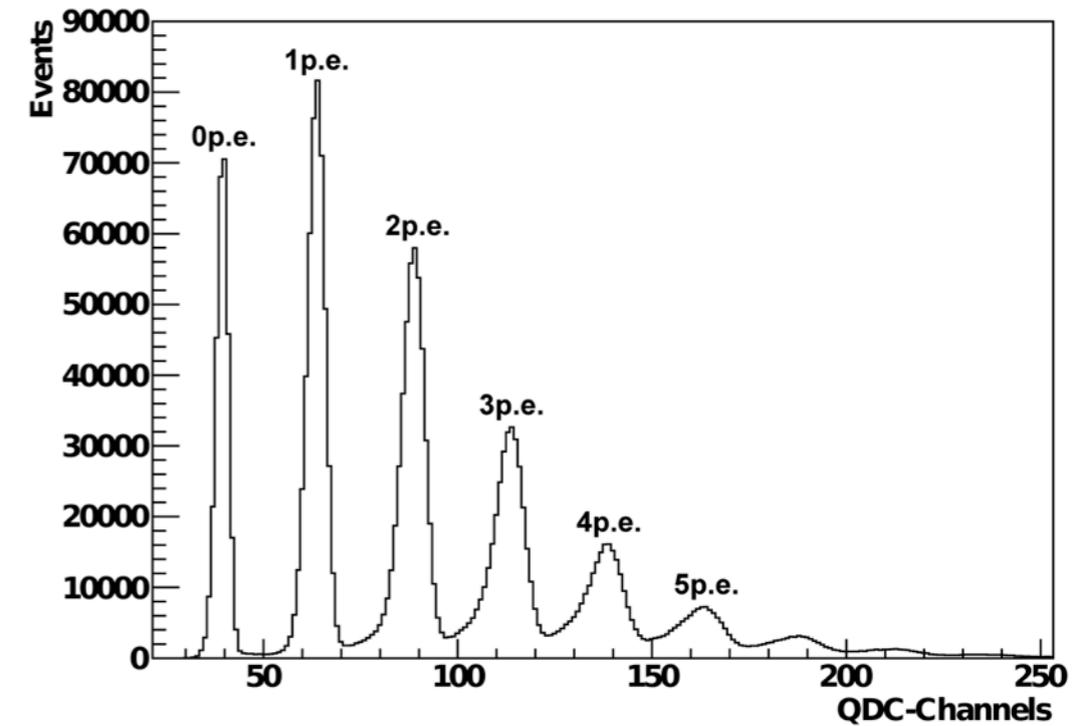
- Cross-talk
- After-pulses
- PDE without cross-talk & after-pulses
- Sensor Scans
- Temperature measurements

Photon Detection Efficiency

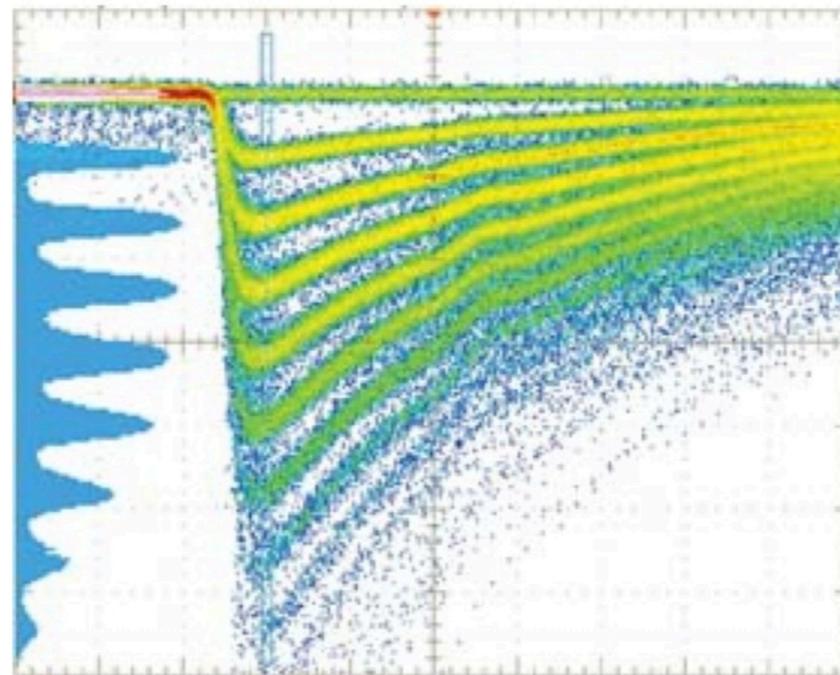


Charge Spectrum

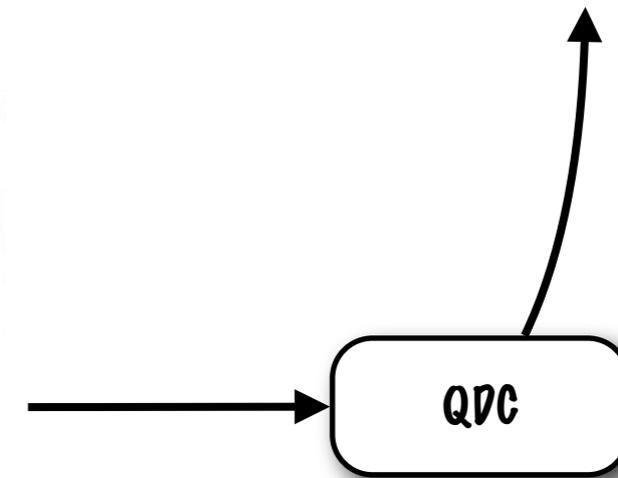
- Signal charge is integrated (integration gate $O(100\text{ns})$)
- Histogram with 10^5 entries is acquired automatically
- Charge spectrum:
 - Clear single photon separation
 - Information about gain & number of detected photons



Number of photons



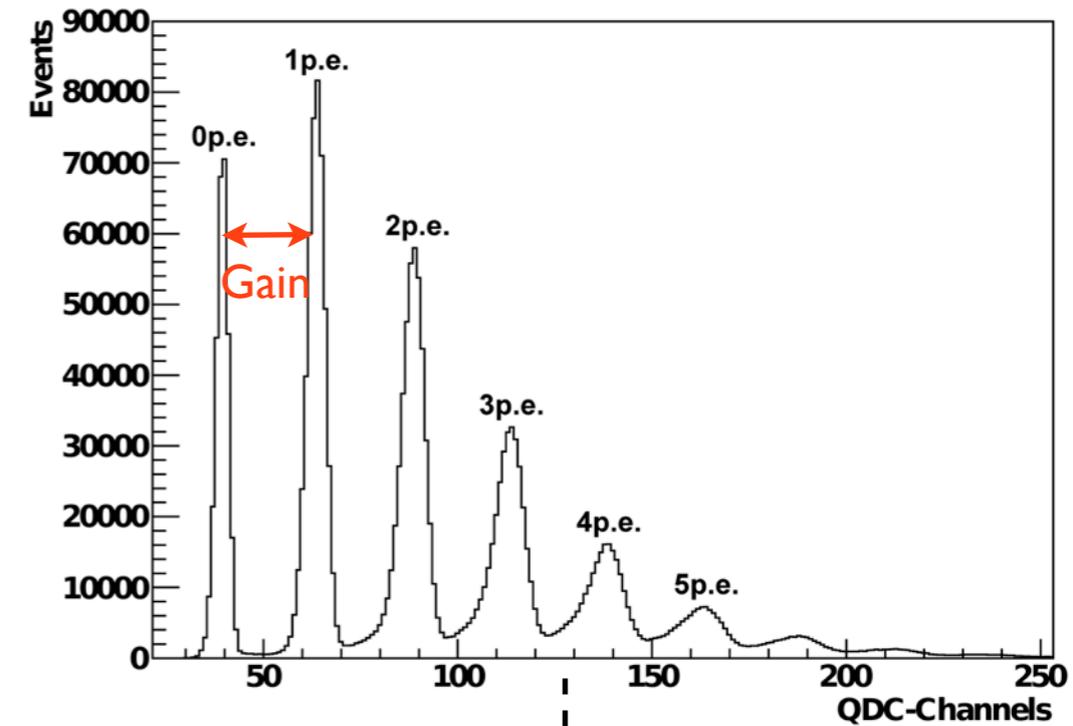
Time



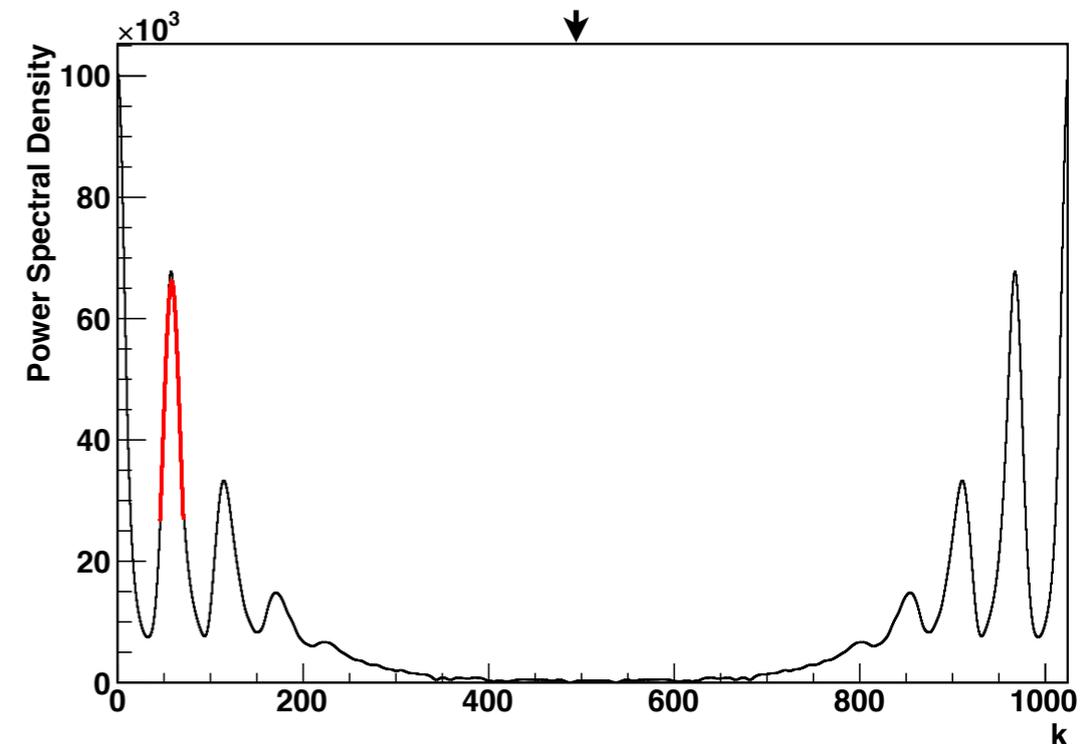
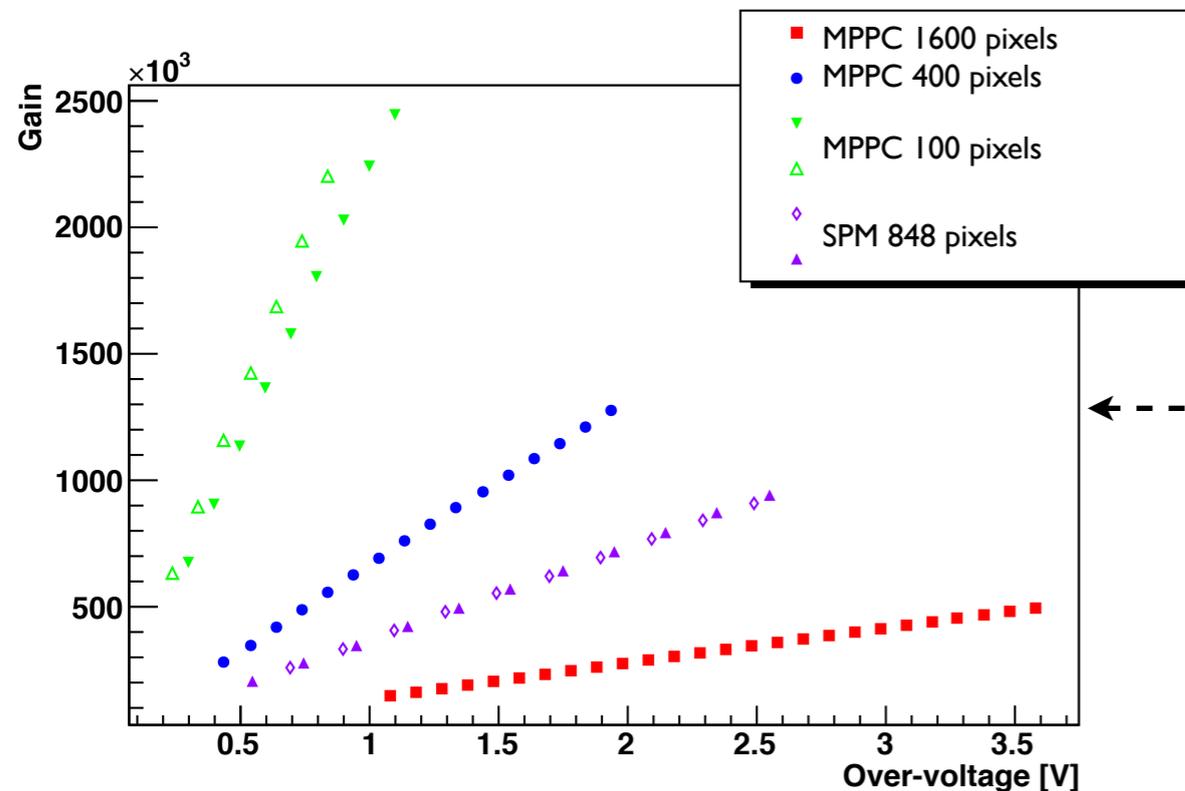
Gain

- Gain = charge difference between peaks
- Gain is automatically determined from frequency spectrum
- Breakdown voltage is automatically determined from a linear fit:

$$G = \frac{C_{pixel}}{q_e} \cdot \underbrace{(V_{bias} - V_{breakdown})}_{\text{Over-voltage}}$$



FFT



Statistical Analysis

- Mean of histogram = mean number of fired pixels (problem: contains cross-talk & after-pulses!)

- Number of incident & detected photons is Poisson distributed:

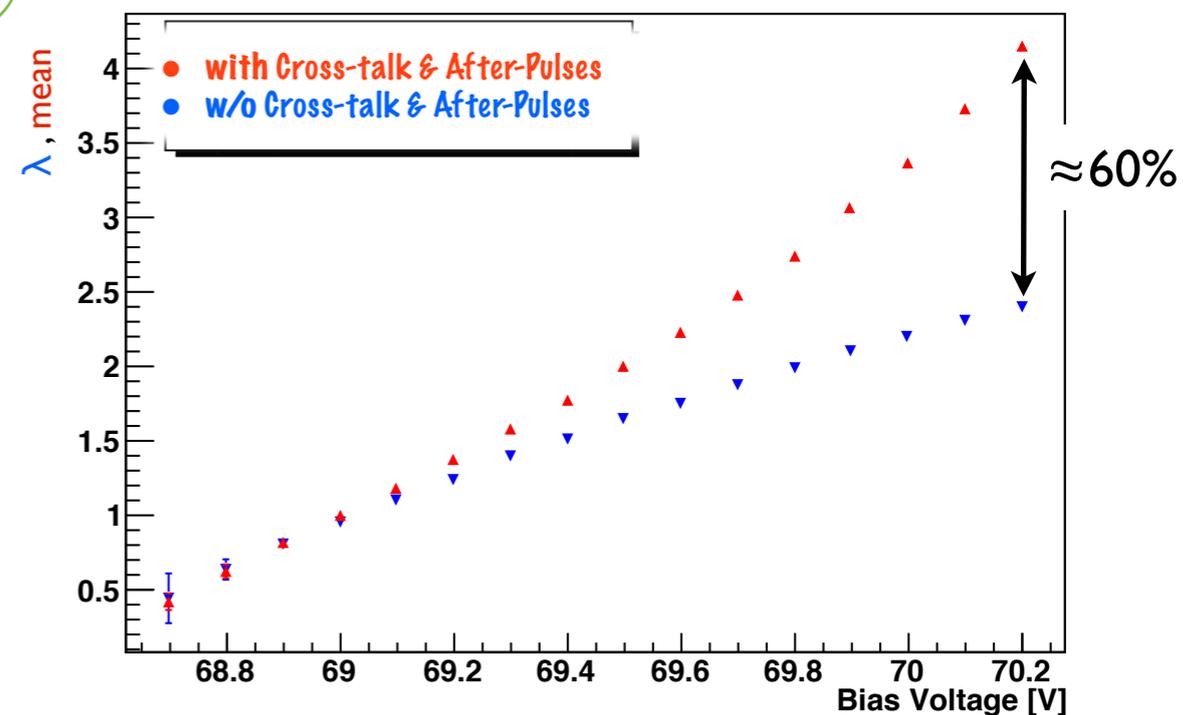
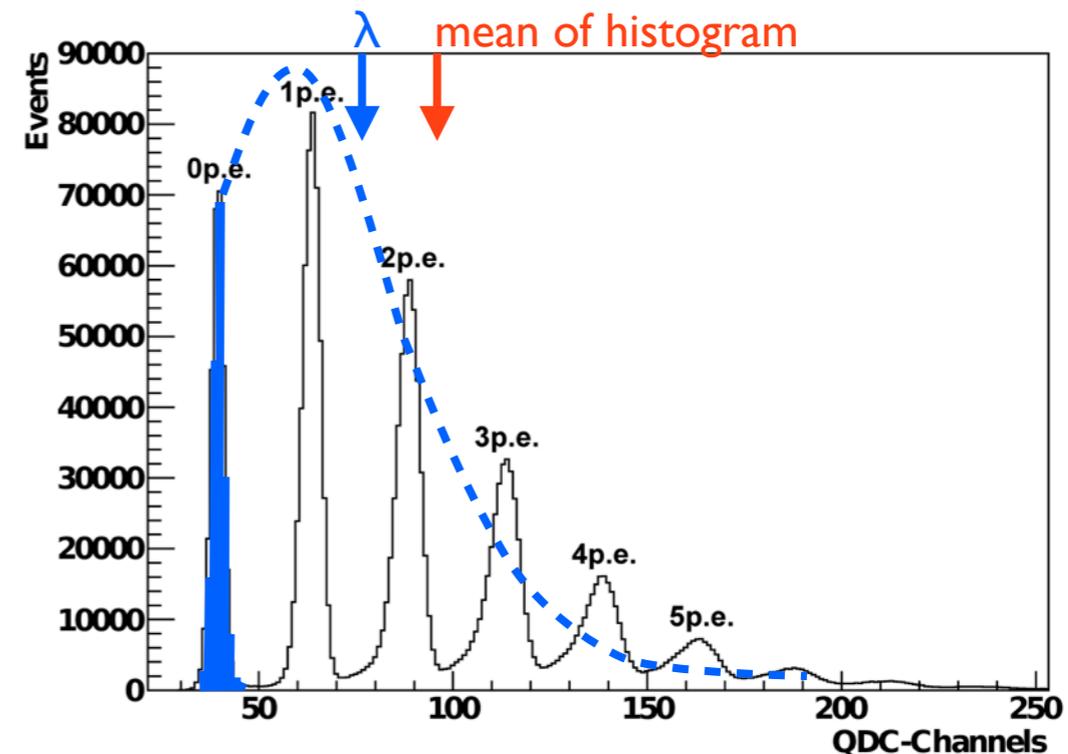
$$P(N, \lambda) = \frac{\lambda^N \cdot e^{-\lambda}}{N!}$$

$$P(0, \lambda) = \frac{N_{Ped.}}{N_{Tot.}} = e^{-\lambda} \Rightarrow \lambda = -\ln \frac{N_{Ped.}}{N_{Tot.}} \quad (-\ln(\alpha))$$

- Pedestal is not influenced by cross-talk and after-pulse!

➔ λ = mean number of detected photons without cross-talk & after-pulses

- Dark-rate can be measured and subtracted



PDE - Intensity Calibration

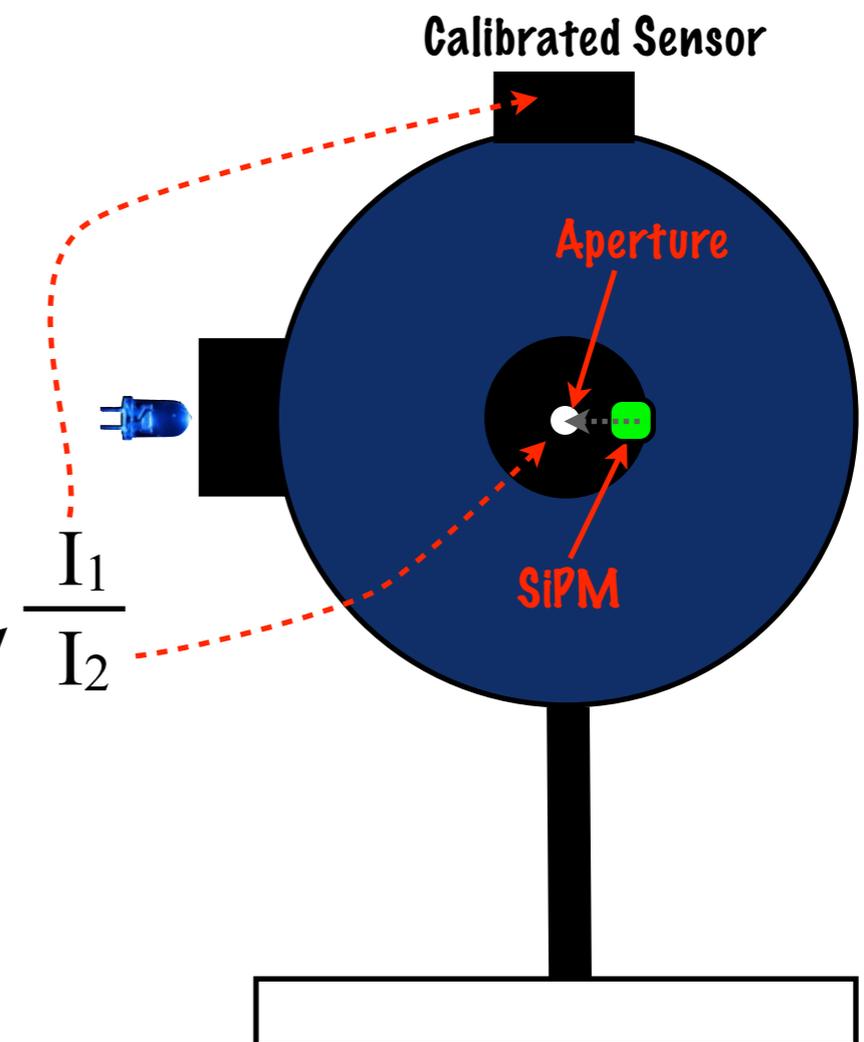
- PDE without cross-talk & after-pulses:

$$PDE = \frac{N_{\gamma}^{SiPM}}{N_{\gamma}} = \frac{N_{\gamma}^{SiPM} / T}{P_{opt} / (h \cdot \frac{c}{\lambda})} \cdot R$$

← LED Pulse Period
← Optical Power at Calibrated Sensor
← Intensity Ratio Between Ports

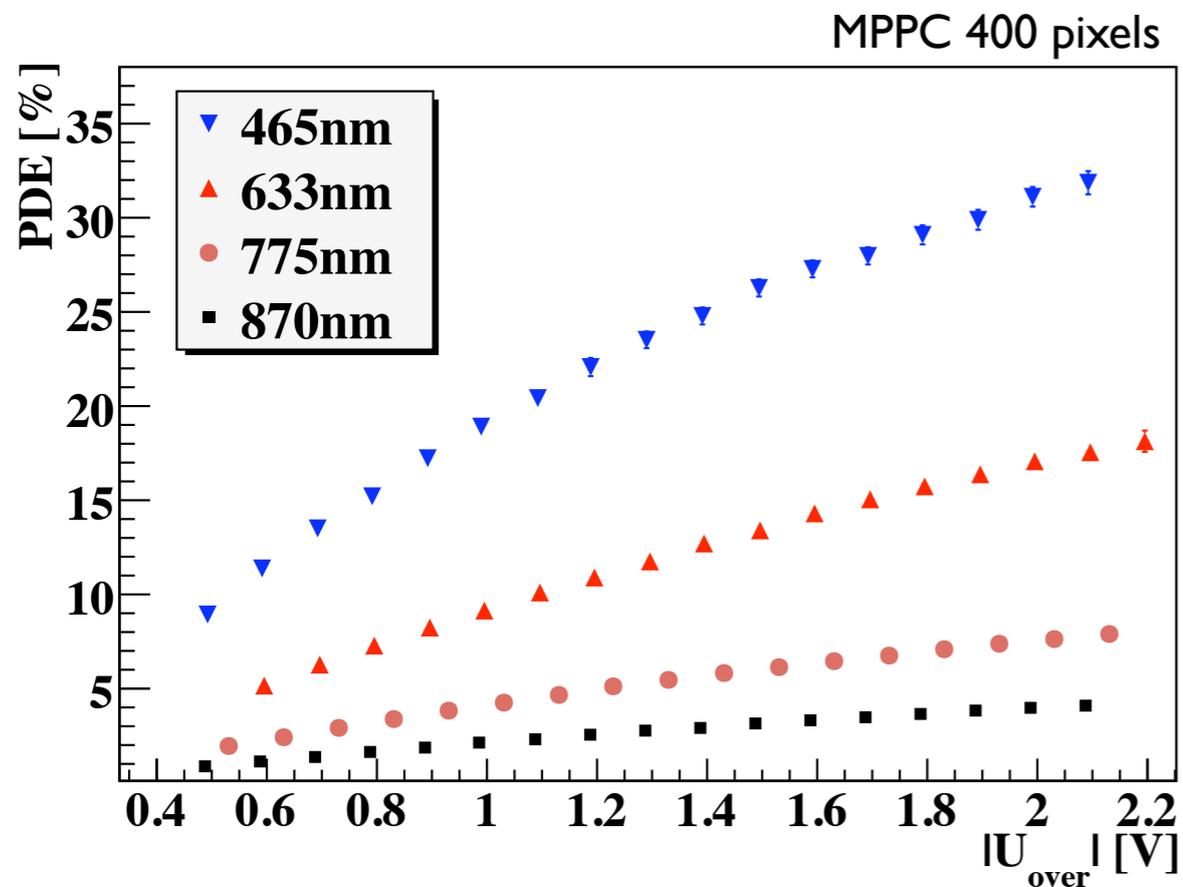
- SiPM is located behind an aperture to only illuminate the active area
- Intensity Ratio R between the two ports has to be calibrated:

Type	λ_{center} [nm]	$R_{0.6}$
LED	465	4200 ± 20
Laser Diode	633	3852 ± 18
Laser Diode	775	4328 ± 7
LED	870	4625 ± 55



PDE

- PDE is automatically measured for a sequence of bias voltages



PDE depends on:

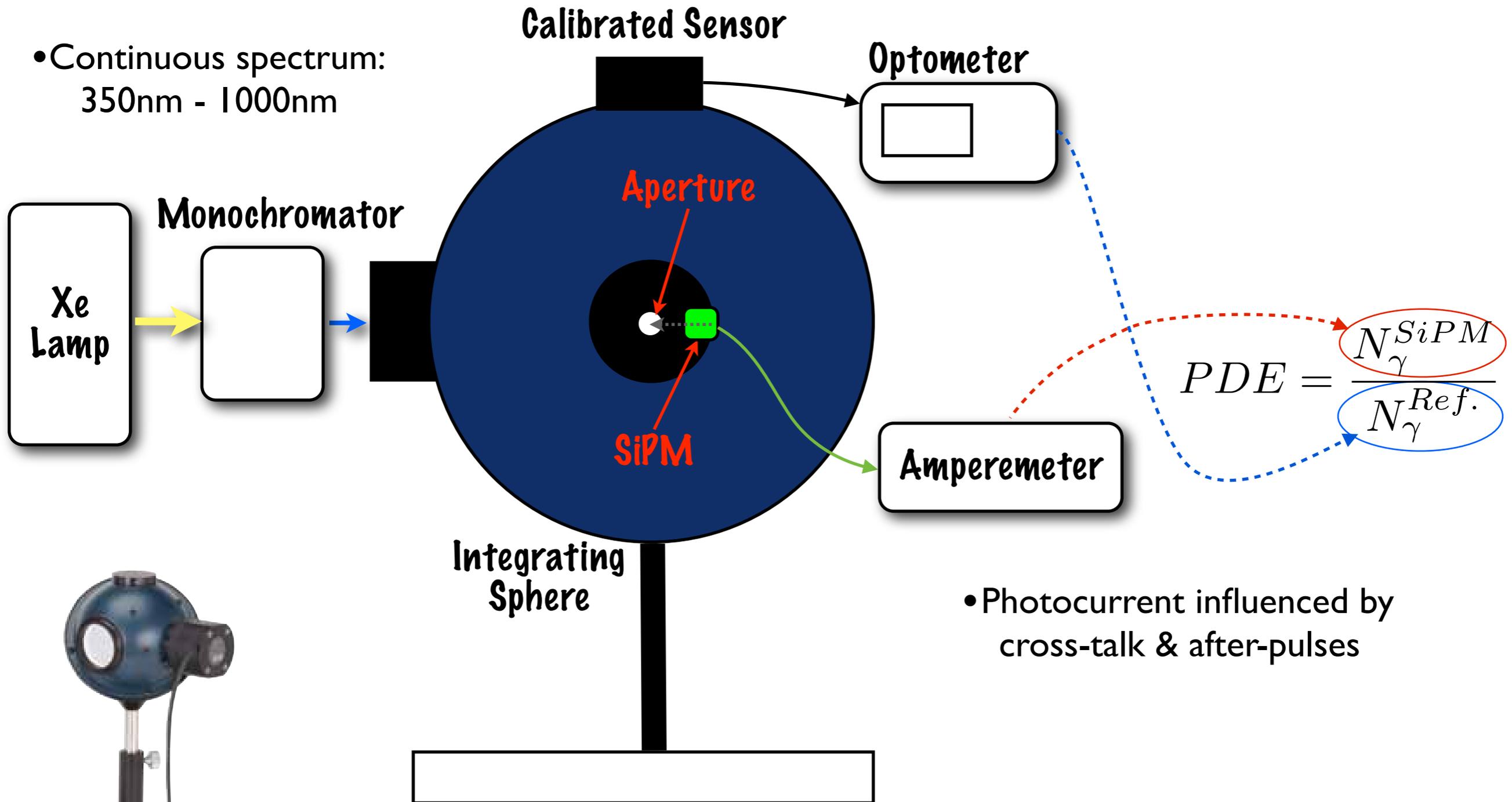
$$PDE = QE \cdot (1 - R) \cdot \epsilon_{geiger} \cdot \epsilon_{geo}$$

- Quantum Efficiency (Wavelength)
- Reflection at surface (Wavelength)
- Geiger probability (Bias voltage)
- Geometrical Fill Factor (Pixel Size)

• Measurement is limited to the wavelength of LEDs / laser diodes

Spectral Sensitivity

- Continuous spectrum:
350nm - 1000nm



- Photocurrent influenced by
cross-talk & after-pulses

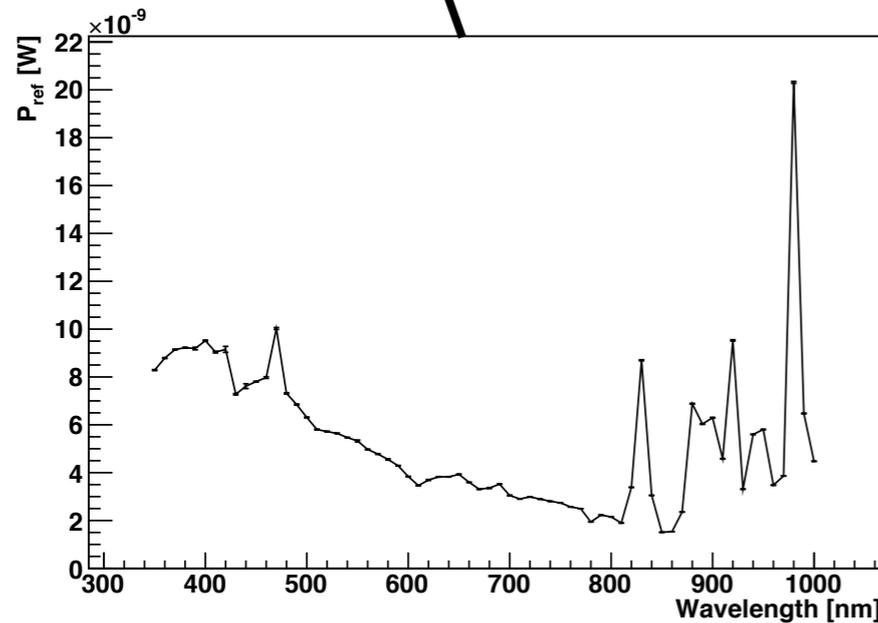
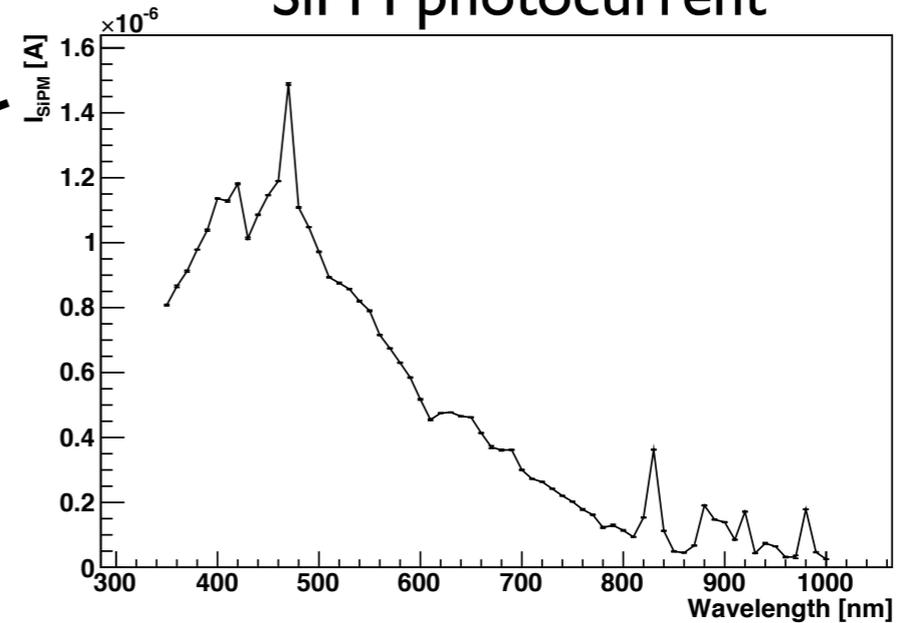
Spectral Sensitivity

Spectral sensitivity:

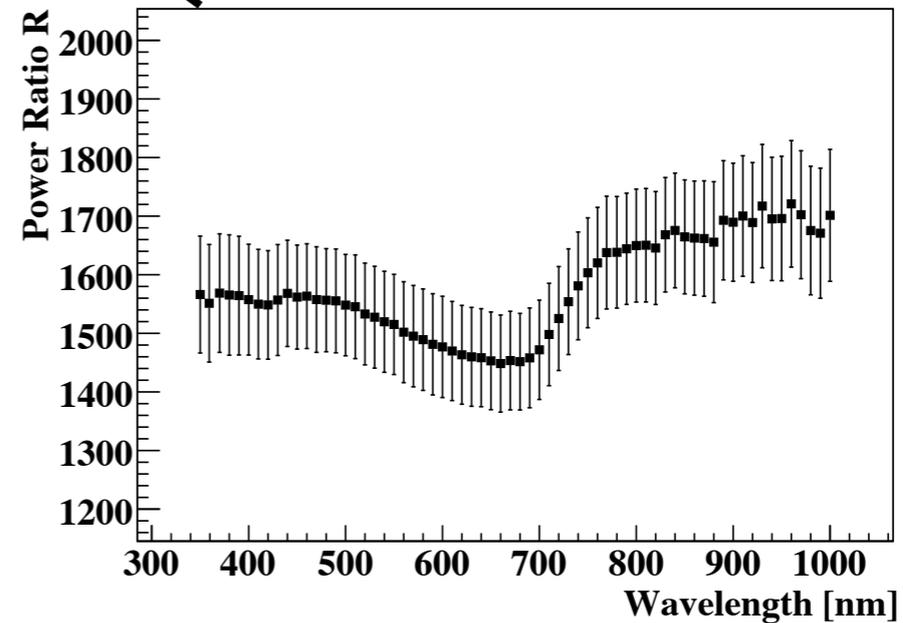
$$S = \frac{I_{SiPM} / (q_e \cdot G)}{P_{opt} / (h \cdot \frac{c}{\lambda})} \cdot R$$

Gain

SiPM photocurrent



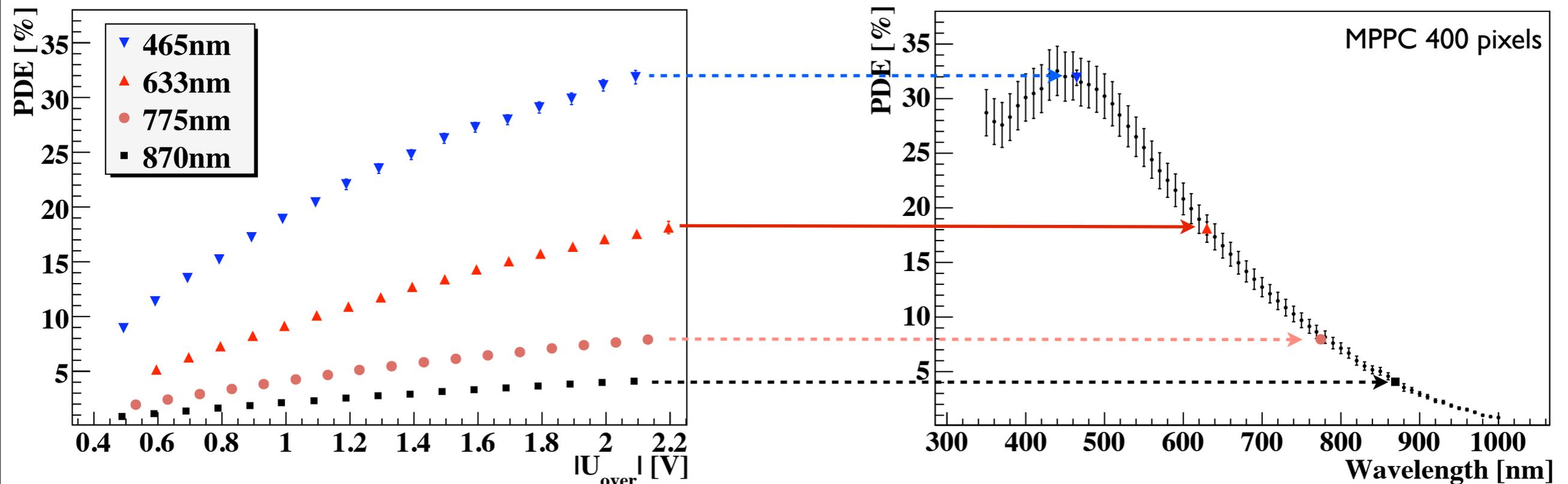
Optical power at calibrated sensor



Intensity ratio between ports

PDE - Spectral Sensitivity

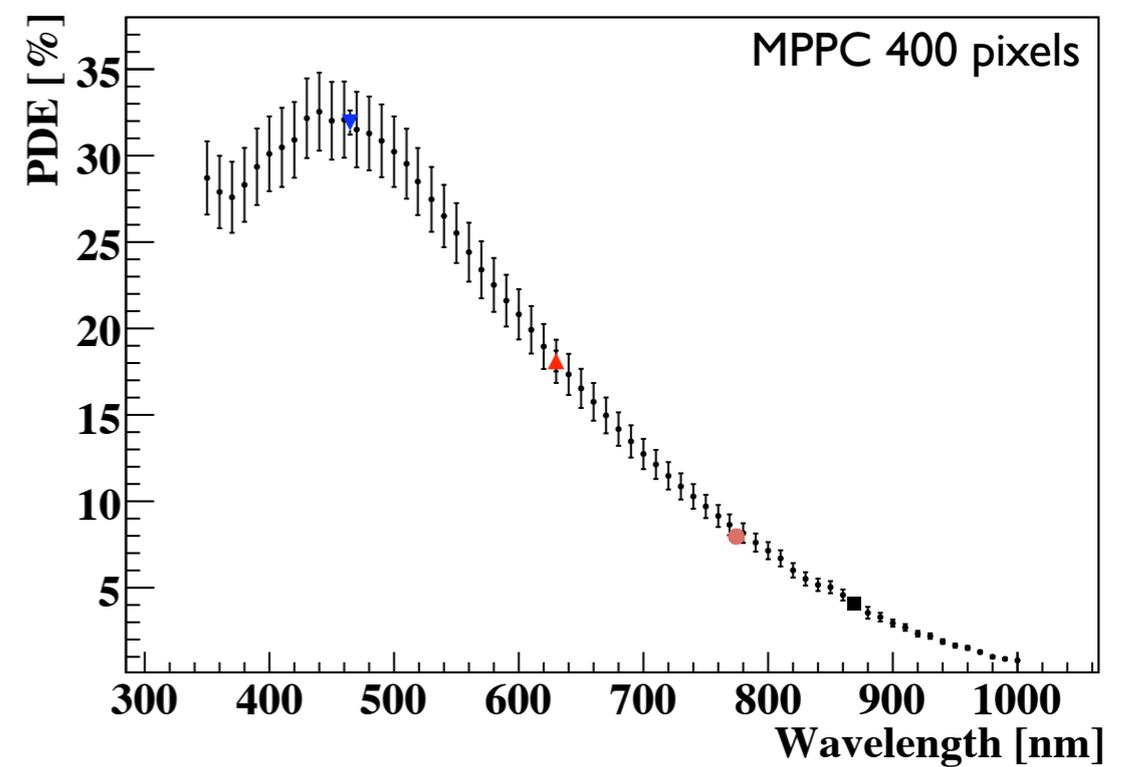
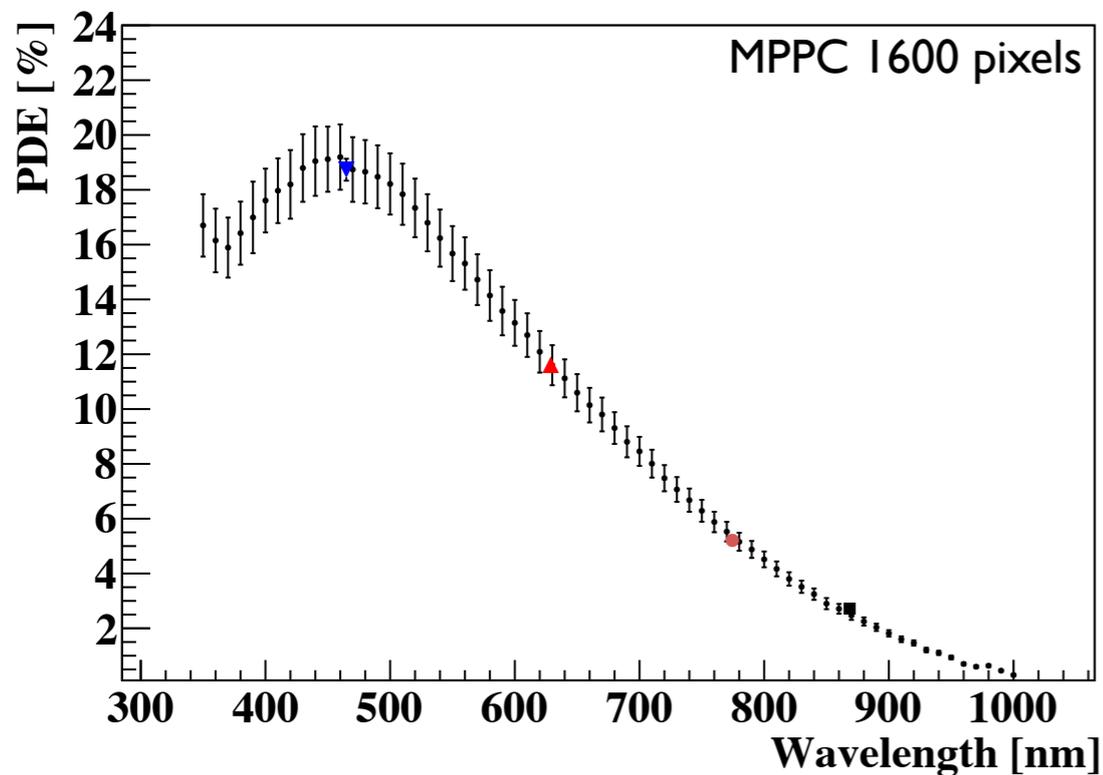
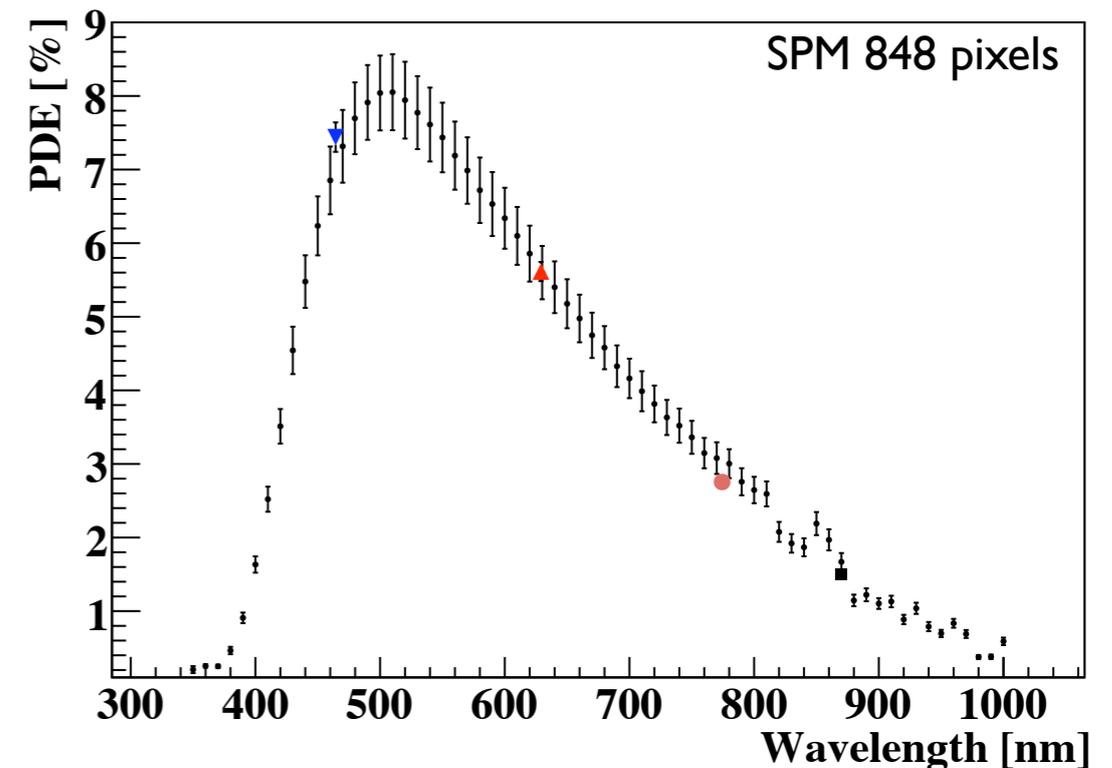
- Automated measurement over wide spectral range
- Measurement contains dark-rate, cross-talk & after-pulses
➔ only relative sensitivity
- Spectral sensitivity can be scaled to measured PDE values



PDE - Spectral Sensitivity

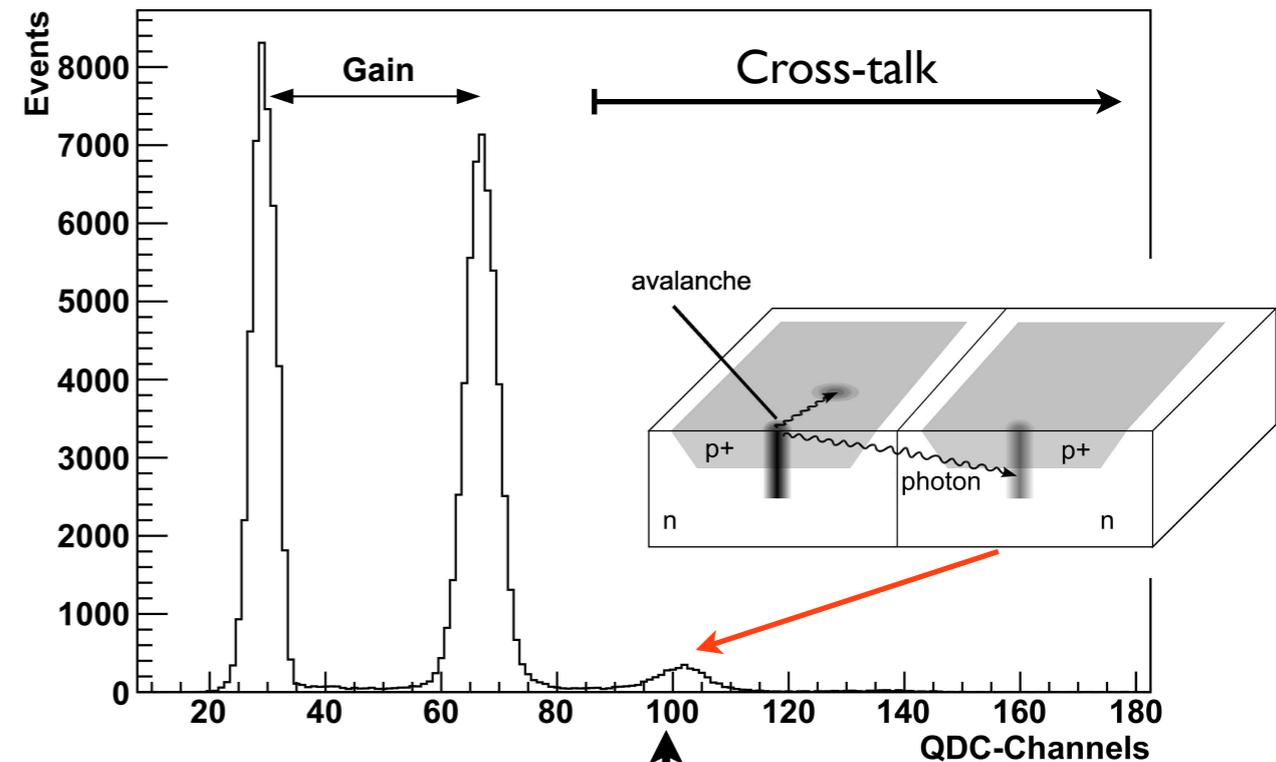
$$PDE = QE \cdot (1 - R) \cdot \epsilon_{geiger} \cdot \epsilon_{geo}$$

- Spectral sensitivity determined by:
 - Quantum efficiency (absorption coefficient)
 - Doping profile
- PDE depends on pixel size (fill factor)

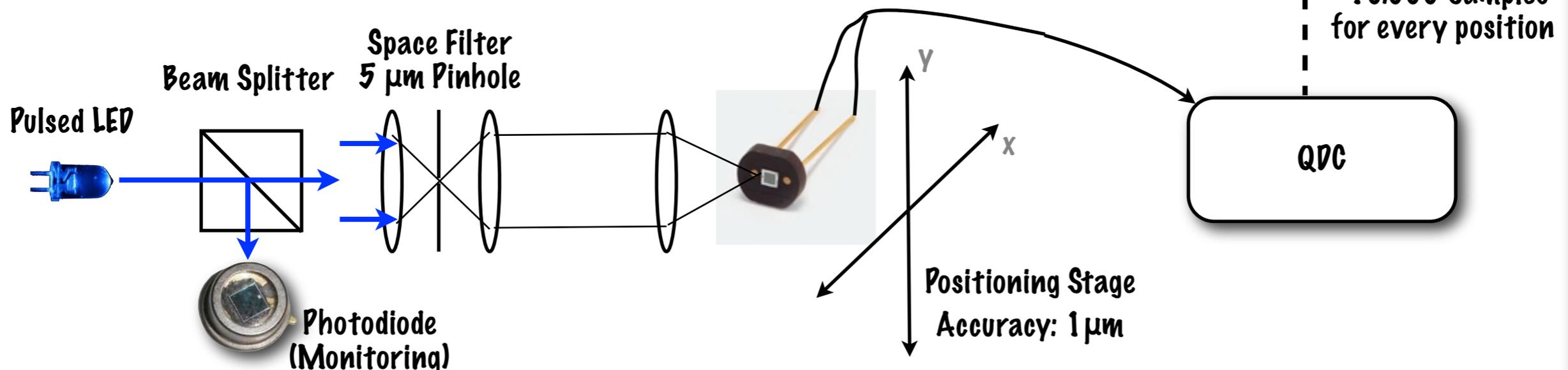


Sensor Scans

- Sensor is scanned with a focused light spot
- Gain & sensitivity can be determined for single pixels
- 2-pixel signals are caused by cross-talk
- Measurement is fully automated

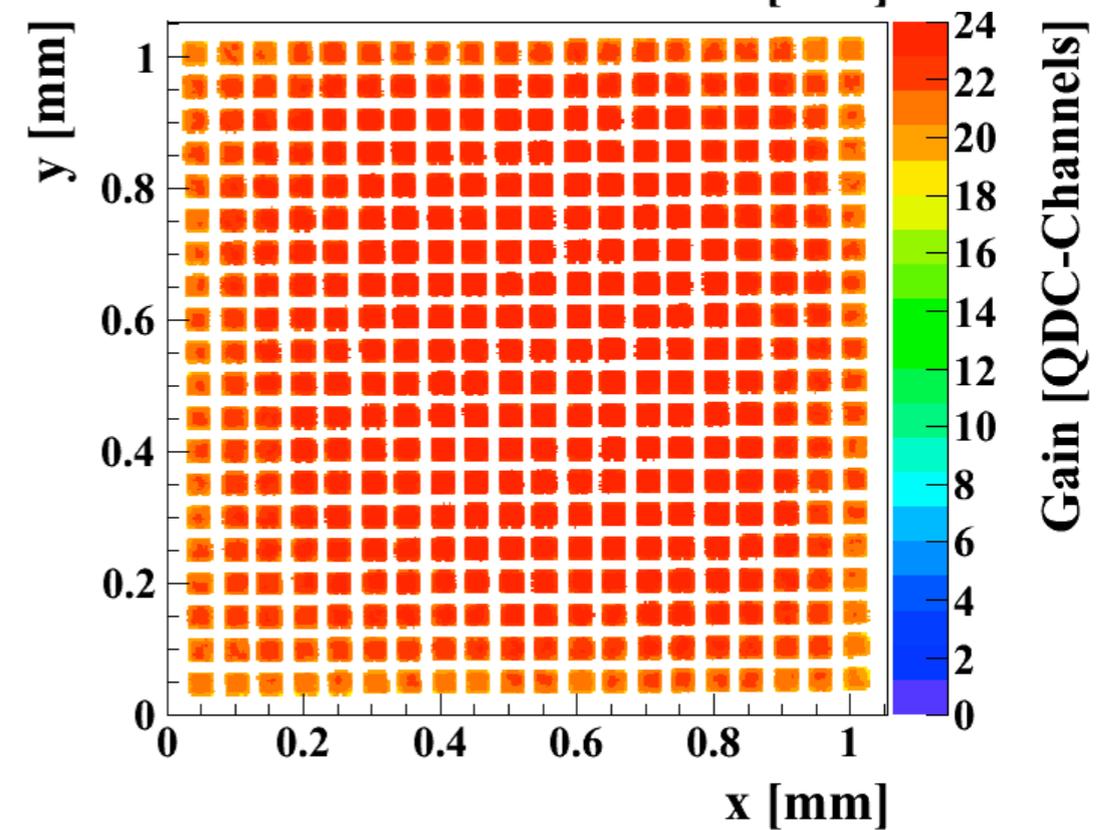
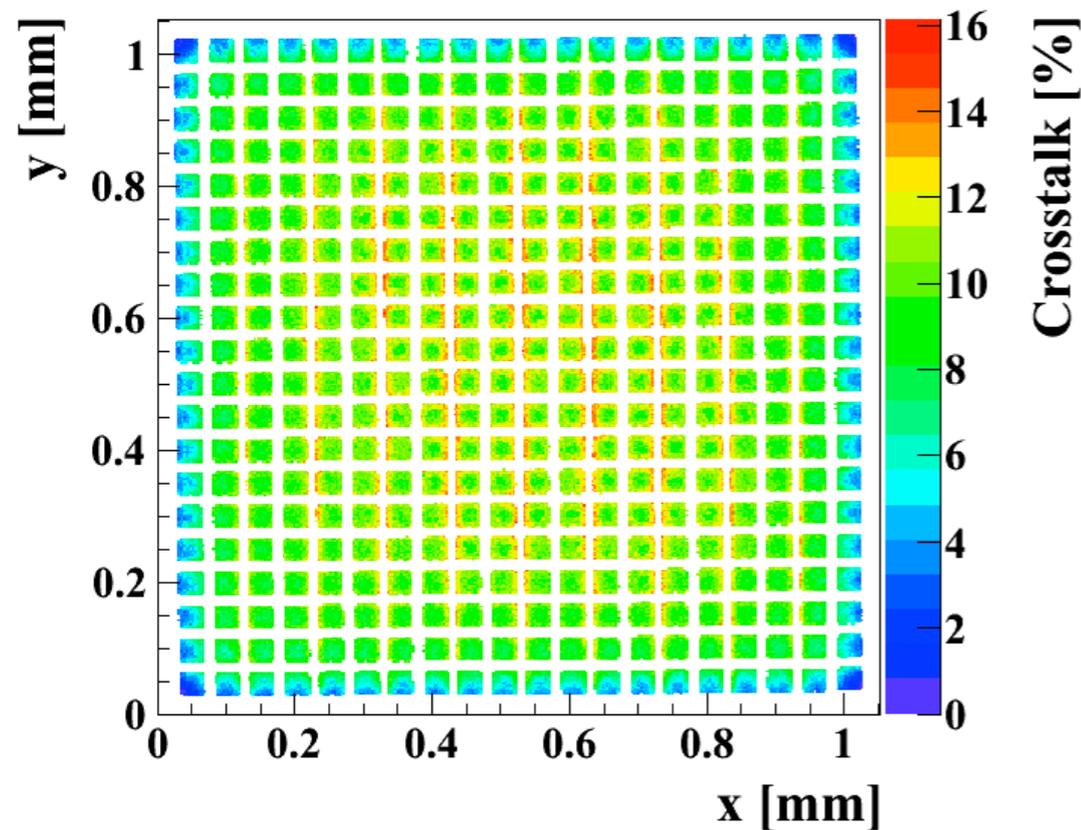
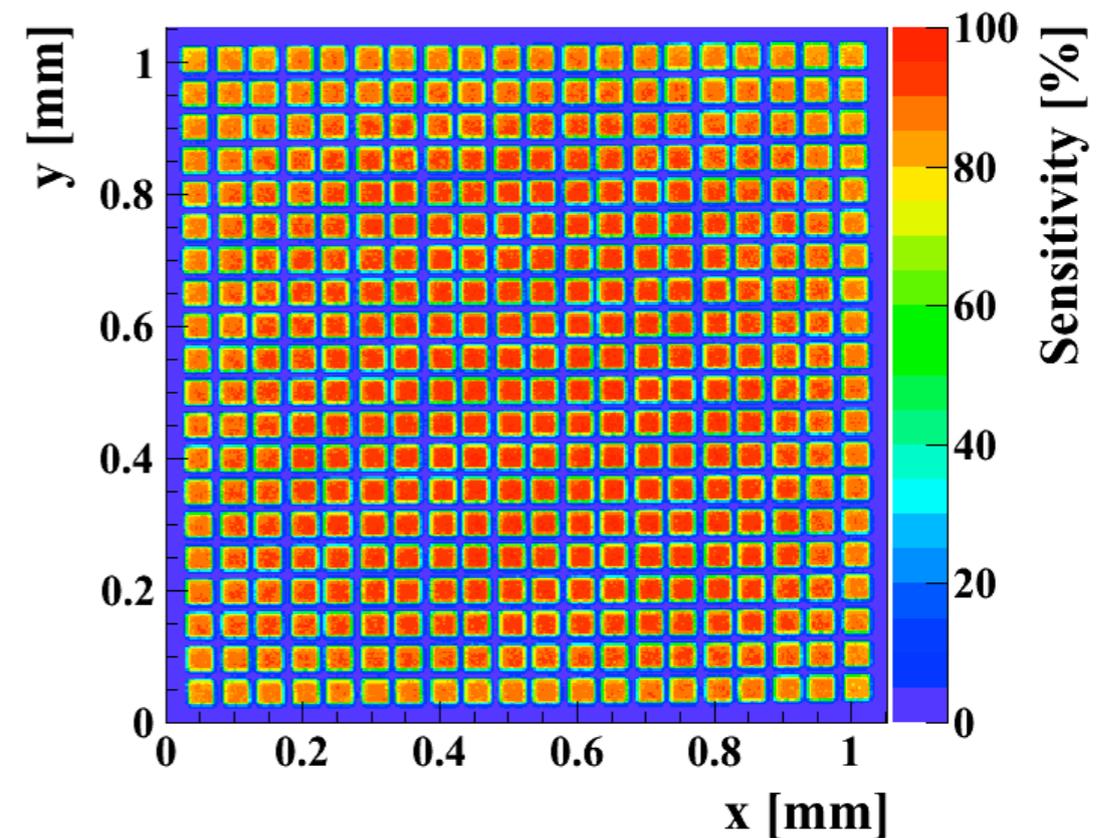


Scan setup:



Sensor Scans

- Uniform sensitivity & gain
- Higher cross-talk in the center due to more neighboring pixels
- Cross-talk varies within pixel
➔ Inhomogeneous avalanche?

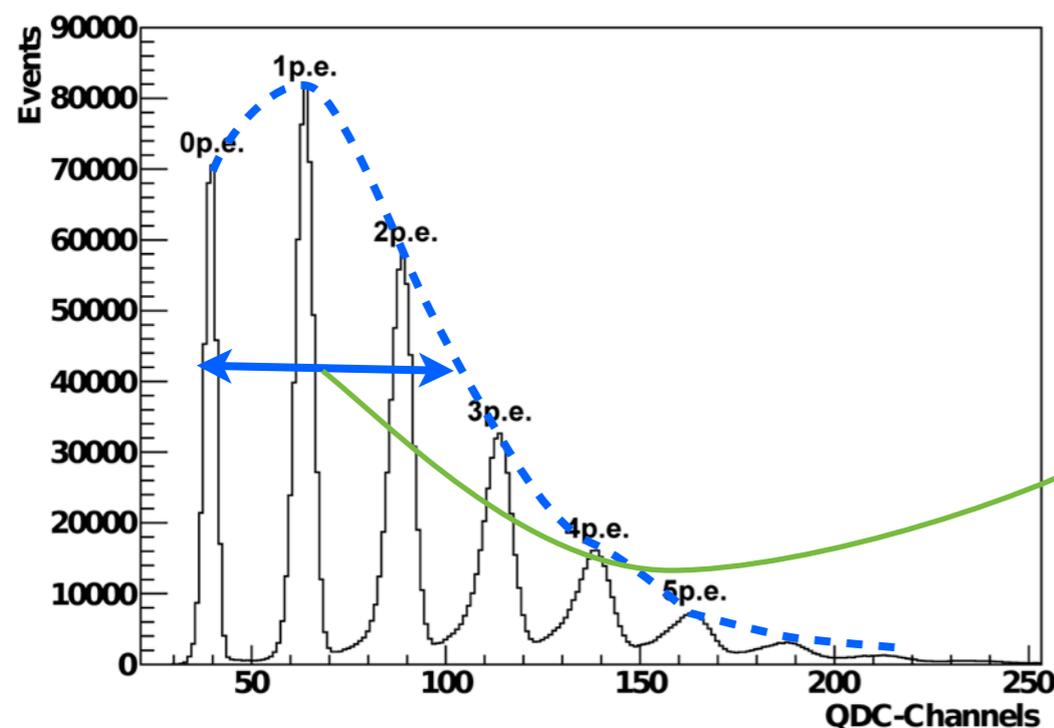


Photon-counting Resolution

- Resolution can be calculated from SiPM properties:

Ideal Sensor (no noise):

- Resolution determined by statistical fluctuation in the number of detected photons:



From PDE measurement:

$$\sigma_{N_{PDE}} = \sqrt{N_{\gamma} \cdot PDE(1 - PDE)}$$

(Only valid for the linear range!)

Real Sensor:

- Also dark-rate, cross-talk & after-pulses generate noise:

From dark-rate, cross-talk & after-pulse measurements

$$\sigma_{Signal} = \sqrt{\sigma_{N_{PDE}}^2 + \sigma_{N_{CT}}^2 + \sigma_{N_{AP}}^2 + \sigma_{N_{DR}}^2}$$

Photon-counting Resolution

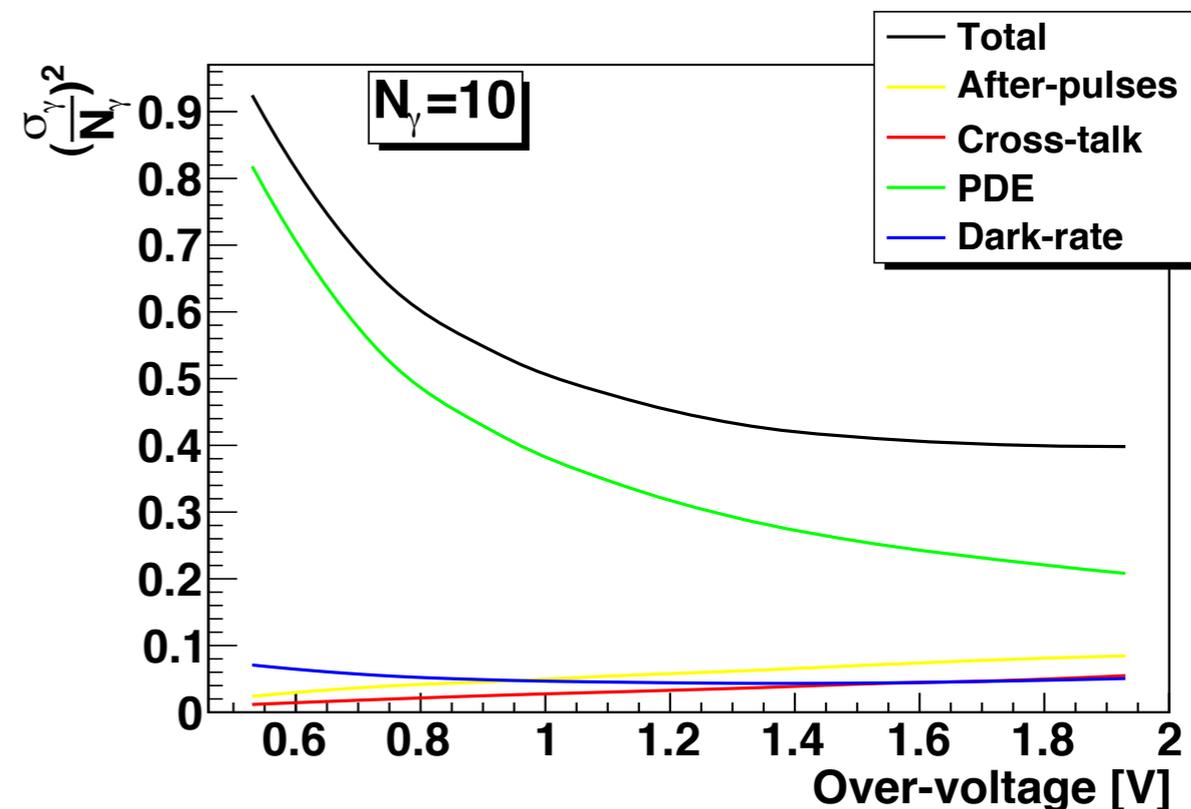
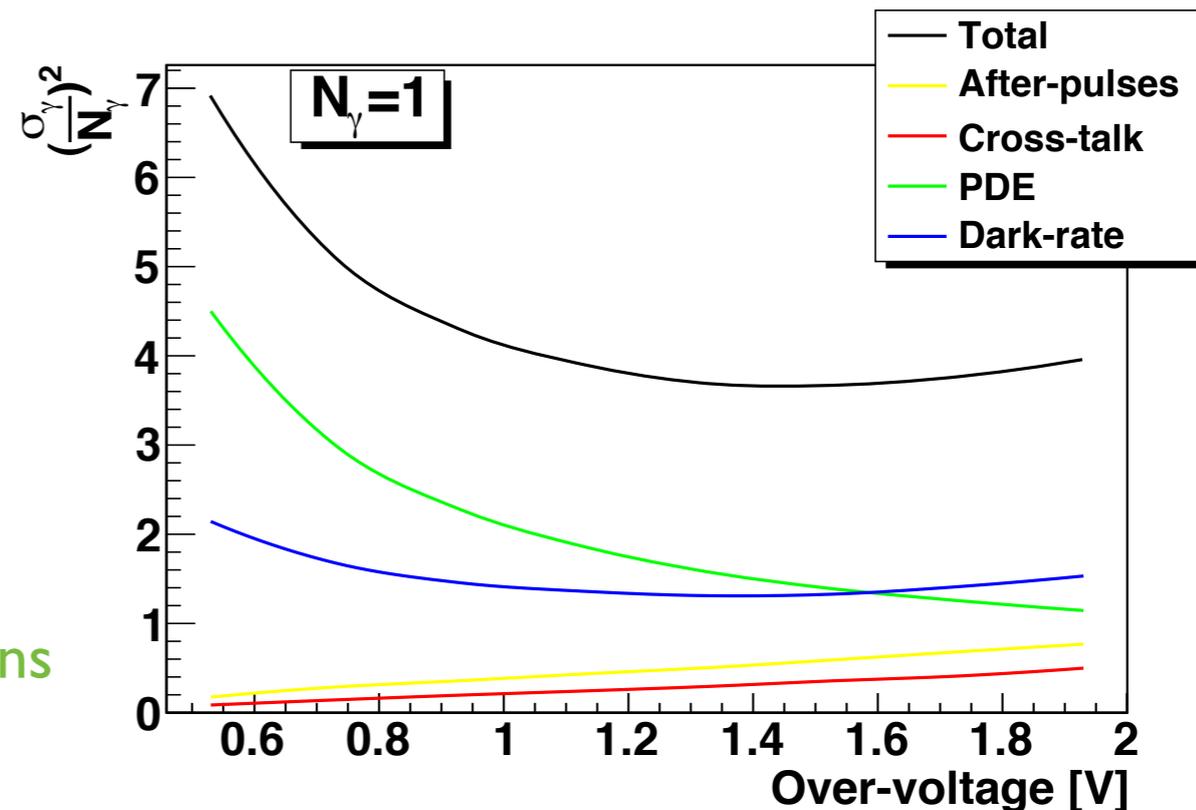
MPPC 400 pixels:

$$\frac{\sigma_{N_\gamma}}{N_\gamma} = \frac{2.93}{N_\gamma} \oplus \frac{1.90}{\sqrt{N_\gamma}}$$

Signals triggered by dark-rate

Signals triggered by photons

- „Optimal“ operation voltage depends on photon flux
- Resolution limited by PDE
- Dark-rate can be neglected for moderate photon fluxes



Summary

- SiPMs are promising devices for many applications
- Our test stand allows a detailed characterization of the sensors
 - Gain
 - Dark-rate
 - Cross-talk & after-pulses
 - PDE w/o cross-talk & after-pulses
 - Sensor Scans
 - Temperature dependence
- Measurements are fully automated
- PDE is the limiting factor for the photon-counting resolution