

Measurement of the polarization amplitudes in $B_d \rightarrow J/\psi K^*$ with LHCb

Christian Linn
Physikalisches Institut, Universität Heidelberg

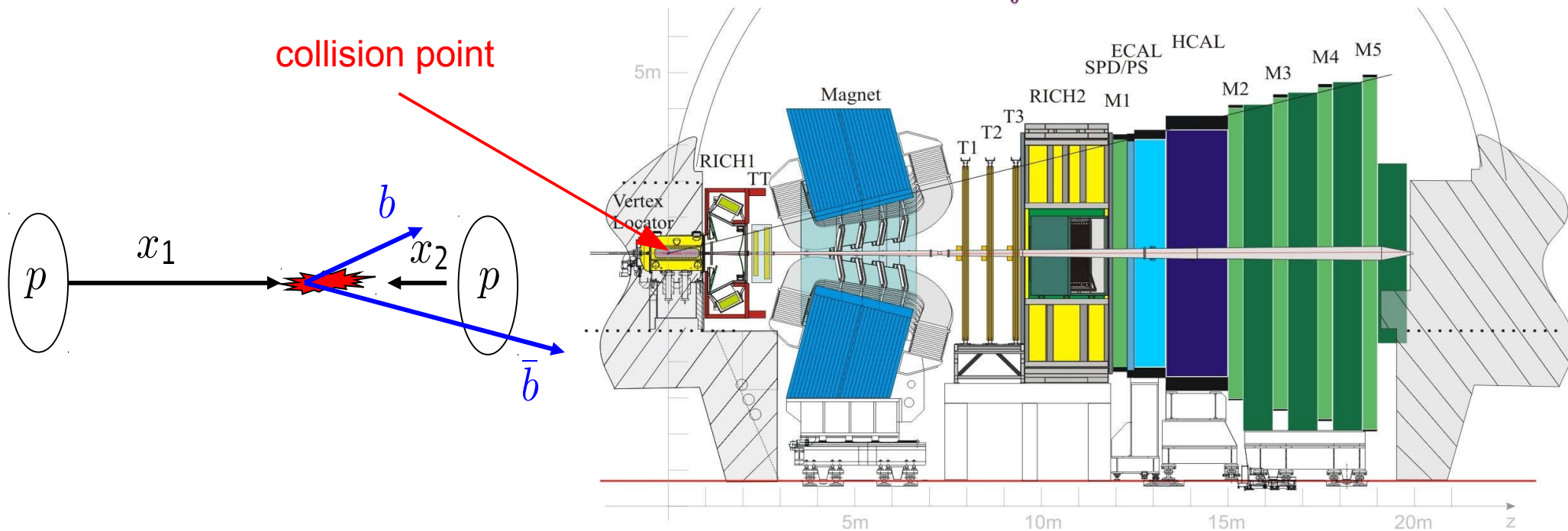
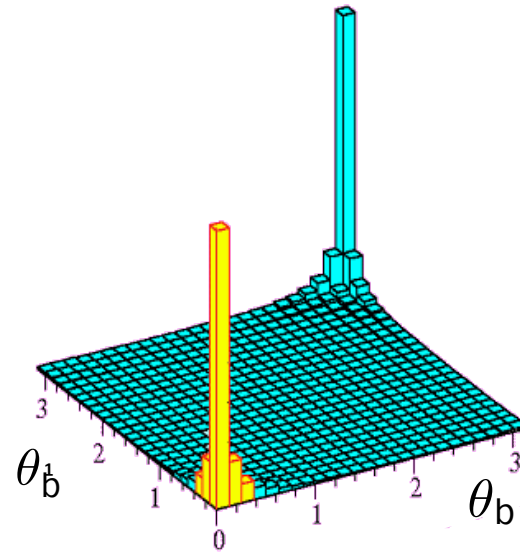


- The LHCb detector
- B – mixing
- Measuring CP violation in $B_s \rightarrow J/\Psi \Phi$
- The reference channel $B_d \rightarrow J/\Psi K^*$
- Systematic studies on detector acceptances
- Sensitivity for polarisation amplitudes
- Outlook

$5 \cdot 10^{11}$ B mesons per nominal year ($= 2 \text{fb}^{-1}$)

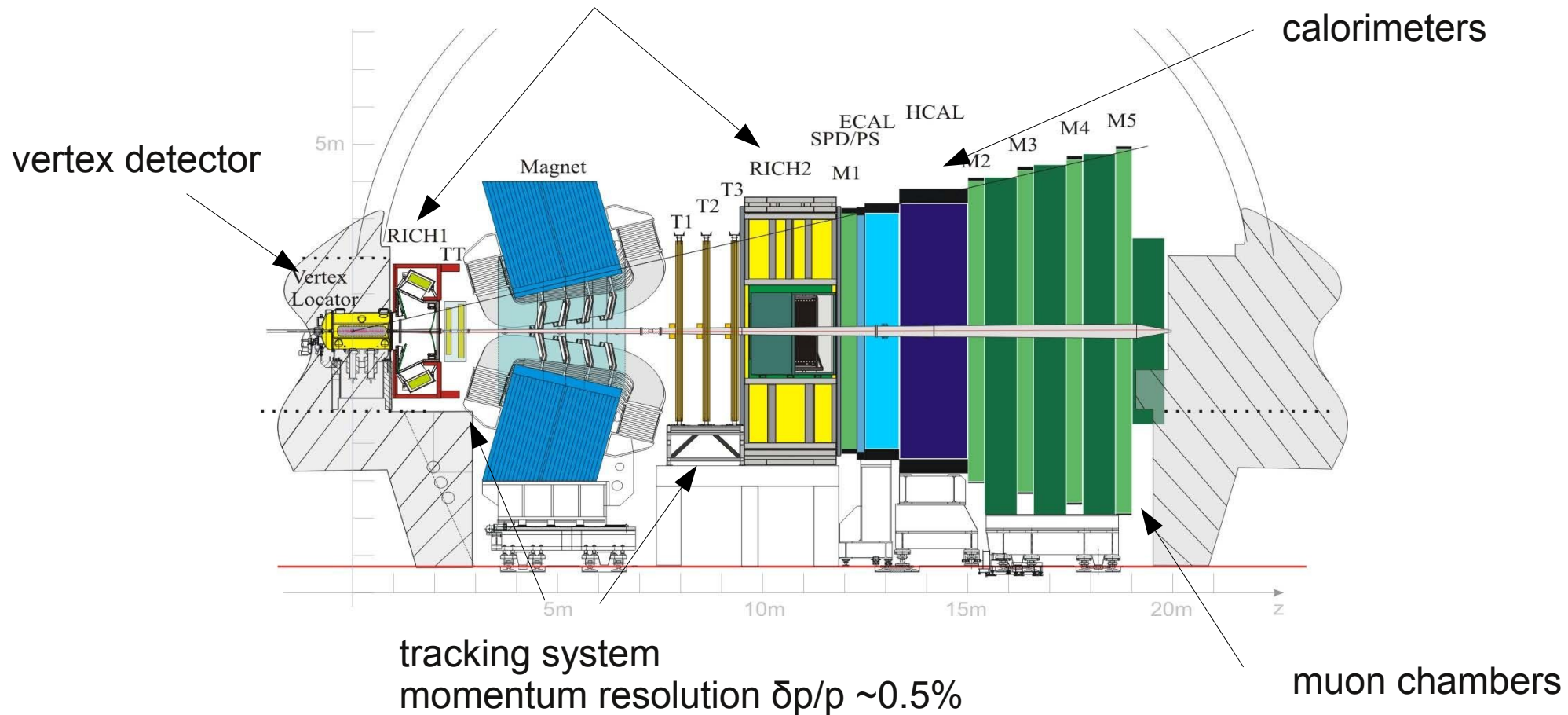
production mainly in forward direction

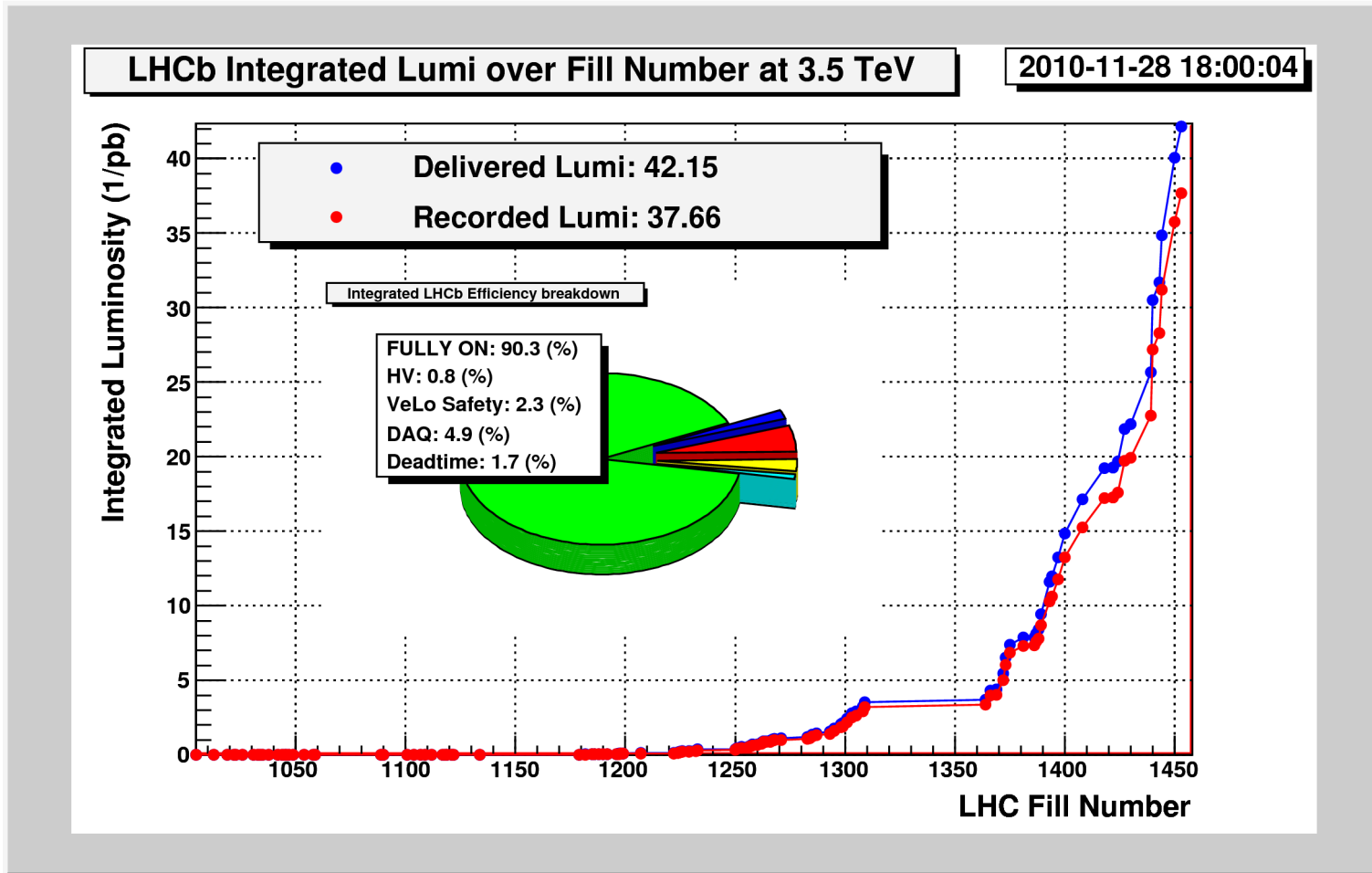
→ LHCb as single arm forward spectrometer



The LHCb detector

RICH detectors
 (2 cherenkov detectors for particle identification)
 momentum range 1 – 100 GeV



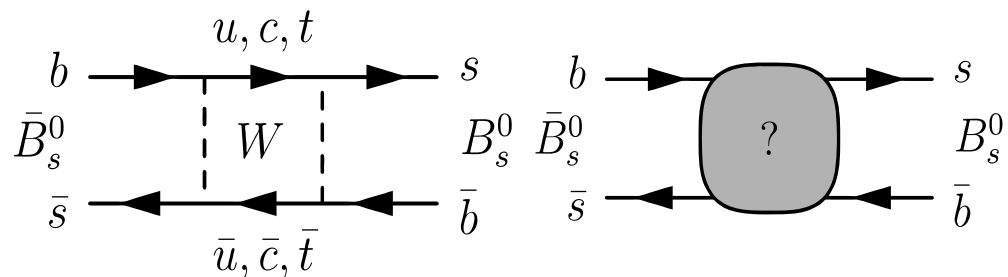


$B_s - \bar{B}_s$ mixing

Time development described by phenomenological Schroedinger eq.

$$i \frac{d}{dt} \begin{pmatrix} B_s \\ \bar{B}_s \end{pmatrix} = \left(M - \frac{i}{2} \Gamma \right) \begin{pmatrix} B_s \\ \bar{B}_s \end{pmatrix}$$

$$\begin{aligned} \Rightarrow \quad & i \frac{d}{dt} B_L = (M_L - \frac{i}{2} \Gamma_L) B_L \\ \text{Diag.} \quad & i \frac{d}{dt} B_H = (M_H - \frac{i}{2} \Gamma_H) B_H \end{aligned}$$



Mixing parameters: $\Delta \Gamma = \Gamma_L - \Gamma_H$

$$\Delta m = m_L - m_H$$

$$\phi_s = 2 \arg V_{ts} V_{tb}^*$$

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

complex

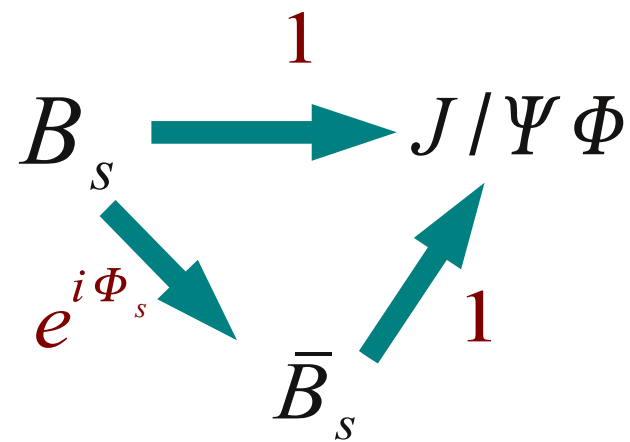
New Physics (e.g SUSY particles in mixing):

→ different mixing amplitude and phase Φ_s

$$\phi_s \rightarrow \phi_{SM} + \phi_{NP}$$

CP violation in $B_s \rightarrow J/\psi \phi$

CP violation only in **interference** of mixing and decay:



for CP eigenstates: $CP(f) = \eta_{CP}(f)$

CP asymmetry:
$$A_{CP}(t) = \frac{\Gamma(\bar{B}_s(t) \rightarrow (J/\psi \phi)_{CP}) - \Gamma(B_s(t) \rightarrow (J/\psi \phi)_{CP})}{\Gamma(\bar{B}_s(t) \rightarrow (J/\psi \phi)_{CP}) + \Gamma(B_s(t) \rightarrow (J/\psi \phi)_{CP})} = -\eta_{CP} \sin \Phi_s \sin(\Delta m \cdot t)$$

But: $J/\psi \phi$ is not a CP eigenstate!!

B_s (spin 0) decays into two vector particles J/Ψ and Φ with spin 1

→ relative angular momentum $L = 0, 1, 2$

$$CP(J/\Psi \Phi) = \eta_{CP}(J/\Psi) \cdot \eta_{CP}(\Phi) \cdot (-1)^L$$

decay described in the basis of three
“transversity angles”

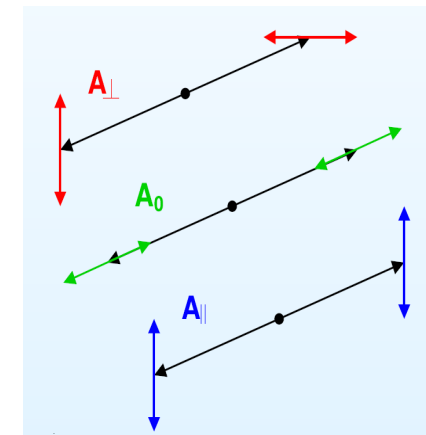
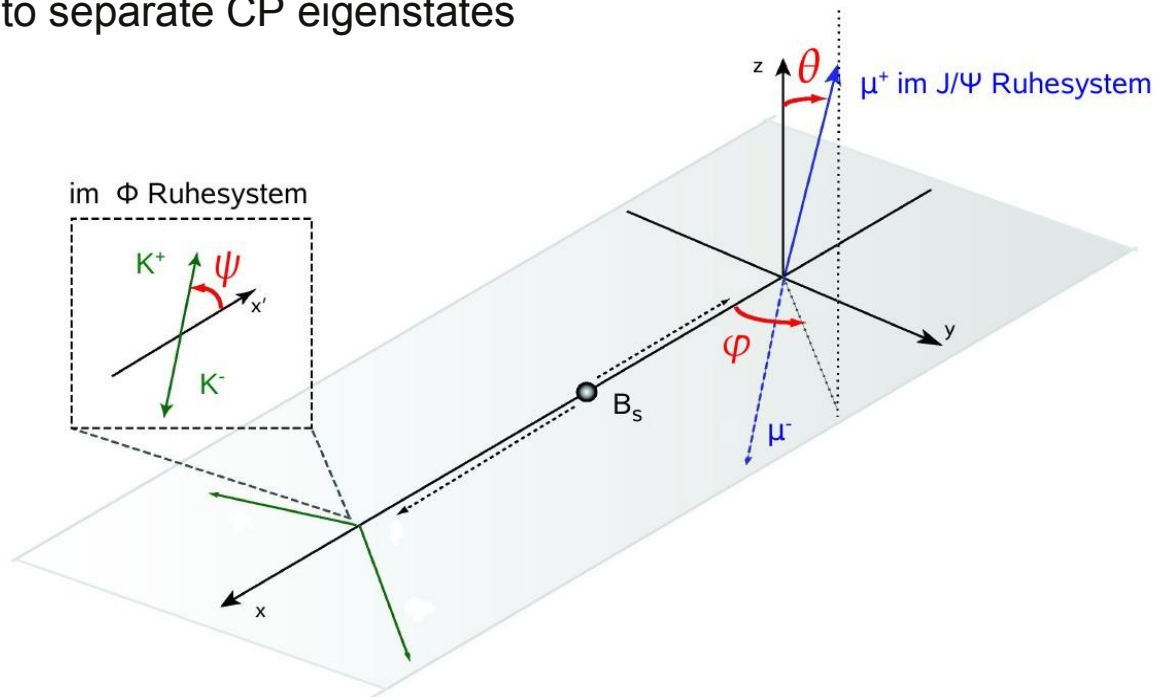
→ combined fit of lifetime and angular distributions
to separate CP eigenstates

$\eta_{CP}(J/\Psi \Phi)$	L	Amplitude
+1	0	$A_0, A_{ }$
-1	1	A_{\perp}
+1	2	$A_0, A_{ }$

A_0 longitudinal polarisation

$A_{||}$ parallel polarisation

A_{\perp} perpendicular polarisation

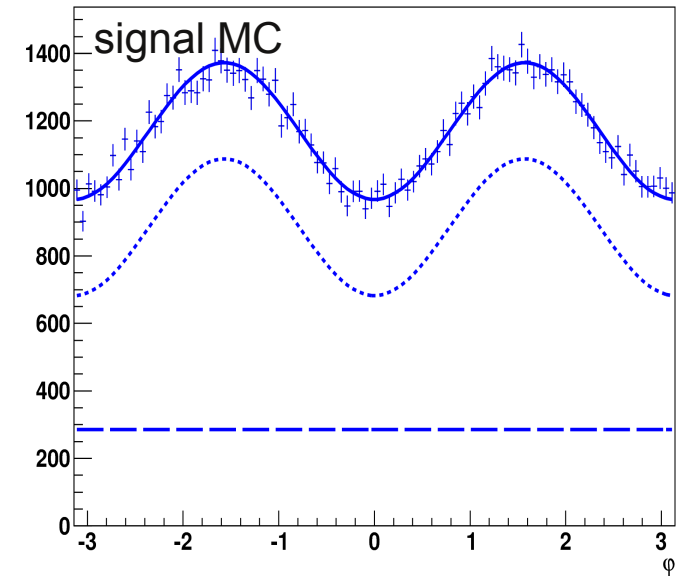




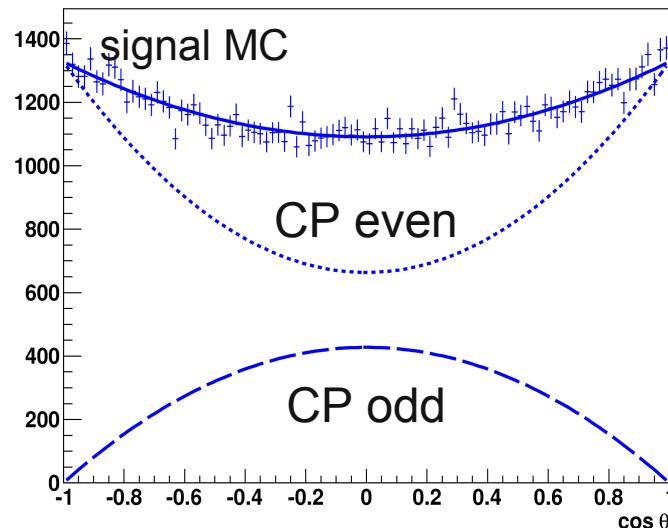
Separation of CP even and CP odd states:

Different shapes in angular distributions
 and proper time

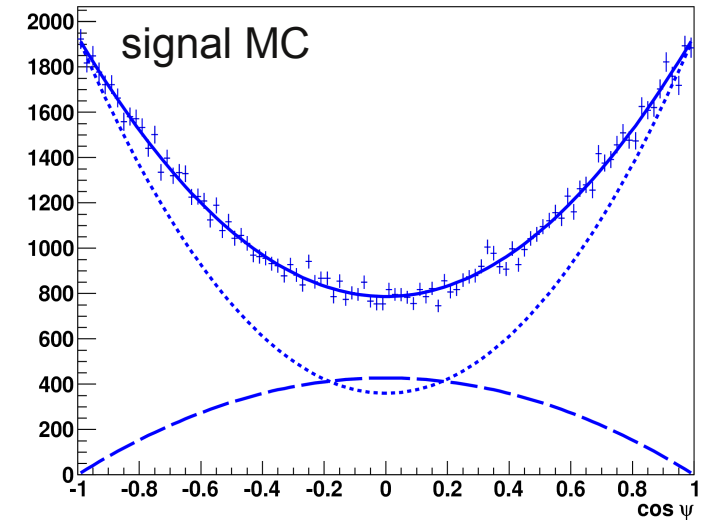
ϕ



$\cos \theta$

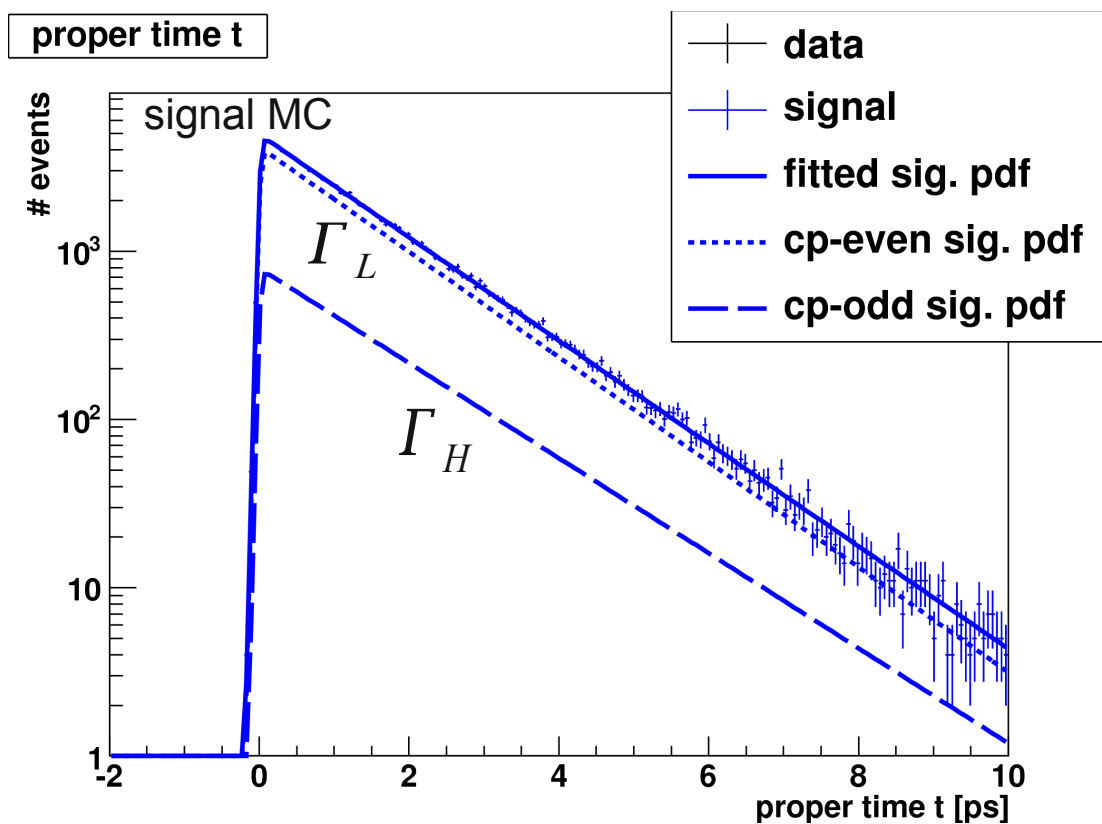


$\cos \psi$



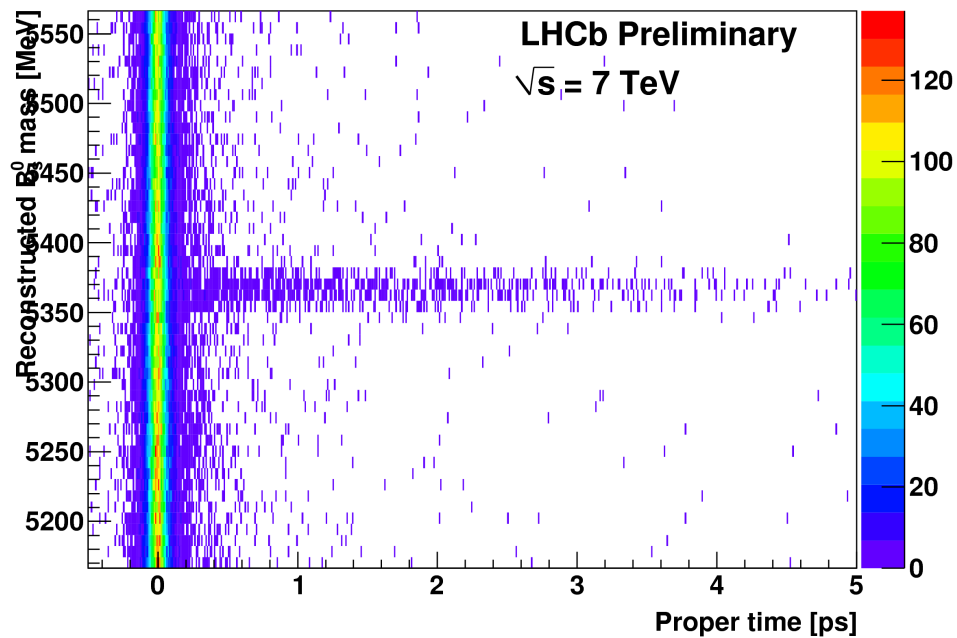
Separation of CP eigenstates

Separation of CP eigenstates allows measurement of Γ_L , Γ_H , $\Delta\Gamma$

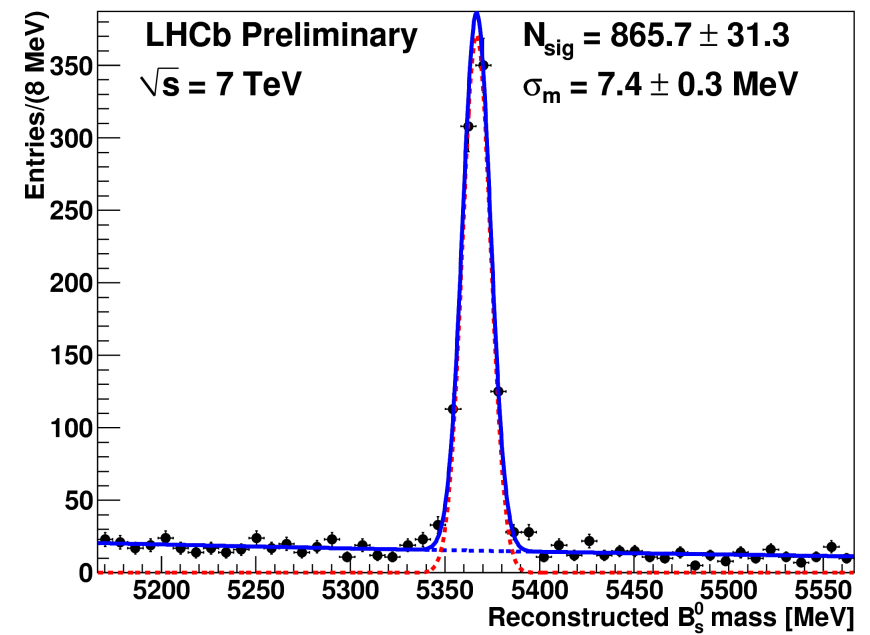


- data corresponds to 37pb^{-1} integrated luminosity
- clean signal for $t > 0.3$ ps
(reduces prompt background)

Proper time vs. Reconstructed B_s^0 mass



B_s^0 mass, $t > 0.30$ ps



Time resolution: fast B_s oscillation needs to be resolved:

$$\Delta m_s = 17.8 \text{ ps}^{-1}$$

$$A_{CP} = -\eta_{CP} \sin \Phi_s \sin(\Delta m \cdot t)$$

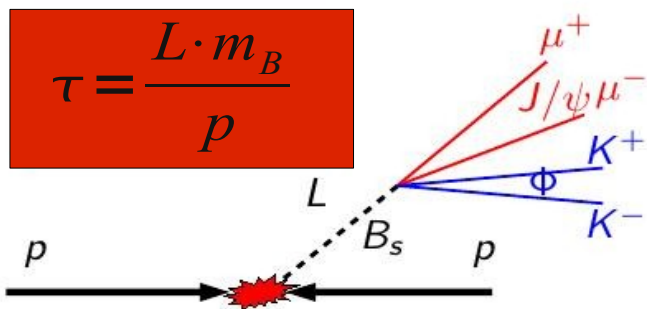
σ_t calibrated from prompt peak

current resolution $\sigma_t \sim 60 \text{ fs}$

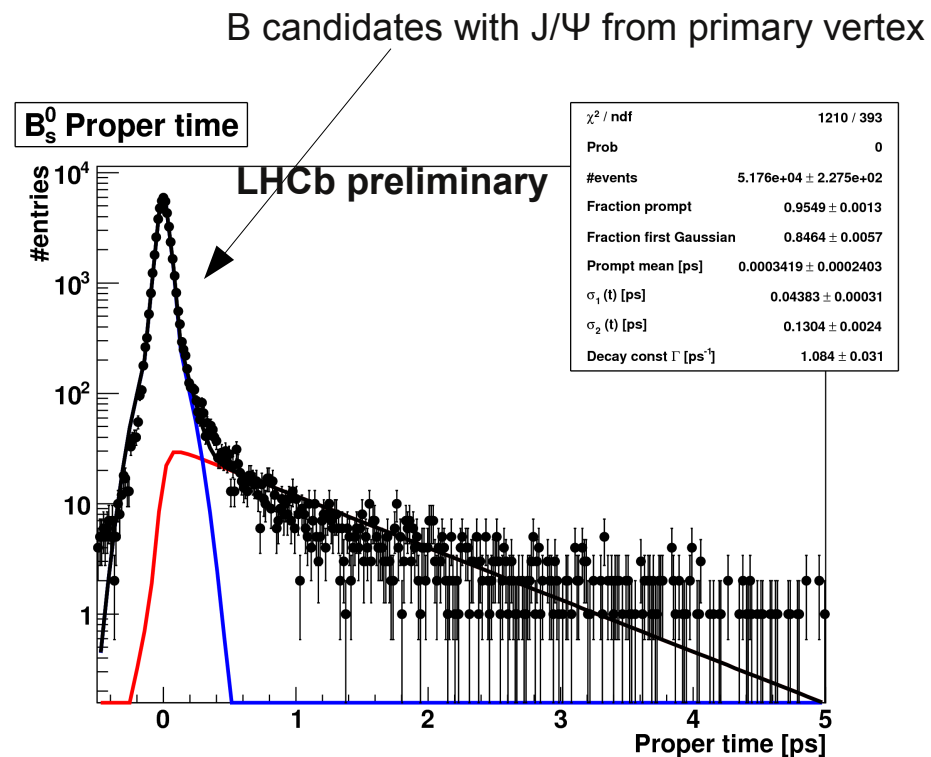
$$L = v \cdot t = \beta \gamma \tau$$

$$\beta = \frac{p}{E}$$

$$\gamma = \frac{E}{m_B}$$



$$\tau = \frac{L \cdot m_B}{p}$$



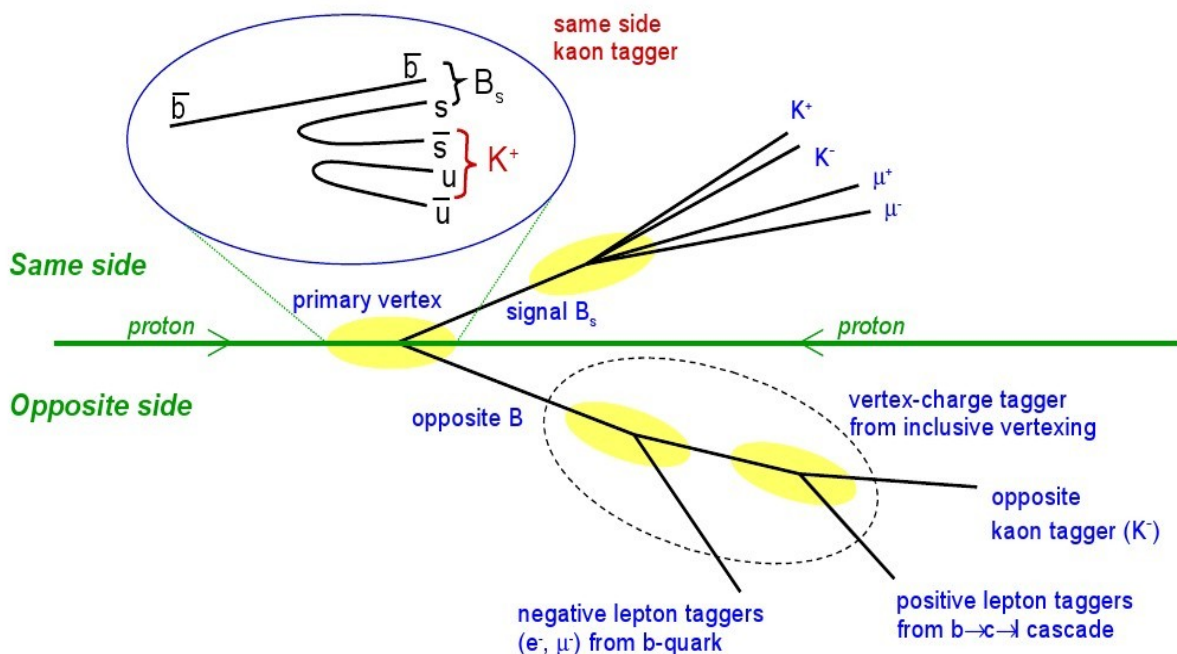
Tagging:

determine flavour of B-meson at production

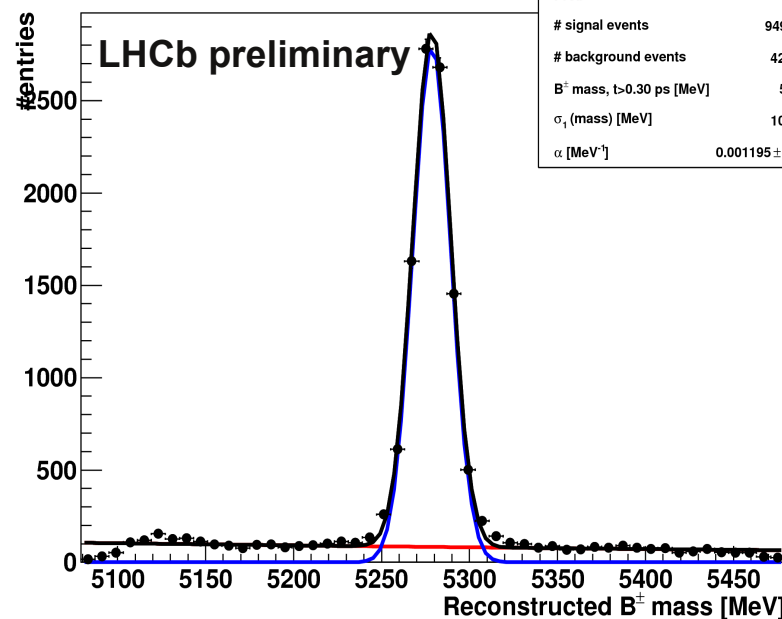
tagging has large impact on A_{CP} $A_{CP} = -\eta_{CP}(1-2\omega)\sin\Phi_s\sin(\Delta m \cdot t)$

efficiency and mistag rate from control channel (e.g. $B^+ \rightarrow J/\Psi K^+$)

mistag probability
(50% \rightarrow no information)



B^\pm mass, $t > 0.30$ ps



detector acceptances: can influence the lifetime and angular distributions
 → check with control channel $B_d \rightarrow J/\Psi K^*$

$B_d \rightarrow J/\Psi K^*$

- same angular analysis as in $B_s \rightarrow J/\Psi \Phi$ ($P \rightarrow VV$)

($J/\Psi \rightarrow \mu\mu$)

→ decay described by three polarisation amplitudes: $A_0, A_{\parallel}, A_{\perp}$

($K^* \rightarrow K \pi$)

- good statistics (650 000 events per 2fb-1)
- already measured precisely by BaBar, Belle, CDF, D0

→ very good cross check for validation of detector acceptances

Parameter	Babar (2007)	Belle (2002)	CDF (2007)	DØ (2009)
$ A_{\parallel} ^2$	$0,211 \pm 0,010 \pm 0,006$	-	$0,211 \pm 0,012 \pm 0,006$	$0,230 \pm 0,013 \pm 0,025$
$ A_0 ^2$	$0,556 \pm 0,009 \pm 0,010$	$0,617 \pm 0,020 \pm 0,027$	$0,569 \pm 0,009 \pm 0,009$	$0,587 \pm 0,011 \pm 0,013$
$ A_{\perp} ^2$	$0,233 \pm 0,010 \pm 0,005$	$0,192 \pm 0,023 \pm 0,026$	-	-
δ_{\parallel} [rad]	$-2,93 \pm 0,08 \pm 0,04$	$2,83 \pm 0,19 \pm 0,08$	$-2,96 \pm 0,08 \pm 0,03$	-
δ_{\perp} [rad]	$2,91 \pm 0,05 \pm 0,03$	$-0,09 \pm 0,13 \pm 0,06$	$2,97 \pm 0,06 \pm 0,01$	-

Selection based on:

transverse momentum cuts

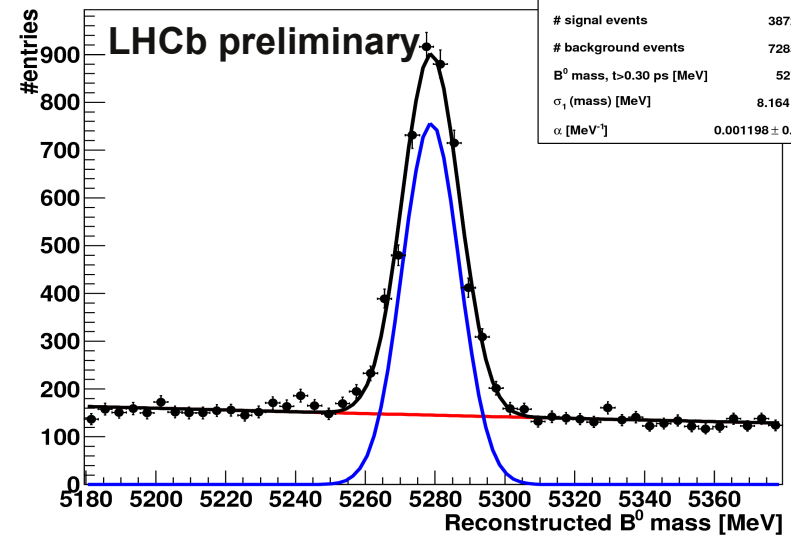
track quality cuts

cuts on quality of vertex reconstruction

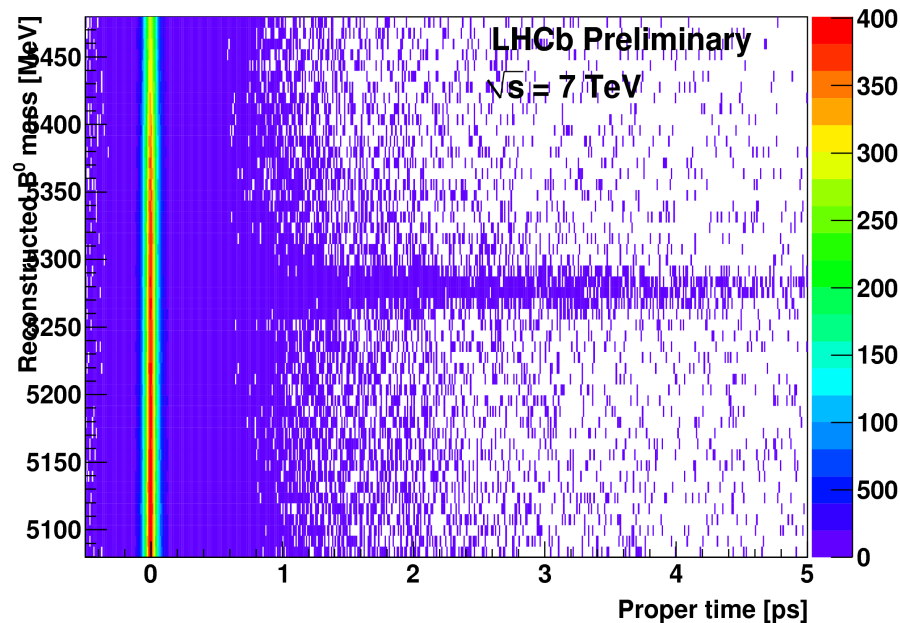
PID cuts

cut on B_d lifetime

B^0 mass, $t > 0.30$ ps



Proper time vs. Reconstructed B^0 mass





For determination of physical parameters:

→ Maximum likelihood method

parameters (physic + detector)

$$\mathcal{L}(\vec{\lambda}) = \prod_i^{all\ events} p_i(\vec{\lambda}, X)$$

↑
↑
 observables
 probability density function (pdf)

Maximizing $\mathcal{L}(\vec{\lambda})$ by variation of $\vec{\lambda}$ maximizes the probability to measure X

$$p(\vec{\lambda}, X) = f_{sig} \cdot S(\vec{\lambda}, X) + (1 - f_{sig}) \cdot B(\vec{\lambda}, X)$$

↑
signal pdf model

↑
background pdf model

Including acceptance effects: $S(\vec{\lambda}, X) \rightarrow \varepsilon(X) \cdot S(\vec{\lambda}, X)$

Perform unbinned maximum likelihood fit to disentangle angular momentum states:

$$\text{Decay rate: } \frac{d^4 \Gamma}{dt d\cos\psi d\phi d\cos\theta} = e^{-\Gamma_d \cdot t} \cdot \sum A_i \cdot f_i(\cos\psi, \cos\theta, \phi)$$

time dependent part
angular dependent part

Observables:

$\cos\theta, \quad \cos\psi, \quad \phi, \quad t$

Physics parameter:

$|A_{\parallel}|^2 \quad |A_{\perp}|^2 \quad \delta_{\parallel} \quad \delta_{\perp} \quad \Gamma_d$

$$A_{\parallel} = |A_{\parallel}| \cdot e^{i\delta_{\parallel}}$$

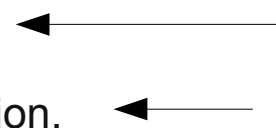
$$A_{\perp} = |A_{\perp}| \cdot e^{i\delta_{\perp}}$$

$$A_0 = |A_0| \cdot e^{i\delta_0}$$

$$|A_{\parallel}|^2 + |A_{\perp}|^2 + |A_0|^2 = 1$$

detector parameters:

time resolution,
mass resolution,
background description,
...



convoluting pdfs with gaussian

fractions, shapes (prompt – longlived)

no CP violation, untagged fit

Perform unbinned maximum likelihood fit to disentangle angular momentum states:

Decay rate:

$$\frac{d^4\Gamma}{dt d\cos\theta d\varphi d\cos\psi} = e^{-\Gamma_d t} \cdot [f_1 |A_0|^2 + f_2 |A_{\parallel}|^2 + f_3 |A_{\perp}|^2 - f_4 A_{\parallel} A_{\perp} \sin(\delta_{\perp} - \delta_{\parallel}) + f_5 A_0 A_{\parallel} \cos\delta_{\parallel} + f_6 A_{\perp} A_0 \sin\delta_{\perp}] .$$

Observables:

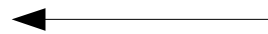
$\cos\theta, \quad \cos\psi, \quad \varphi, \quad t$

Physics parameter:

$|A_{\parallel}|^2, \quad |A_{\perp}|^2, \quad \delta_{\parallel}, \quad \delta_{\perp}, \quad \Gamma_d$

detector parameters:

time resolution,
mass resolution,
background description,
...



convoluting pdfs with gaussian



fractions, shapes (prompt – longlived)

$f_k(\theta, \psi, \varphi)$
$\frac{9}{32\pi} 2 \cos^2 \psi (1 - \sin^2 \theta \cos^2 \varphi)$
$\frac{9}{32\pi} \sin^2 \psi (1 - \sin^2 \theta \sin^2 \varphi)$
$\frac{9}{32\pi} \sin^2 \psi \sin^2 \theta$
$-\frac{9}{32\pi} \sin^2 \psi \sin 2\theta \sin \varphi$
$\frac{9}{32\pi} \frac{1}{\sqrt{2}} \sin 2\psi \sin^2 \theta \sin 2\varphi$
$\frac{9}{32\pi} \frac{1}{\sqrt{2}} \sin 2\psi \sin 2\theta \cos \varphi$

no CP violation, untagged fit

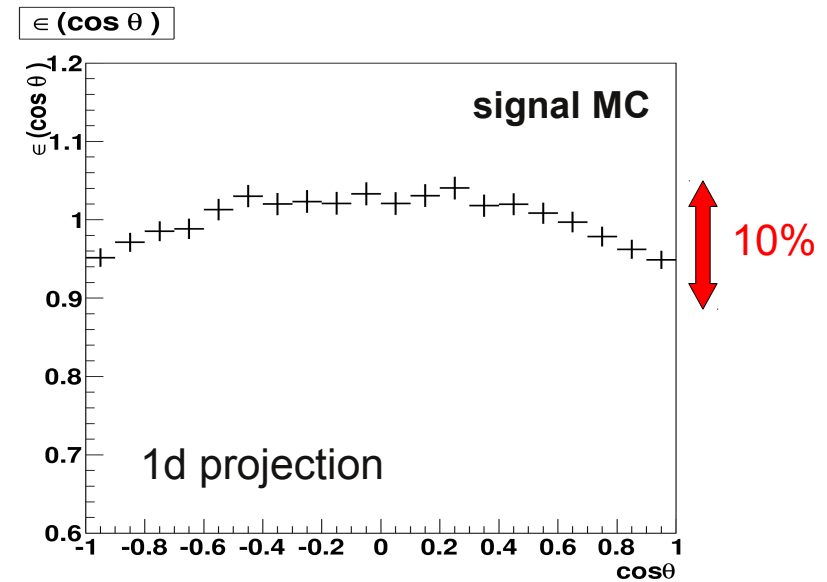
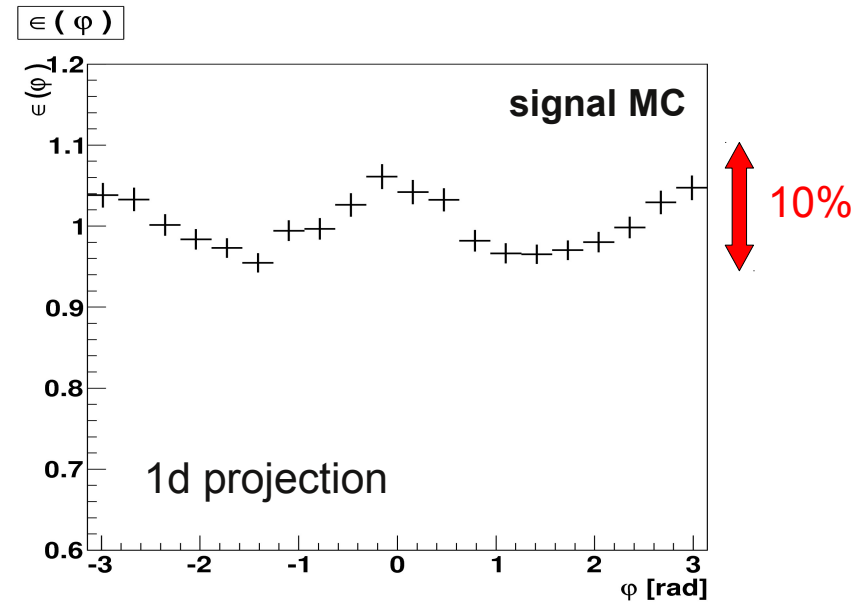
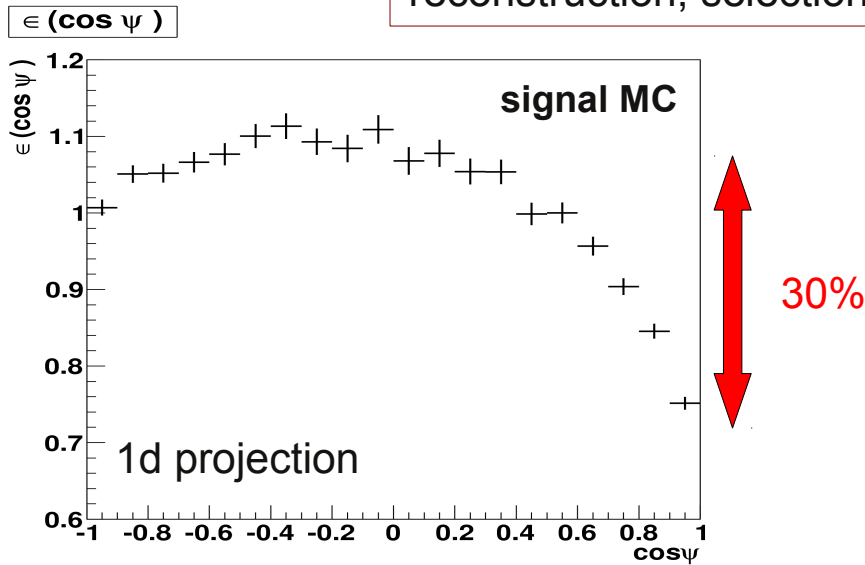


- Angular acceptances deform the signal angular distributions
- Have to calculate angular acceptances from MC

Acceptance calculation: 3 dimensional

$$\epsilon(\cos\theta, \cos\psi, \phi) = \frac{MC \text{ particles}(\cos\theta, \cos\psi, \phi)}{theory \text{ distribution}(\cos\theta, \cos\psi, \phi)}$$

acceptance includes effects of:
reconstruction, selection, trigger,...



How are acceptances determined?

detector angular cut

+

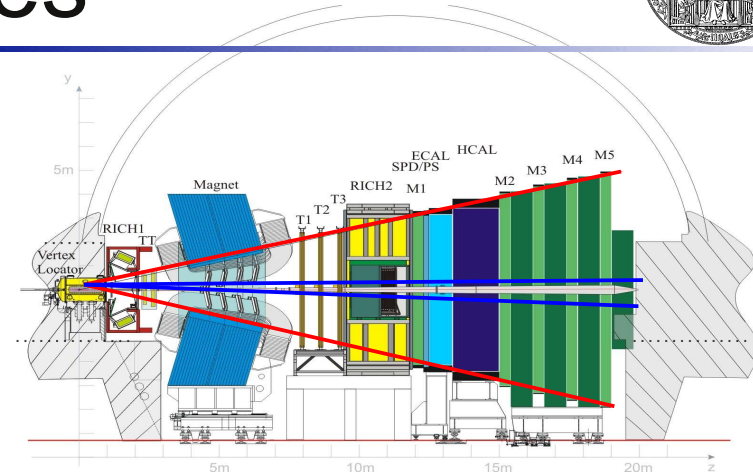
reconstruction

+

selection

+

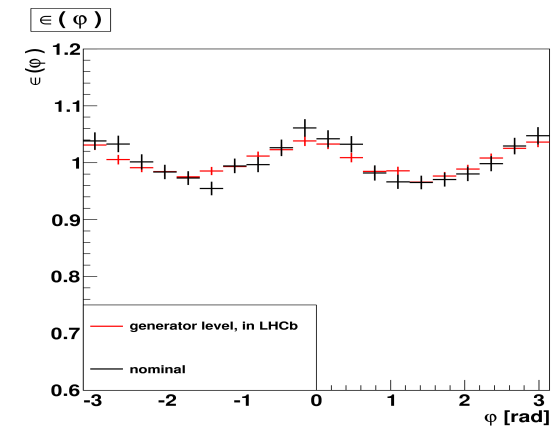
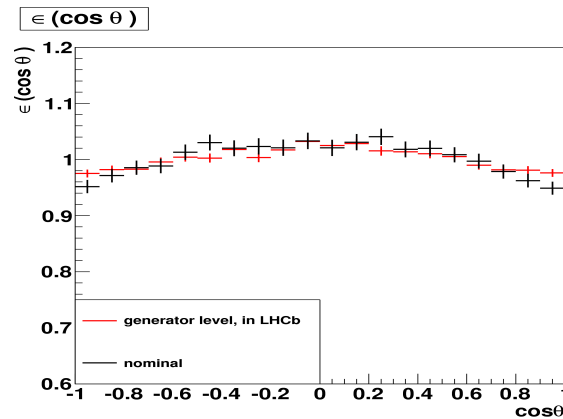
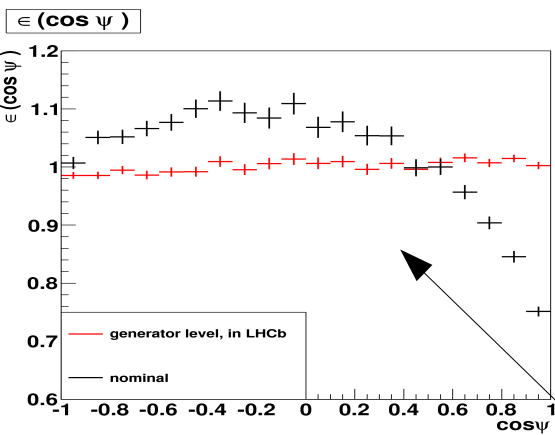
trigger



detector region: $10 \text{ mrad} < \Theta < 400 \text{ mrad}$

Black: include all effects of reconstruction, selection, ...

Red: only detector angular cut



remaining reconstruction effects

How are acceptances determined?

detector angular cut

+

reconstruction

+

selection

+

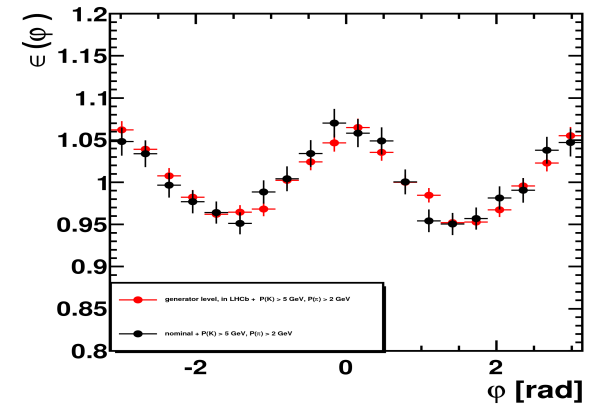
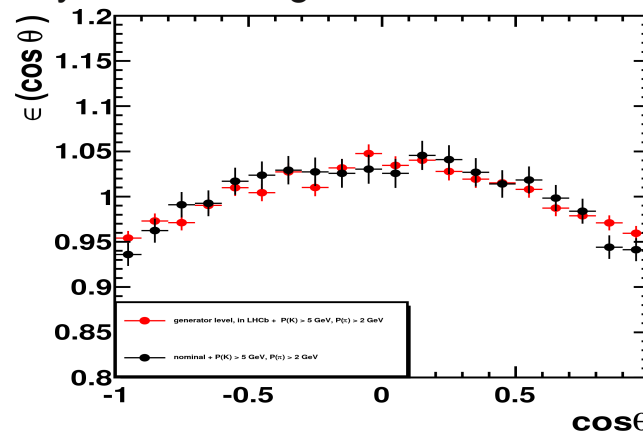
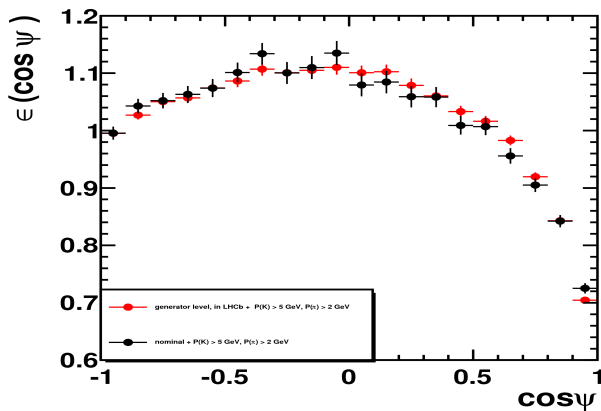
trigger

implicit momentum cut in reconstruction!

→ apply cut on $P(K) > 5\text{ GeV}$
 $P(\pi) > 2\text{ GeV}$

Black: include all effects of reconstruction, selection, ...

Red: only detector angular cut + momentum cuts



How are acceptances determined?

detector angular cut

+

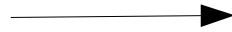
reconstruction

+

selection

+

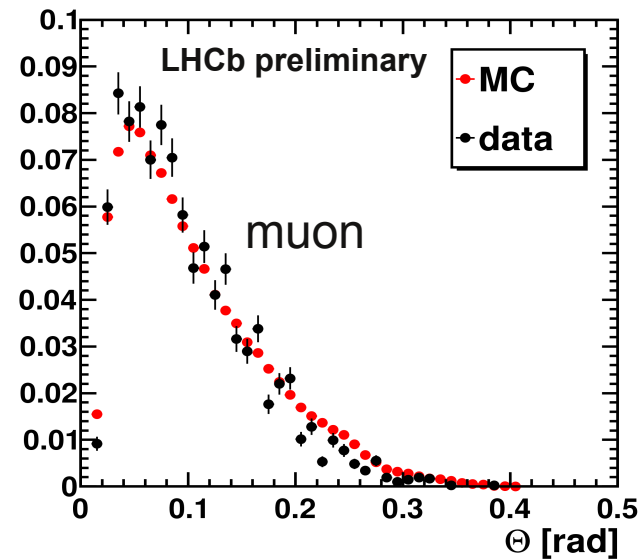
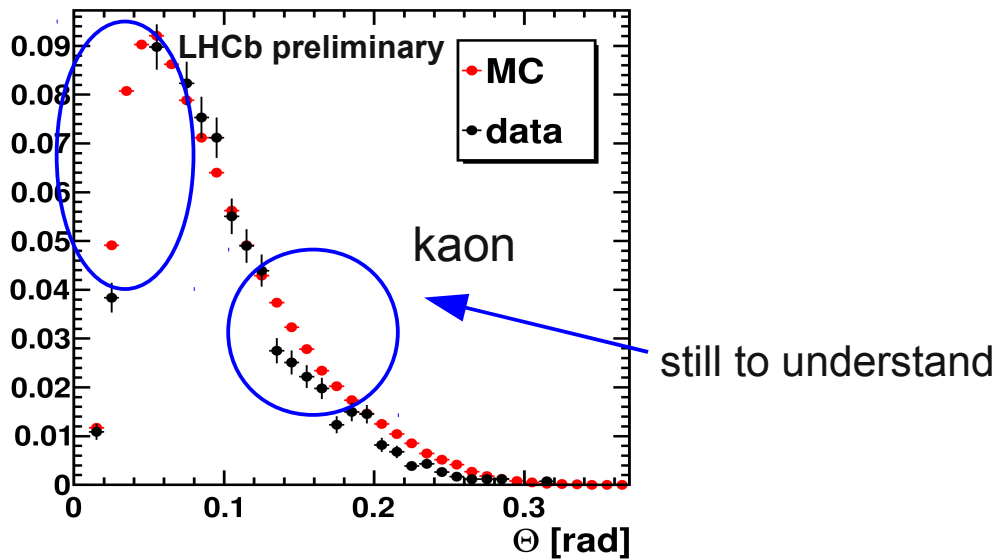
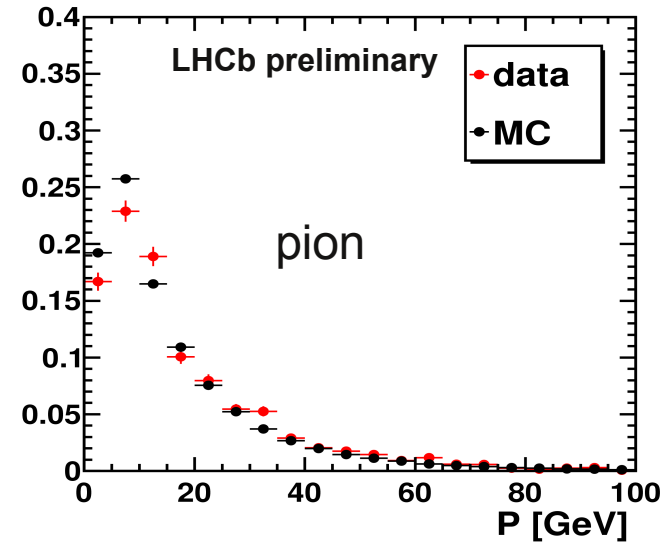
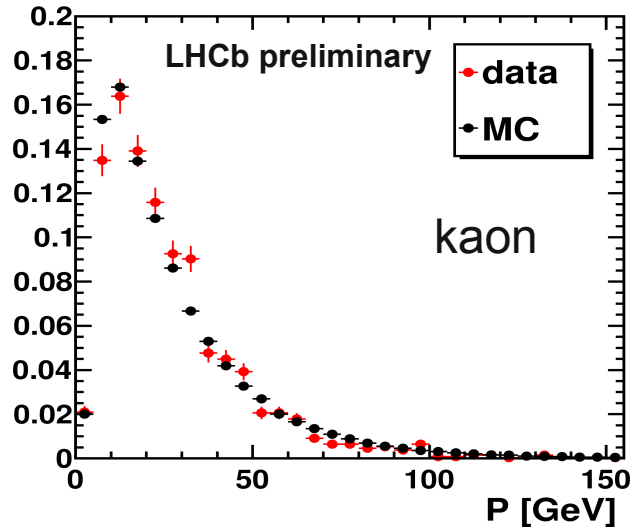
trigger



only very small effects

→ acceptance determined by detector angular cut and momentum cut in reconstruction

How large is the difference between data and MC in these variables?



How can we estimate the systematic uncertainties due to acceptance calculation?

→ toy experiments simulating wrong acceptances:

Acceptance modification	deviation in σ_{stat} from nominal value			
	$ A_{\parallel} ^2$	$ A_{\perp} ^2$	δ_{\parallel}	δ_{\perp}
changing detector cut:				
12.5 mrad < Θ < 375 mrad	0.07	0.20	0.13	0.14
15 mrad < Θ < 350 mrad	0.06	0.25	0.01	0.04
changing momentum cut:				
P (K) > 4.9 GeV P (π) > 1.9 GeV	0.10	0.10	0.13	0.10
P (K) > 5.1 GeV P (π) > 2.1 GeV	0.10	0.24	0.15	0.13

no large deviations compared to statistical error

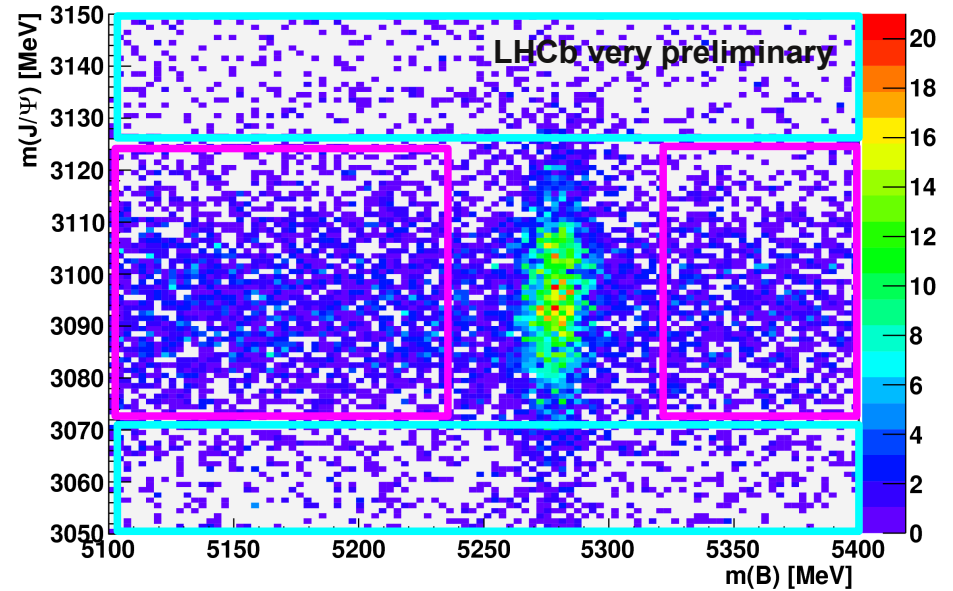
→ have to assign only small systematic uncertainties due to acceptance description

Different background sources:

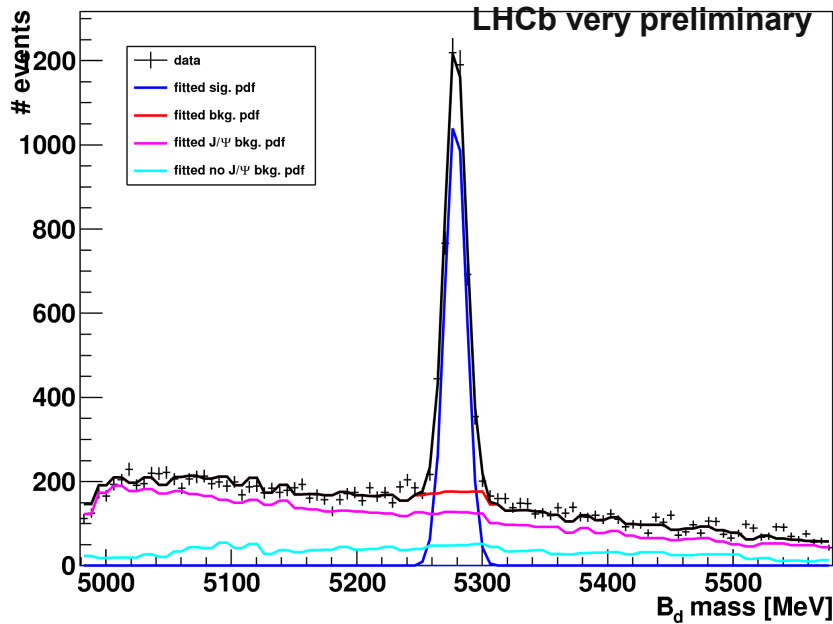
B candidates from real J/Ψ

background from other combinatorics

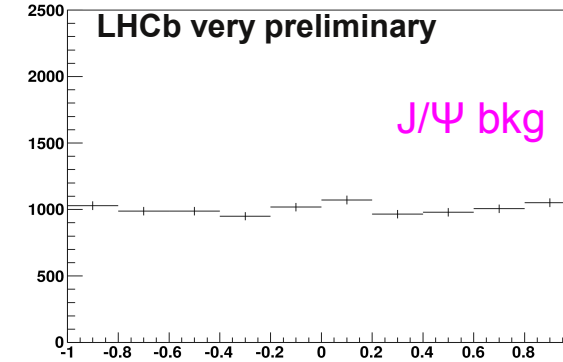
→ different angular distributions



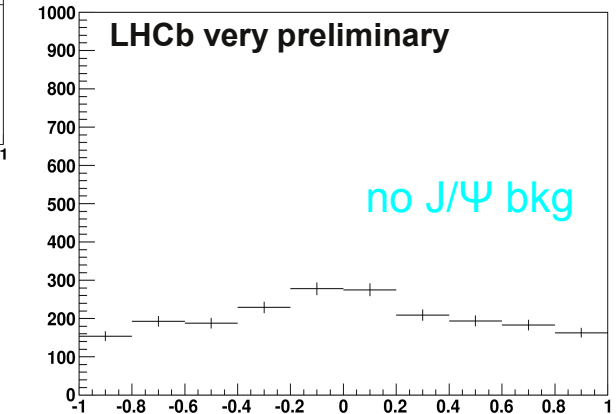
Reconstructed B_d mass



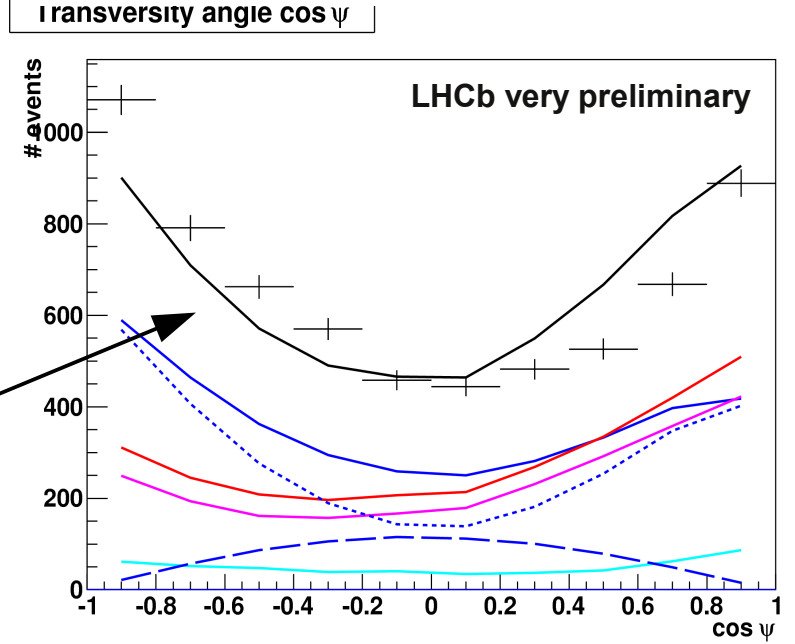
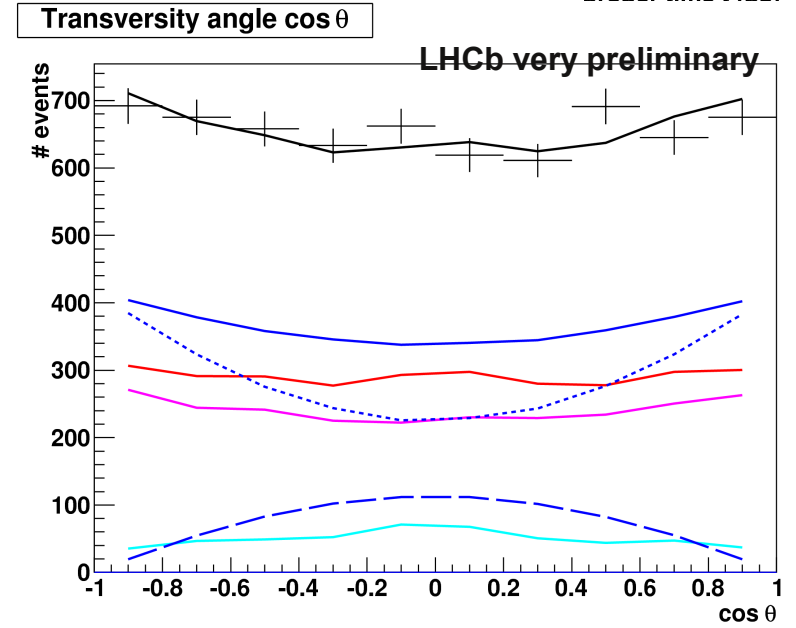
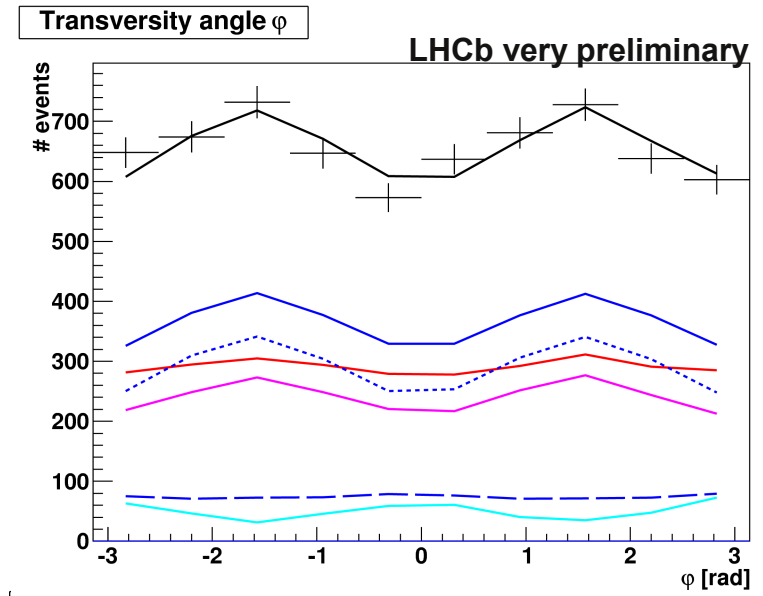
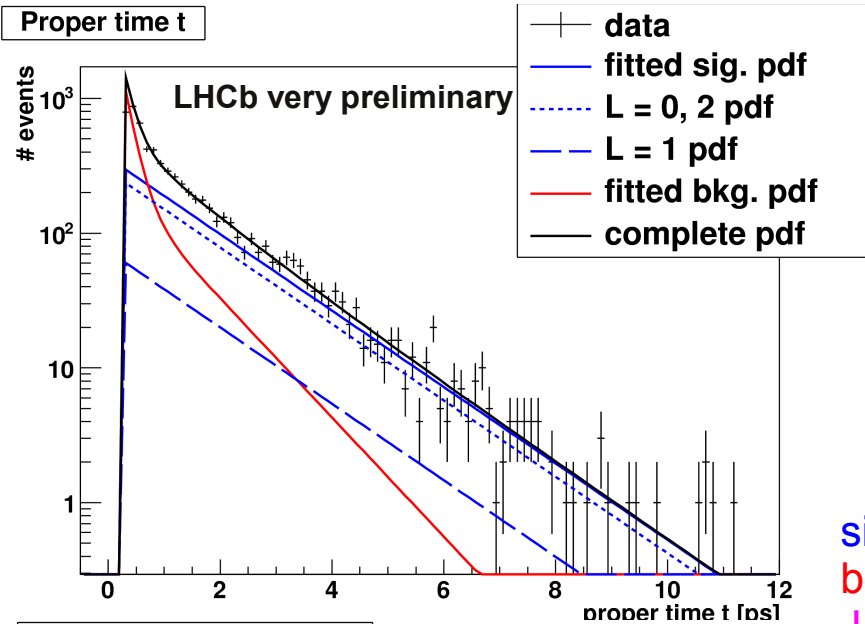
$\cos(\theta)$ Sig



$\cos(\theta)$ Sig



$B_d \rightarrow J/\Psi K^*$ fit projections



signal pdf
background pdf
J/ Ψ bkg pdf
no J/ Ψ bkg pdf

still to understand

Expected sensitivity on the polarisation amplitudes:

for 37 pb⁻¹

parameter	sensitivity
$ A_{\parallel} ^2$	0.021
$ A_{\perp} ^2$	0.020
δ_{\parallel}	0.12
δ_{\perp}	0.099

for 2 fb⁻¹

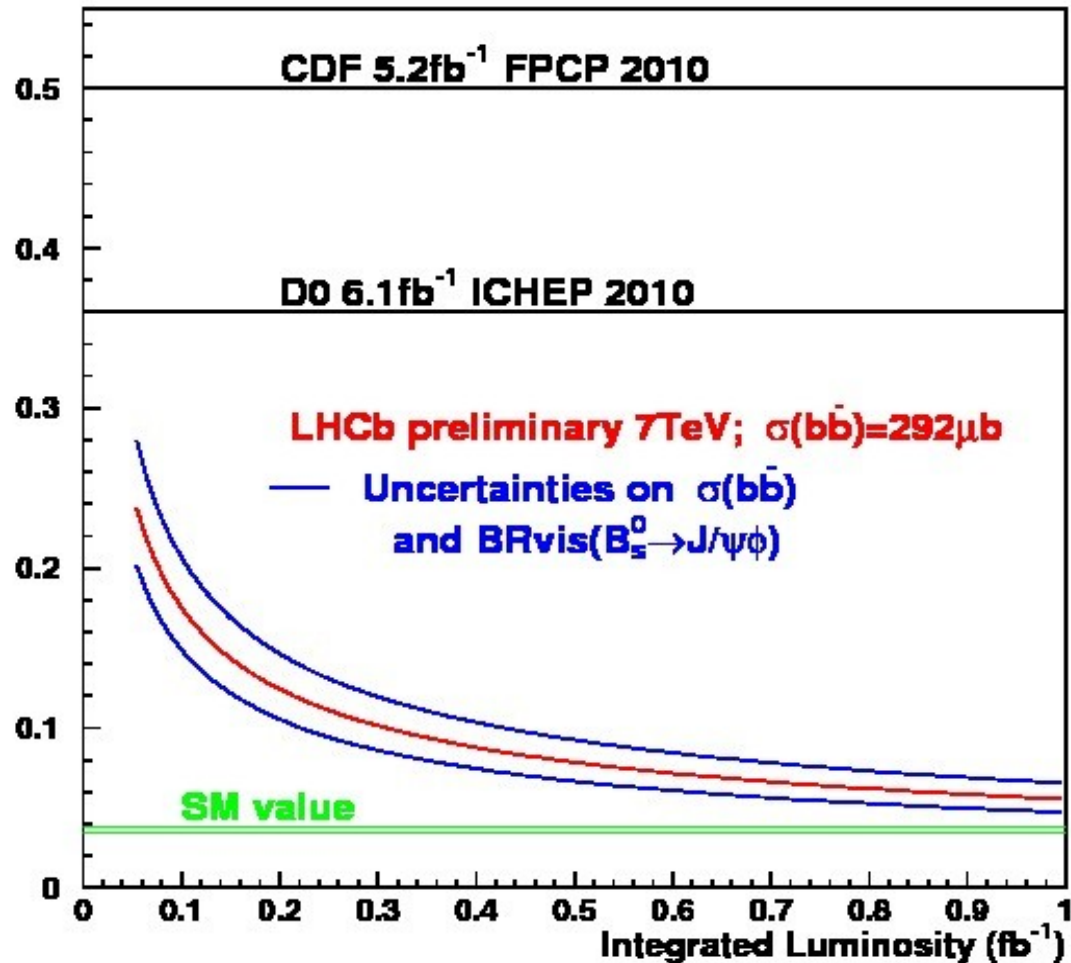
parameter	sensitivity
$ A_{\parallel} ^2$	0.001
$ A_{\perp} ^2$	0.001
δ_{\parallel}	0.007
δ_{\perp}	0.006

parameter	sensitivity			
	Babar (2007) stat. / syst.	Belle (2002) stat. / syst.	CDF (2007) stat. / syst.	DØ (2009) stat. / syst.
$ A_{\parallel} ^2$	0.010 / 0.006	-	0.012 / 0.006	0.013 / 0.025
$ A_{\perp} ^2$	0.009 / 0.010	0.020 / 0.027	0.009 / 0.009	0.011 / 0.013
δ_{\parallel}	0.08 / 0.04	0.19 / 0.08	0.08 / 0.03	-
δ_{\perp}	0.05 / 0.03	0.13 / 0.06	0.06 / 0.01	-

→ with current statistics not yet competitive with other experiments

→ with 2fb-1 larger statistical sensitivity

Important ingredients: proper time resolution, tagging efficiency, acceptances



Monte Carlo assumptions:

- proper time resolution:

$$\sigma_t = 0.038 \text{ ps}$$

(in data still $\sim 1.3x$ worse)

- tagging efficiency:

$$\varepsilon D^2 = 6.2\%$$

(not yet calibrated with data)



- B_s meson system offers probability to search for New Physics
 - CP violation is a very sensitive observable
- The prototype channel to search for New Physics is $B_s \rightarrow J/\Psi \Phi$
Very involved analysis, requires many steps:

proper time calibration

tagging calibration

detector acceptances



my current work: measuring the polarisation amplitudes in $B_d \rightarrow J/\Psi K^*$

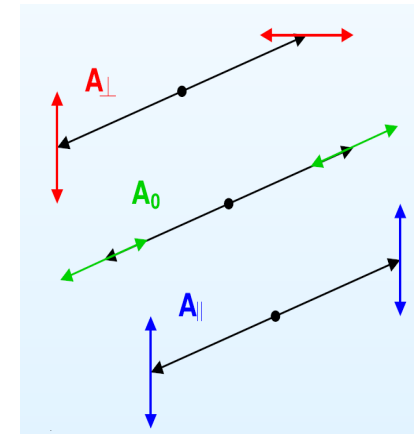
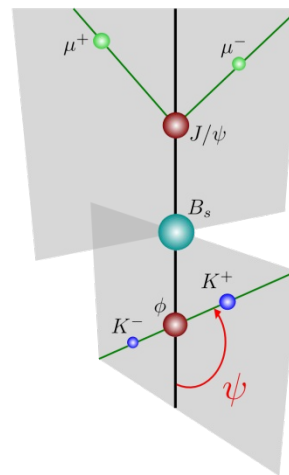
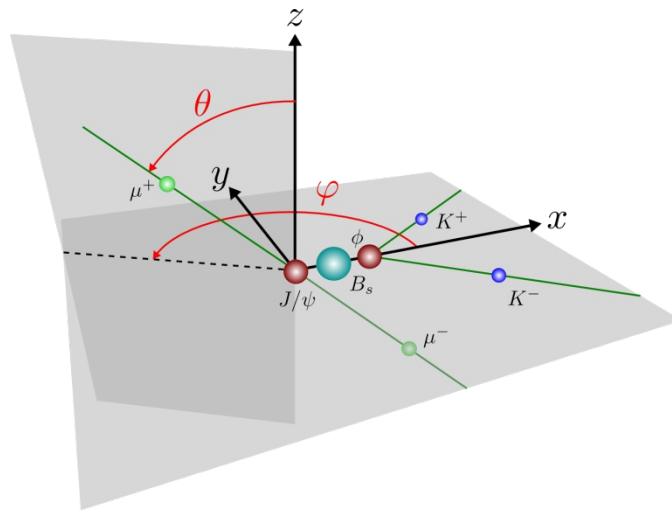
test the angular acceptances

first results shown today → hope to have publishable results by March 2011

BACKUP

Transversity Basis

- B_s is a pseudo scalar (spin=0), ϕ and J/ψ are vectors mesons ($JPC = 1---$)
- Total angular momentum conservation \square
in the B_s rest frame, ϕ and J/ψ have relative orbital momentum $\ell = 0, 1, 2$
- Since $CP|J/\psi\rangle = (-1)^\ell|J/\psi\rangle$,
final state is mixture of CP even ($\ell=0, 2$) and CP odd ($\ell=1$)
- Decompose decay amplitudes in term of linear polarization, when J/ψ and ϕ are:
 - A_0 : longitudinally polarized (CP-even)
 - A_\perp : transversely polarized and \perp to each other (CP-odd)
 - A_\parallel : transversely polarized and \parallel to each other (CP-even)
- \square 3 angles θ, ϕ, ψ describe directions of final decay products $J/\psi \rightarrow \mu\mu$, $\phi \rightarrow K+K$



3131